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## Title:Control System-Second Order System

```
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%Date:10/04/2021
%Version:1.4
```

## This Document has equation for DC Motor

```
%Equation:Ldi/dt+Ri+Kw=V
%          Jdw/dt+bw=Ki
%T(s)=(K/LJ)/(s^2+((b/J)+(R/L)s+(R*b)/(L*J)+(K*K)/(L*J))
```

## Math analysis

```
%dependent variables:w
%independent variables:t
%constant:K,R,L,J,b
%Roots:0.5*(-(b/J)-(R/L))+sqrt(((b*b)/(J*J))+((R*R)/(L*L))-((2*R*b)/(L*J))-((4*K*K)/(L*J)))
%          0.5*(-(b/J)-(R/L))-sqrt(((b*b)/(J*J))+((R*R)/(L*L))-((2*R*b)/(L*J))-((4*K*K)/(L*J)))
```

## Negtaive Feedback

```
J = 0.01;
b = 0.1;
K = 1;
R = 1;
L = 0.5;
TF=tf([K/(J*L)],[1,((b/J)+(R/L)),((K*K)+(R*b))/(L*J)]);
CF=10
sys = CF*TF
NCTF1=feedback(sys,1)
subplot(3,2,1)
step(NCTF1)
title("Step with negative")
subplot(3,2,2)
impulse(NCTF1)
title("impulse with negative")
S = stepinfo(NCTF1)
```

---

```
[wn,zeta]=damp(NCTF1)
```

```
J = 0.01;
b = 0.1;
K = 1;
R = 1;
L = 0.5;
TF=tf([K/(J*L)], [1, ((b/J)+(R/L)), ((K*K)+(R*b))/(L*J)]);
CF=tf([1,0],[1])
sys = CF*TF
NCTF2=feedback(sys,1)
subplot(3,2,3)
step(NCTF2)
title("Step with diff")
subplot(3,2,4)
impulse(NCTF2)
title("impulse with diff")
S = stepinfo(NCTF2)
[wn,zeta]=damp(NCTF2)
```

```
J = 0.01;
b = 0.1;
K = 1;
R = 1;
L = 0.5;
TF=tf([K/(J*L)], [1, ((b/J)+(R/L)), ((K*K)+(R*b))/(L*J)]);
CF=tf([1],[1,0])
sys = CF*TF
NCTF3=feedback(sys,1)
subplot(3,2,5)
step(NCTF3)
title("Step with integrator")
subplot(3,2,6)
impulse(NCTF3)
title("impulse with integrator")
S = stepinfo(NCTF3)
[wn,zeta]=damp(NCTF3)
```

```
CF =
```

```
10
```

```
sys =
```

```
2000
```

```
-----
s^2 + 12 s + 220
```

---

Continuous-time transfer function.

NCTF1 =

$$\frac{2000}{s^2 + 12 s + 2220}$$

Continuous-time transfer function.

S =

struct with fields:

RiseTime: 0.0245  
SettlingTime: 0.6206  
SettlingMin: 0.4993  
SettlingMax: 1.5026  
Overshoot: 66.7860  
Undershoot: 0  
Peak: 1.5026  
PeakTime: 0.0667

wn =

47.1169  
47.1169

zeta =

0.1273  
0.1273

CF =

s

Continuous-time transfer function.

sys =

$$\frac{200 s}{s^2 + 12 s + 2220}$$

Continuous-time transfer function.

---

*NCTF2 =*

$$\frac{200\ s}{s^2 + 212\ s + 220}$$

*Continuous-time transfer function.*

*S =*

*struct with fields:*

*RiseTime: 0*  
*SettlingTime: 3.7813*  
*SettlingMin: 6.5963e-04*  
*SettlingMax: 0.9234*  
*Overshoot: Inf*  
*Undershoot: 0*  
*Peak: 0.9234*  
*PeakTime: 0.0253*

*wn =*

*1.0429*  
*210.9571*

*zeta =*

*1*  
*1*

*CF =*

*1*  
*-*  
*s*

*Continuous-time transfer function.*

*sys =*

$$\frac{200}{s^3 + 12\ s^2 + 220\ s}$$

*Continuous-time transfer function.*

---

*NCTF3* =

$$\frac{200}{s^3 + 12 s^2 + 220 s + 200}$$

*Continuous-time transfer function.*

*S* =

*struct with fields:*

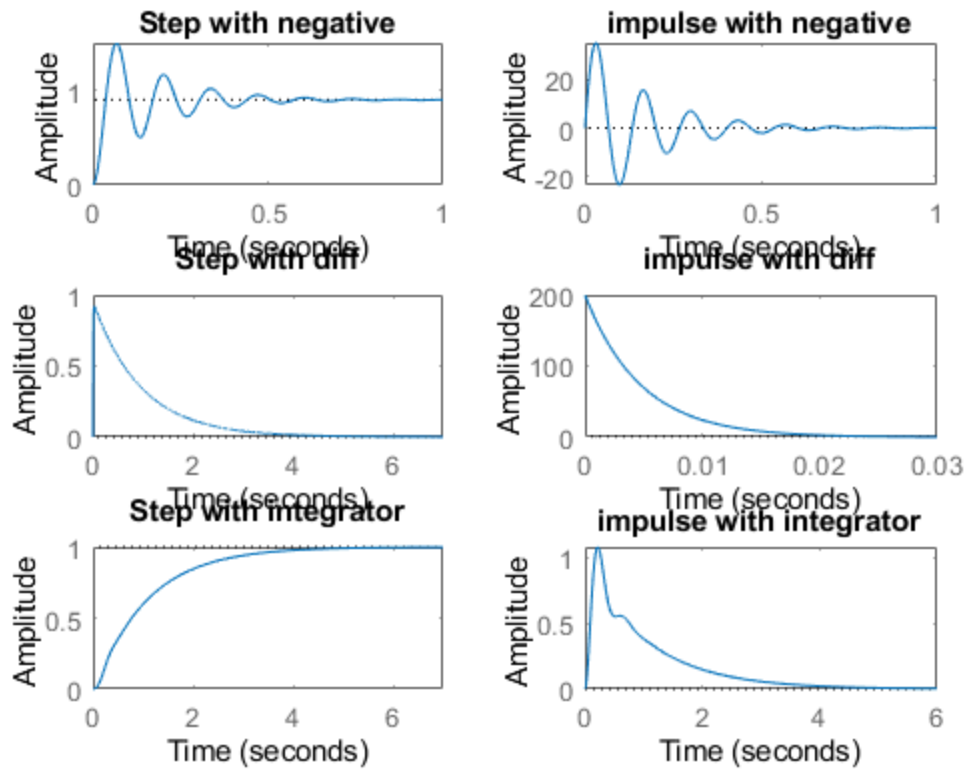
*RiseTime: 2.2719*  
*SettlingTime: 4.1463*  
*SettlingMin: 0.9044*  
*SettlingMax: 0.9993*  
*Overshoot: 0*  
*Undershoot: 0*  
*Peak: 0.9993*  
*PeakTime: 7.6683*

*wn* =

*0.9549*  
*14.4725*  
*14.4725*

*zeta* =

*1.0000*  
*0.3816*  
*0.3816*



## Positive Feedback

```
figure
J = 0.01;
b = 0.1;
K = 1;
R = 1;
L = 0.5;
TF=tf([K/(J*L)], [1, ((b/J)+(R/L)), ((K*K)+(R*b))/(L*J)]);
CF=10
sys = CF*TF
PCTF1=feedback(sys,-1)
subplot(3,2,1)
step(PCTF1)
title("Step with positive")
subplot(3,2,2)
impulse(PCTF1)
title("impulse with positive")
S = stepinfo(PCTF1)
[wn,zeta]=damp(PCTF1)

J = 0.01;
b = 0.1;
```

---

```

K = 1;
R = 1;
L = 0.5;
TF=tf([K/(J*L)], [1, ((b/J)+(R/L)), ((K*K)+(R*b))/(L*J) ]);
CF=tf([1,0],[1])
sys = CF*TF
PCTF2=feedback(sys,-1)
subplot(3,2,3)
step(PCTF2)
title("Step with diff")
subplot(3,2,4)
impulse(PCTF2)
title("impulse with diff")
S = stepinfo(PCTF2)
[wn,zeta]=damp(PCTF2)

```

```

J = 0.01;
b = 0.1;
K = 1;
R = 1;
L = 0.5;
TF=tf([K/(J*L)], [1, ((b/J)+(R/L)), ((K*K)+(R*b))/(L*J) ]);
CF=tf([1],[1,0])
sys = CF*TF
PCTF3=feedback(sys,-1)
subplot(3,2,5)
step(PCTF3)
title("Step with integrator")
subplot(3,2,6)
impulse(PCTF3)
title("impulse with integrator")
S = stepinfo(PCTF3)
[wn,zeta]=damp(PCTF3)

```

$CF =$

10

$sys =$

$$\frac{2000}{s^2 + 12s + 220}$$

Continuous-time transfer function.

$PCTF1 =$

---


$$\frac{2000}{s^2 + 12s - 1780}$$

Continuous-time transfer function.

$S =$

struct with fields:

RiseTime: NaN  
 SettlingTime: NaN  
 SettlingMin: NaN  
 SettlingMax: NaN  
 Overshoot: NaN  
 Undershoot: NaN  
 Peak: Inf  
 PeakTime: Inf

$\omega_n =$

36.6146  
 48.6146

$\zeta =$

-1  
 1

$CF =$

$s$

Continuous-time transfer function.

$sys =$

$$\frac{200s}{s^2 + 12s + 220}$$

Continuous-time transfer function.

$PCTF2 =$

$$\frac{200s}{s^2 - 188s + 220}$$



---

Continuous-time transfer function.

$S =$

struct with fields:

RiseTime: NaN  
SettlingTime: NaN  
SettlingMin: NaN  
SettlingMax: NaN  
Overshoot: NaN  
Undershoot: NaN  
Peak: Inf  
PeakTime: Inf

$\omega_n =$

1.1776  
186.8224

$\zeta =$

-1  
-1

$CF =$

1  
-  
s

Continuous-time transfer function.

$sys =$

200  
-----  
 $s^3 + 12 s^2 + 220 s$

Continuous-time transfer function.

$PCTF3 =$

200  
-----  
 $s^3 + 12 s^2 + 220 s - 200$

---

*Continuous-time transfer function.*

*S =*

*struct with fields:*

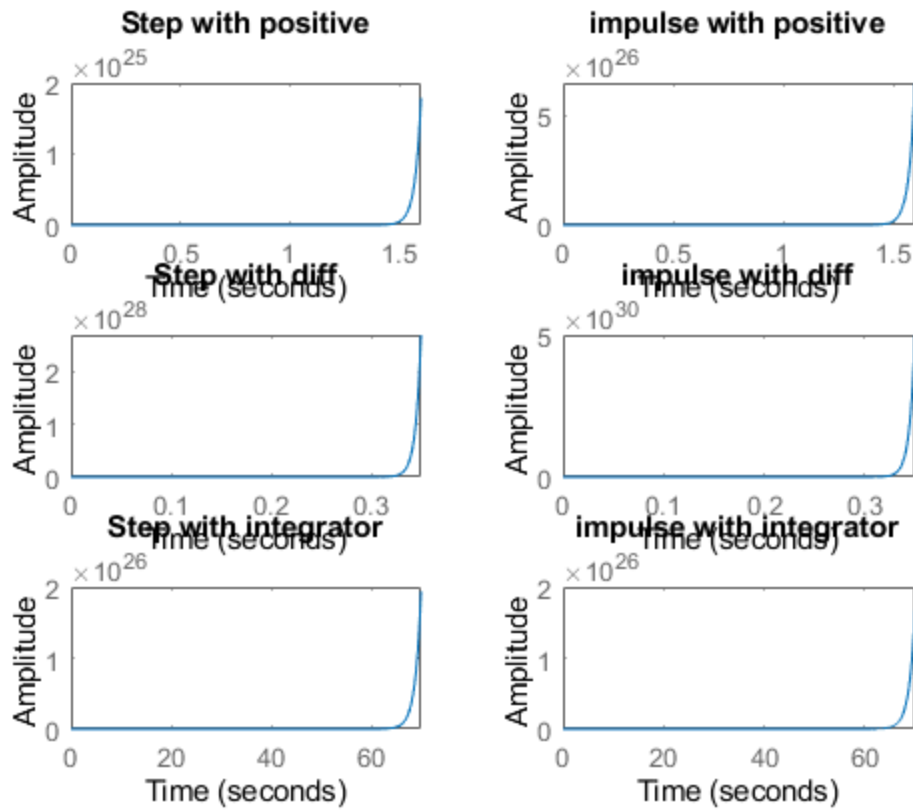
*RiseTime: NaN*  
*SettlingTime: NaN*  
*SettlingMin: NaN*  
*SettlingMax: NaN*  
*Overshoot: NaN*  
*Undershoot: NaN*  
*Peak: Inf*  
*PeakTime: Inf*

*wn =*

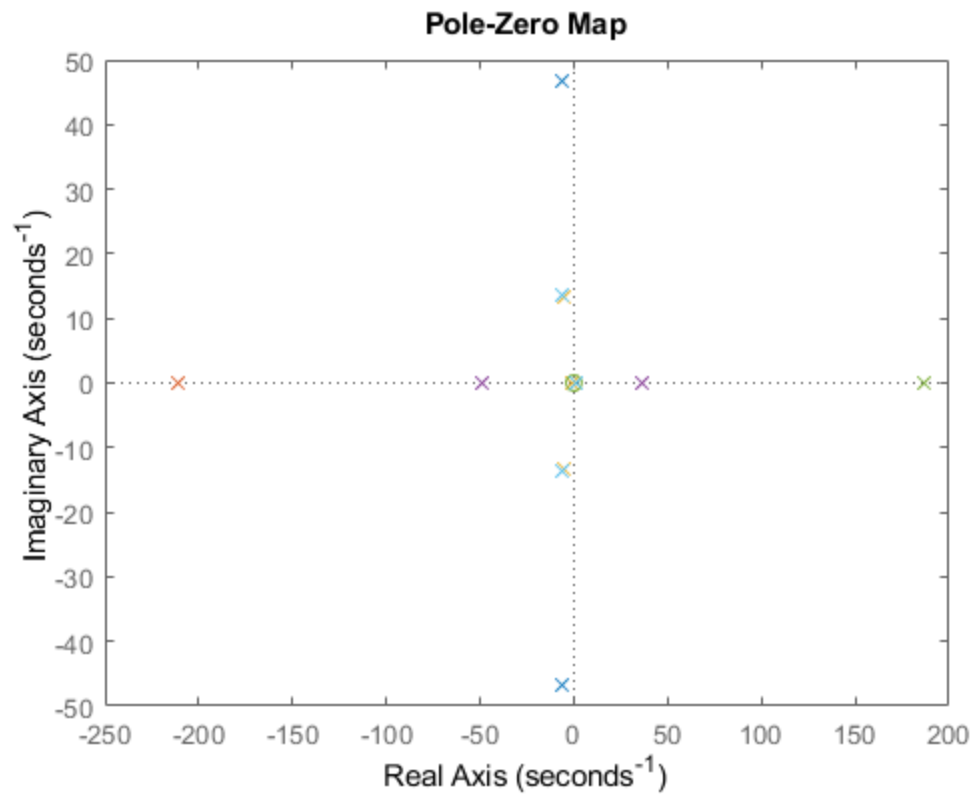
*0.8653*  
*15.2030*  
*15.2030*

*zeta =*

*-1.0000*  
*0.4231*  
*0.4231*



```
figure
hold on
pzmap(NCTF1)
pzmap(NCTF2)
pzmap(NCTF3)
pzmap(PCTF1)
pzmap(PCTF2)
pzmap(PCTF3)
```



## Analysis

- %1. Positive feedback system when P,I,D are added system becomes unstable.
- %2. Rise time will decrease when you add a differentiator because overshoot increases,  $T_s$  also increases.
- %3. When we add an integrator to this system rise time became higher and overshoot became zero this says that system is getting towards stable.
- %4. Adding the positive feed back makes the zeta value change.

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