

3(a) Second Order Population Growth system

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Plant Description

It is a exponential increasing system of a Population Growth Equation- $\frac{dN(t)}{dt} = kN(t)$ N =Population a time t , k =constant, t =time Values- $k=0.14$, $A=200$

Without Controller

```
clc;
k= 0.14;
A= 200;
sys = tf([k*A],[1,k,0])
figure(1);
subplot(3,1,1);
impz(sys);
title('Impulse Input');
subplot(3,1,2);
step(sys);
title('Step Input');
[z,p,k] = tf2zp([k*A],[1,k,0])
subplot(3,1,3);
zplane(z,p);
s = stepinfo(sys)
```

sys =

$$\frac{28}{s^2 + 0.14 s}$$

Continuous-time transfer function.

z =

0x1 empty double column vector

p =

0
-0.1400

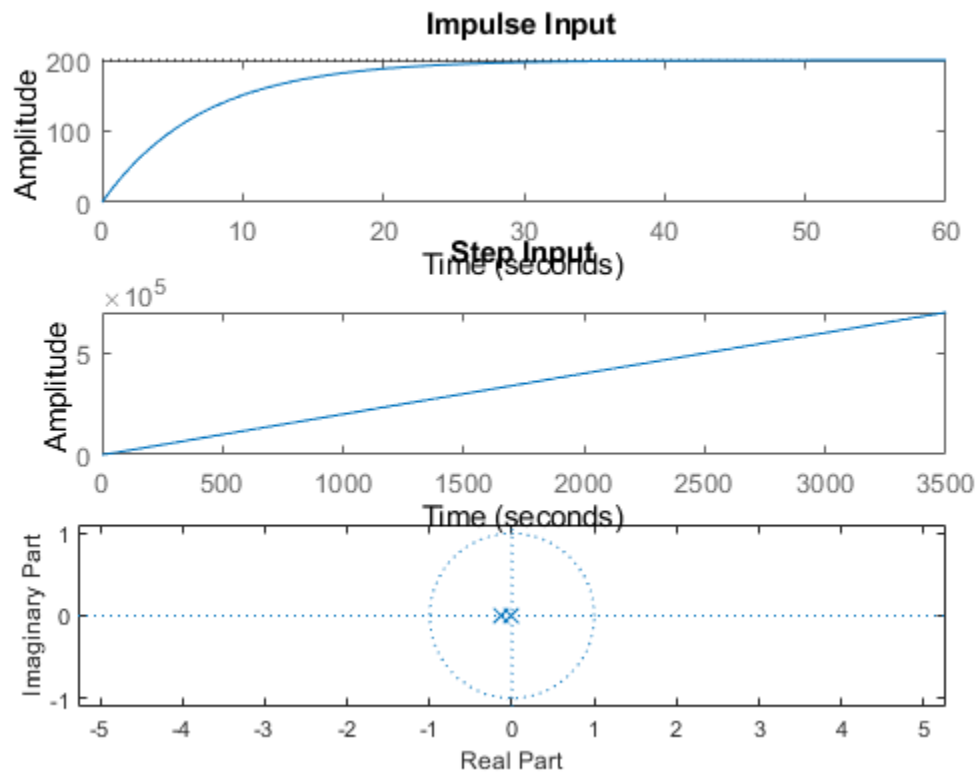
k =

28.0000

s =

struct with fields:

RiseTime: NaN
SettlingTime: NaN
SettlingMin: NaN
SettlingMax: NaN
Overshoot: NaN
Undershoot: NaN
Peak: Inf
PeakTime: Inf



Open Loop with Controller (P)

```
P= 2;  
sys = tf([P*(k)*A],[1,k,0])  
figure(2);  
subplot(3,1,1);  
impz(sys);  
title('Impulse Input');  
subplot(3,1,2);  
step(sys);  
title('Step Input');  
[z,p,k] = tf2zp([P*k*A],[1,k,0])  
subplot(3,1,3);  
zplane(z,p);  
S = stepinfo(sys)
```

sys =

```
1.12e04  
-----  
s^2 + 28 s
```

Continuous-time transfer function.

z =

0x1 empty double column vector

p =

```
0  
-28.0000
```

k =

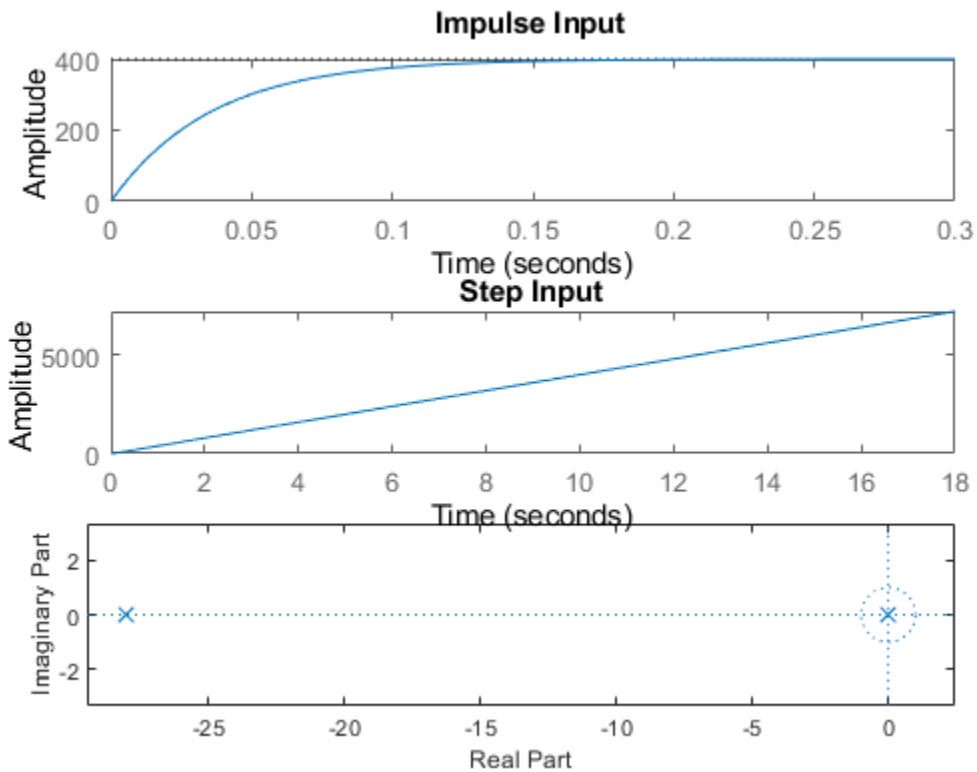
```
1.1200e+04
```

S =

struct with fields:

```
RiseTime: NaN  
SettlingTime: NaN  
SettlingMin: NaN  
SettlingMax: NaN  
Overshoot: NaN  
Undershoot: NaN  
Peak: Inf
```

PeakTime: Inf



Open Loop with Controller (I)

```
sys = tf([k*A],[1,k,0,0])
figure(3);
subplot(3,1,1);
impz(sys);
title('Impulse Input');
subplot(3,1,2);
step(sys);
title('Step Input');
[z,p,k] = tf2zp([k*A],[1,k,0,0])
subplot(3,1,3);
zplane(z,p);
S = stepinfo(sys)
```

sys =

```
      2.24e06
-----
s^3 + 1.12e04 s^2
```

Continuous-time transfer function.

z =

0x1 empty double column vector

p =

1.0e+04 *

0

0

-1.1200

k =

2.2400e+06

s =

struct with fields:

RiseTime: NaN

SettlingTime: NaN

SettlingMin: NaN

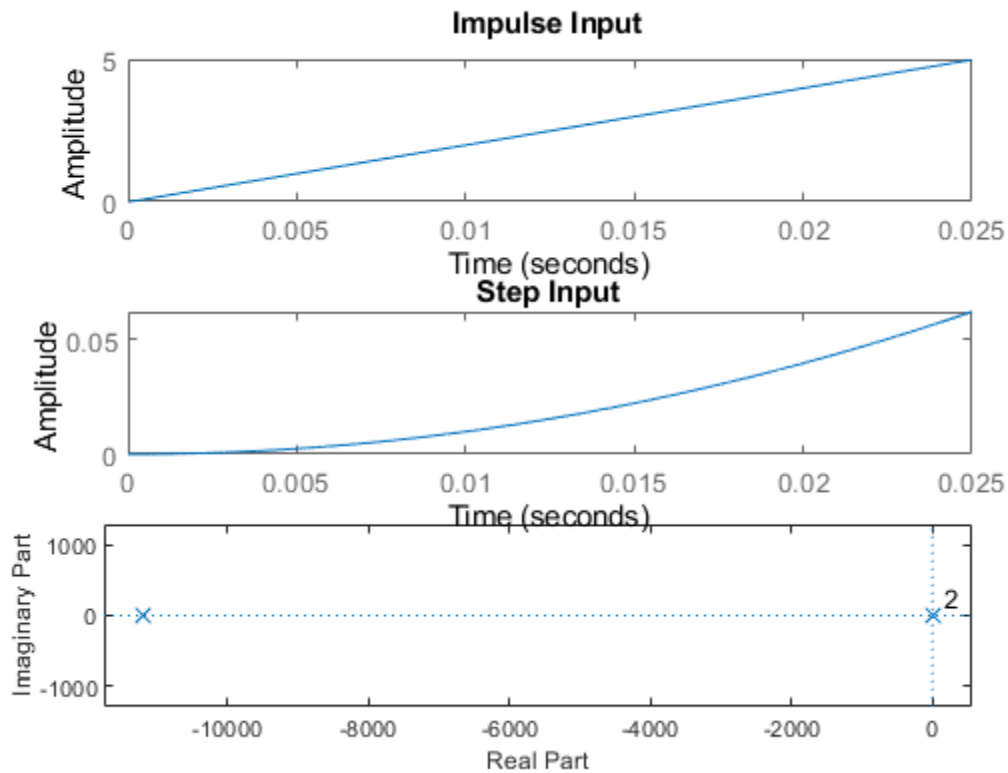
SettlingMax: NaN

Overshoot: NaN

Undershoot: NaN

Peak: Inf

PeakTime: Inf



Closed Loop- Negative feedback with Controller (D)

```
sys = tf([k*A,0],[1,k,(-k)*A])
figure(4);
subplot(3,1,1);
impz(sys);
title('Impulse Input');
subplot(3,1,2);
step(sys);
title('Step Input');
[z,p,k] = tf2zp([k*A,0],[1,k,(-k)*A])
subplot(3,1,3);
zplane(z,p);
s = stepinfo(sys)
```

sys =

$$\frac{4.48e08}{s^2 + 2.24e06 s - 4.48e08}$$

Continuous-time transfer function.

z =

0

p =

1.0e+06 *

-2.2402

0.0002

k =

4.4800e+08

S =

struct with fields:

RiseTime: NaN

SettlingTime: NaN

SettlingMin: NaN

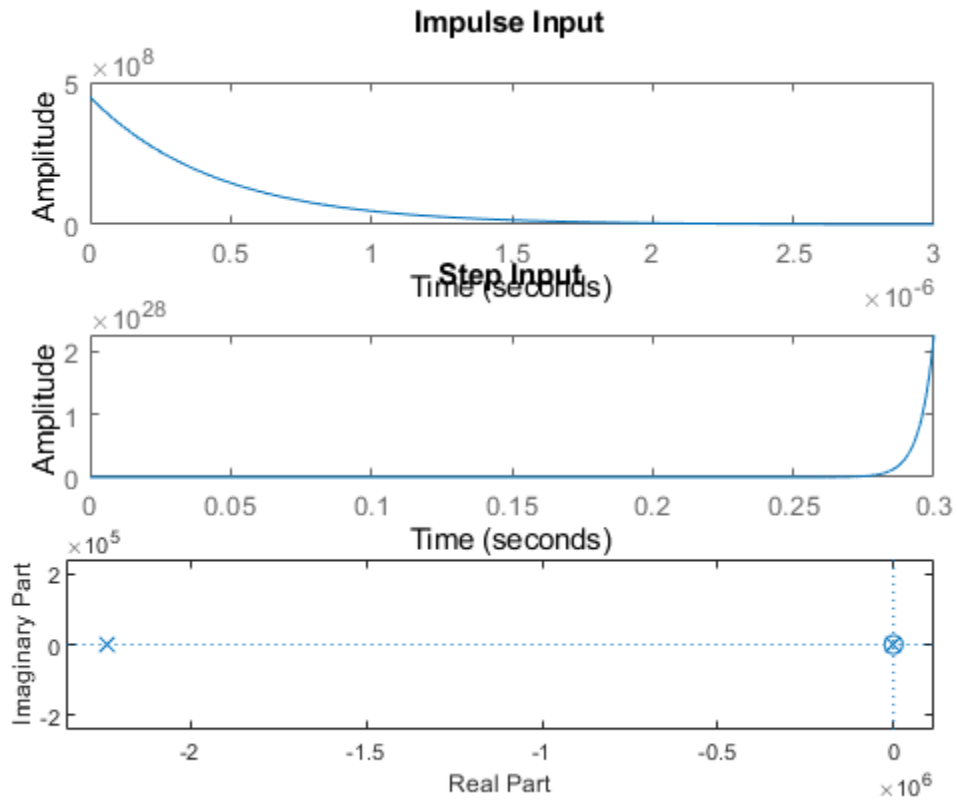
SettlingMax: NaN

Overshoot: NaN

Undershoot: NaN

Peak: Inf

PeakTime: Inf



Closed Loop- Positive feedback with Controller (D)

```
sys = tf([k*A,0],[1,k,k*A])
figure(5);
subplot(3,1,1);
impz(sys);
title('Impulse Input');
subplot(3,1,2);
step(sys);
title('Step Input');
[z,p,k] = tf2zp([k*A,0],[1,k,k*A])
subplot(3,1,3);
zplane(z,p);
S = stepinfo(sys)
```

sys =

$$\frac{8.96 \times 10^{10} \text{ s}}{s^2 + 4.48 \times 10^8 \text{ s} + 8.96 \times 10^{10}}$$

Continuous-time transfer function.

z =

0

p =

1.0e+08 *

-4.4800

-0.0000

k =

8.9600e+10

s =

struct with fields:

RiseTime: 0

SettlingTime: 0.0196

SettlingMin: 0.2598

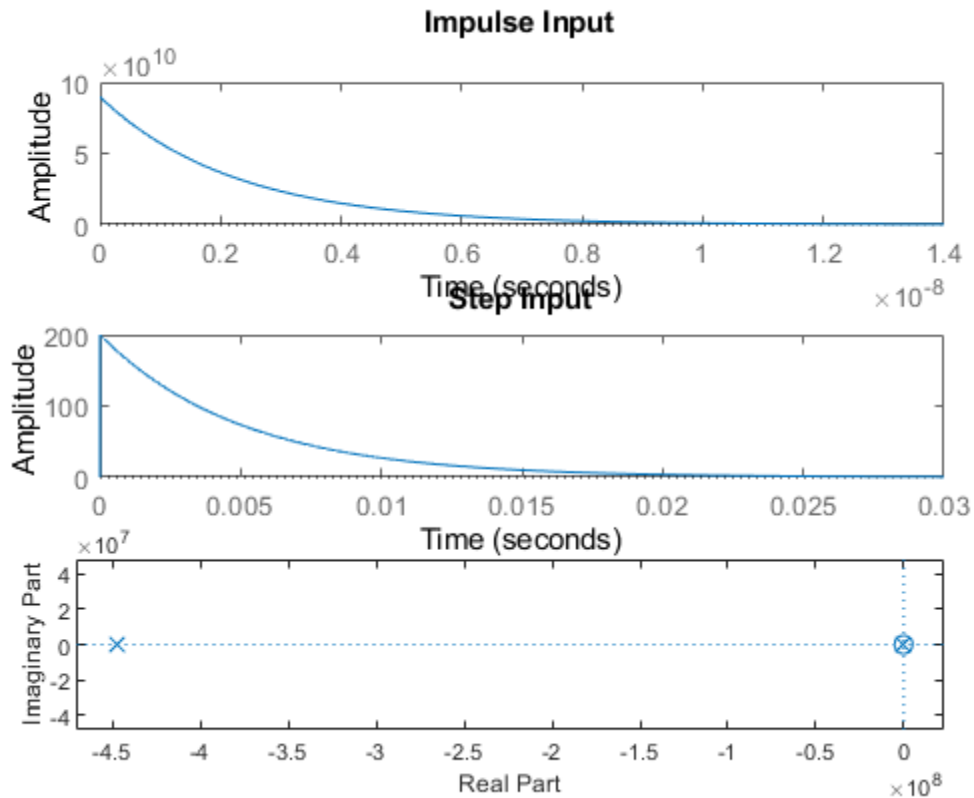
SettlingMax: 199.9633

Overshoot: Inf

Undershoot: 0

Peak: 199.9633

PeakTime: 9.2103e-07



Math Analysis

Independent: Time(t) Dependent: Population(N) Constant: Constant(A)

Comparison Analysis

1) System without controller behaves exactly like an exponential Growth. with the system growing exponentially. 2) On adding a proportionality controller to system, the system becomes unstable. 3) On adding a Integrator controller to system, the response times have decreased hugely, making the system reach stability faster than a P controller. 4) Integrator controller adds a pole to zero also. 5) On addition of a differentiator controller in negative feedback the system becomes unstable. 6) A zero gets added at origin due to the differentiator. 7) On addition of a differentiator controller in positive feedback the system becomes stable.

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