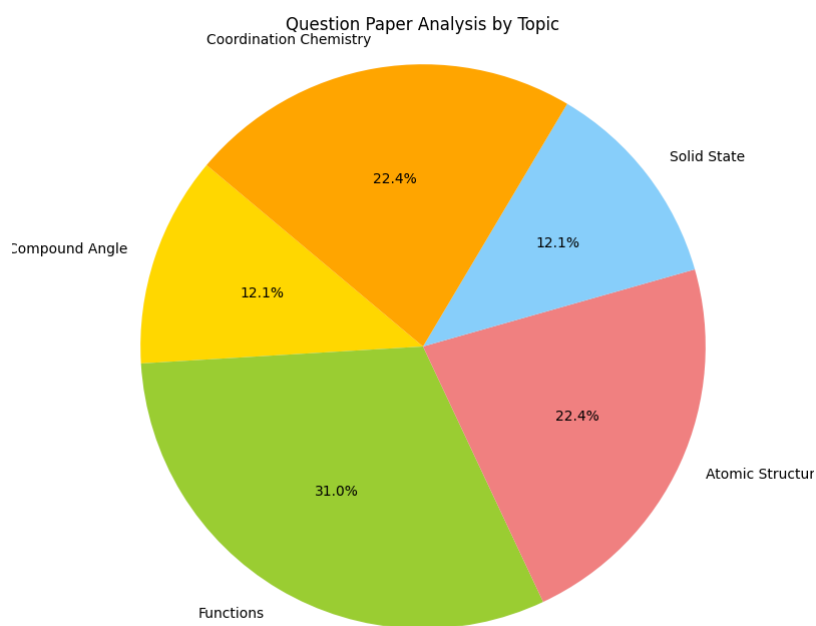
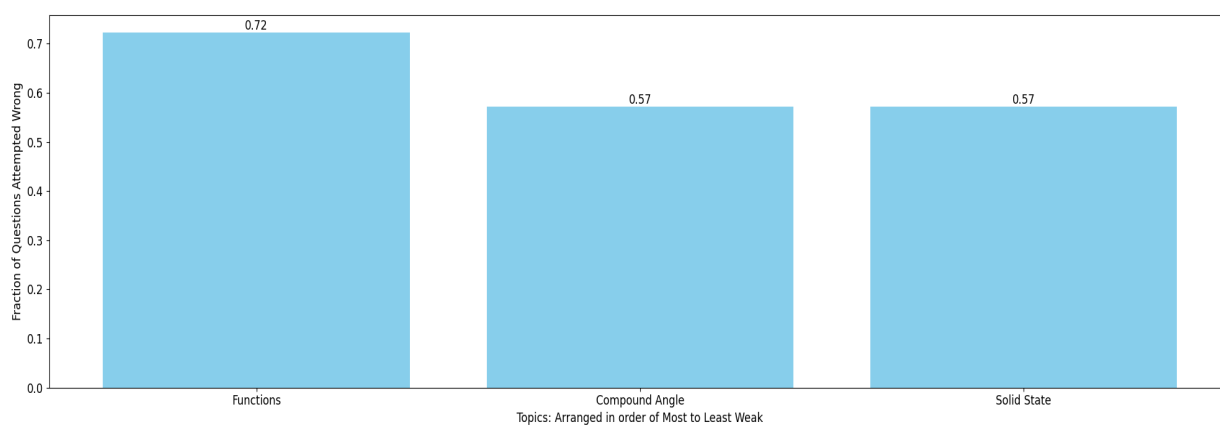


Amrendra Krishna gupta Total MLAssist - Personalised DPP

Question Paper Analysis:



Weak Topic Analysis:



Practice Questions:

Functions:

4. Let $f: \mathbb{R} \rightarrow [1, \infty)$ be defined as

$f(x) = \log_{10} (\sqrt{3x^2 - 4x + k + 1} + 10)$. If $f(x)$ is surjective, then

- (A) $k = \frac{1}{3}$ (B) $k < \frac{1}{3}$ (C) $k > \frac{1}{3}$ (D) $k = 1$

1. Let

$$F(x) = \begin{cases} x|x| & \text{if } x \leq -1 \\ [1+x] + [1-x] & \text{if } -1 < x < 1 \\ -x|x| & \text{if } x \geq 1 \end{cases}$$

where $[x]$ denotes the greatest integer function then $F(x)$ is

- (A) even (B) odd
(C) neither odd nor even (D) even as well as odd

8. Let $f(x) = x^2 + \frac{1}{x^2}$ and $g(x) = x - \frac{1}{x}, x \in \mathbb{R} - \{-1, 0, 1\}$.

If $h(x) = \frac{f(x)}{g(x)}$, then the local minimum value of $h(x)$ is

[JEE - Main 2018]

- (A) -3 (B) $-2\sqrt{2}$ (C) $2\sqrt{2}$ (D) 3

4. Let $f: [0, a] \rightarrow \mathbb{S}$ be a function defined by $f(x) = 3\cos \frac{x}{a}$. If the largest value of a for which $f(x)$ has

38. Let R_1 and R_2 be relations on the set $\{1, 2, \dots, 50\}$ such that

$R_1 = \{(p, p^n) : p \text{ is a prime and } n \geq 0 \text{ is an integer}\}$ and

$R_2 = \{(p, p^n) : p \text{ is a prime and } n = 0 \text{ or } 1\}$.

Then, the number of elements in $R_1 - R_2$ is _____.

[JEE - Main 2022]

Compound Angle:

15. If x and y are real number such that $x^2 + 2xy - y^2 = 6$, find the minimum value of $(x^2 + y^2)^2$.
2. If the expression $\cos^2 \frac{\pi}{11} + \cos^2 \frac{2\pi}{11} + \cos^2 \frac{3\pi}{11} + \cos^2 \frac{4\pi}{11} + \cos^2 \frac{5\pi}{11}$ has the value equal to $\frac{p}{q}$ in its lowest form ; then find $(p + q)$.

$$\sqrt{1 - \sin \theta} \quad [\sec \theta - \tan \theta \quad ; \text{ if } -\frac{\pi}{2} < \theta < \frac{\pi}{2}]$$

5. If $\cos \alpha + \cos \beta + \cos \gamma = 0$;

then prove that $\cos 3\alpha + \cos 3\beta + \cos 3\gamma = 12 \cos \alpha \cos \beta \cos \gamma$

20. (a) If $A + B + C = \pi$; prove that $\tan^2 \frac{A}{2} + \tan^2 \frac{B}{2} + \tan^2 \frac{C}{2} \geq 1$.
 (b) Prove that the triangle ABC is equilateral iff , $\cot A + \cot B + \cot C = \sqrt{3}$.

5. Which of the following relations is (are) possible?

(A) $\sin \theta = \frac{\pi}{2}$ (B) $\tan \theta = 2016$

C) $\cos \theta = \frac{1+t^2}{1-t^2} (t \neq 0, \pm 1)$ (D) $\sec \theta = \frac{3}{4}$

Solid State:

17. The type of unit cell is:
 (A) Simple cubic (B) BCC (C) FCC (D) Edge-centred
2. Calculate the density of diamond from the fact that it has face centered cubic structure with two

19. The edge length of unit cell of a metal having atomic weight 75 g/mol is 5 \AA which crystallizes in cubic lattice. If the density is 2 g/cc then find the radius of metal atom. ($N_A = 6 \times 10^{23}$). Give the answer in pm. **[JEE 2006]**

27. If the length of the body diagonal for CsCl which crystallises into a cubic structure with Cl^- ions at the corners and Cs^+ ions at the centre of the unit cells is 7 \AA and the radius of the Cs^+ ion is

7. A hard substance melts at high temperature and is an insulator in both solid and in molten state.

This solid is most likely to be a / an :

[JEE Main, Mar. 2021]

- | | |
|--------------------|---------------------|
| (A) Ionic solid | (B) Molecular solid |
| (C) Metallic solid | (D) Covalent solid |
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