FuzzyLite v1.5 A Fuzzy Logic Control Library written in C++

by Juan Rada-Vilela

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Chapter 1

Overview

1.1 Introduction

FuzzyLite v1.5 is a multiplatform, free, and open-source Fuzzy Logic Control Library written in C++ and released under the Apache License 2.0, which makes this software freely available for commercial and non-commercial use. The idea behind this library is to have a very simple and light-weight fuzzy controller. Simple as in simple to use, simple to understand, and simple to extend, without sacrificing performance. And light-weighted because it requires no additional libraries other than the Standard Template Library included in the C++ Standard Library. It has an object-oriented approach and a clear separation between the headers and sources, so it is easy to extend. Furthermore, it is GUI-agnostic, meaning that the library does not require a GUI to run, encouraging its use as a library. Nonetheless, a Qt-based GUI is also provided using FuzzyLite v1.5 as an external library.

1.2 Features

- Linguistic terms are continuous and the following ones are available: triangular, trapezoidal, rectangular, shoulder, singleton, custom function, and compound (multiple functions).
- Export any fuzzy system to text using a slightly modified version of the Fuzzy Controller Language (FCL).
- Defuzzification using center of gravity (COG).
- Mamdani rule parsing with grammar checking.
- Takagi Sugeno rules of any order (e.g. $f(x) = (\sin x) / x$, f(x) = 0.5 * input-1).
- Weights for each rule.
- TNorm: minimum, product, bounded difference.
- SNorm: maximum, sum, bounded sum.
- Modulation: clipping, scaling.
- Aggregation: maximum, sum, bounded sum.
- Variable sampling size for membership functions to compute area and centroid.
- Triangulation and Trapezoidal algorithms to compute the area and centroid.

- Hedges: not, somewhat, very, any.
- Very easy to implement and incorporate new linguistic terms, defuzzification methods, fuzzy rules (antecedents and consequents), fuzzy operations (T-Norms, S-Norms, methods for modulation and aggregation), algorithms for computing the area and centroid of linguistic terms, hedges, among other things.

1.3 What's new?

1.3.1 FuzzyLite v1.5

- Fixed the Trapezoidal Algorithm.
- Changed most of the #includes for forward declarations.
- Moved repository to http://code.google.com/p/fuzzylite/.
- Updated the building scripts for Unix systems.
- Removed building scripts for Mac OS X due to the lack of access to such OS.

1.3.2 FuzzyLite v.1.03

- Fixed the Triangulation Algorithm to include the first and last triangle (improved accuracy). Courtesy of rctaylor.
- Implemented the Trapezoidal Algorithm suggested by William Roeder, although its accuracy is not as good as the Triangulation algorithm.
- Created the scripts for building fuzzylite as static and dynamic library, as well as building a demo version of it. Tested on Linux Ubuntu and Mac OS X 10.5. Although the Unix version should work under Windows as well using G++.
- Added LeftShoulderTerm and RightShoulderTerm, just to provide a better understanding when configuring the FuzzyEngine.
- Changed all the #include <fuzzylite/?.h> for `` fuzzylite/?.h''.
- Included the Trapezoidal Algorithm into the GUI.

1.3.3 FuzzyLite v.1.01

- The source can be built on Linux with no need to add several includes to some files. (I work on MacOSX and I did not build fuzzylite on Linux, I just assumed it would build just fine, but some includes were missing in some files. This was FIXED).
- Several scripts for building fuzzylite using a simple make. These scripts are created automatically by NetBeans, however, you do not need NetBeans to build fuzzylite nor the gui. The scripts are available for Linux and Mac OS X.

1.3.4 FuzzyLite v1.0

- The GUI is working again.
- A class diagram of FuzzyLite v1.5.
- A detailed explanation of FuzzyLite v1.5.
- Minor changes.

1.4 What's next?

- Figure out why the accuracy of the Trapezoidal Algorithm is not as good as the Triangulation algorithm.
- Fix the GUI so Takagi Sugeno rules can be tested with their respective graph.
- Improve the InfixToPostfix class so infix functions are parsed as one would normally expect.
- Load the fuzzy engine from text using the Fuzzy Controller Language (FCL).
- Include more linguistic terms (e.g. sigmoidal, gaussian, sine, cosine).
- Include more defuzzifiers (e.g. Right Most Maximum, Left Most Maximum, Mean Maximum).
- Make some functions inline to increase performance and check those that are already inline to ensure they do increase performance.

1.5 Known bugs

- The Trapezoidal Algorithm had a bug in version 1.03. This bug has been fixed from version 1.5.
- InfixToPostfix conversion might not parse functions as one would normally expect. For example, $\sin(x)/x$ is *not* equivalent to $(\sin x)/x$, the latter yields the result one might expect. Make sure by validating the postfix expression, or by evaluating its results.
- In the GUI, when using a Takagi Sugeno system, the output graphs do not work.

1.6 Building as a project

The sources can be built by creating a project on your favorite C++ IDE. All you need to remember is to add './' to the INCLUDE_PATH since all the #includes from the library are in the form #include 'fuzzylite/...'. You will also need to specify whether is an application you are building from fuzzylite or a library (either static or dynamic). Additional settings involve activating the preprocessor directive 'FL_USE_LOG' so you can output messages to the console (useful for the demo).

1.7 Building from source

Alternatively, you can build the library using the scripts provided which were created automatically from the Eclipse IDE once the previous parameters were set. Building from the scripts is shown below.

1.7.1 FuzzyLite v1.5

Inside ./fuzzylite there are now 3 folders, on each there is a makefile. So all you have to do is execute from the folder the command make. The folders are described below.

- unix-demo: Builds a demo version of fuzzylite which can be executed later as ./fuzzylite. It shows the results for four examples of Fuzzy Engines.
- unix-static: Builds the library as a static library (fuzzylite.a).
- unix-dynamic: Builds the library as a dynamic library (fuzzylite.so.

1.7.2 FuzzyLite v.1.03

Inside ./fuzzylite there are 6 folders, on each there is a makefile. So all you have to do is execute from the folder the command make. The folders are described below (notice that <code>[OS]</code> stands for the operating system).

- [OS] -demo: Builds a demo version of fuzzylite which can be executed later as ./fuzzylite. It shows the results for four examples of Fuzzy Engines.
- [OS] -static: Builds the library as a static library (fuzzylite.a).
- [OS]-shared: Builds the library as a dynamic library (fuzzylite.so (unix) or fuzzylite.dylib (mac)).

This is a huge improvement from those really nasty NetBeans scripts. These scripts were automatically created by Eclipse.

1.7.3 FuzzyLite v.1.01

Version 1.01 contains the following files linux-Makefile and macosx-Makefile, and the following folders linux-nbproject and macosx-nbproject. Depending on your platform, you must rename them by removing the name of the platform, so the new names are Makefile and nbproject respectively. This should work, otherwise, follow the steps below.

- 1. Create a C++ Project either in Eclipse IDE or Netbeans IDE.
- 2. Add all the source files and include files to the project.
- 3. Add . to the includes path in the project properties.
- 4. Add the directive <code>-DFL_USE_LOG</code> to enable the use of logging via <code>FL_LOG</code> (message). In <code>./include/defs.h</code> there are more symbols that can be defined via <code>-D</code> for further customization.
- 5. Decide whether to build a library or an executable (in project properties).
- 6. Use the IDE's normal build.

1.7.4 Graphic User Interface

1.7.5 Requirements

• Qt which can be freely downloaded from http://qt.nokia.com/.

1.7.6 FuzzyLite v1.5

Building from source is the same as previous version.

1.7.7 FuzzyLite v.1.03

In order to build this version, all you need to do (aside from having installed Qt which can be freely downloaded from http://qt.nokia.com/.) is execute from ./fuzzylite/ the command qmake. This will create a Makefile. Then, run make and it should start building the GUI. Notice that in qui.pro it links to the unix version of fuzzylite static library using relative path, so be sure to build such library first. If it is not unix version of puzzylite static library using relative path, so be sure to build such library first. If it is not unix version of puzzylite static library using relative path, so be sure to build such library first. If it is not unix version of puzzylite static library using relative path, so be sure to build such library first. If it is not unix version of unix version of <a

1.7.8 FuzzyLite v.1.01

In order to build the graphical user interface of FuzzyLite v1.5, it is necessary to first install Qt which can be freely downloaded from http://qt.nokia.com/.

The Makefile included within the ./gui is quite easy to read. Basically, the most important thing here is to copy the libfuzzylite.dylib (or whatever the extension be according to your platform) into the folder ./gui/dist which is where the executable will be put. An alternative is to copy the library into /usr/local/lib and comment those lines in the Makefile that build and copy the library into the ./gui/dist directory.

After configuring the Makefile to fit your system, a make all from ./gui would build the graphical user interface of FuzzyLite v1.5. To run, it suffices to execute ./gui from ./gui/dist.

1.8 Acknowledgements

This work was possible thanks to the Foundation for the Advancement of Soft Computing, to the Master of Soft Computing and Intelligent Data Analysis, and especially to Sergio Guadarrama and Luis Magdalena.

Chapter 2

The Model

This chapter is devoted to explain FuzzyLite v1.5 by means of a class diagram based on UML. For a better comprehension, it is divided in five groups: Fuzzy operations, Linguistic variables and terms, Linguistic terms, Fuzzy rules, Fuzzy engine, and Fuzzy exceptions. It is important to mention that all classes related to FuzzyLite v1.5 are inside the namespace f1.

2.1 Fuzzy operations

Figure 2.1 shows the class diagram for this group. The classes that can be seen in it are briefly explained in the following sections.

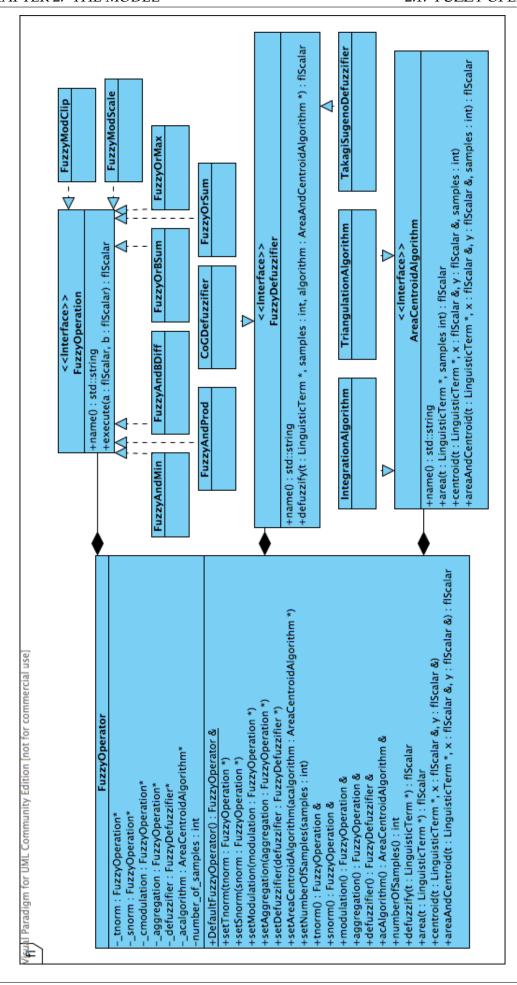


Figure 2.1: Class diagram: Fuzzy operations

2.1.1 FuzzyOperator

FuzzyOperator centralizes all the operations that can be performed in the fuzzy system. It contains the type of T-Norms, S-Norms, modulation, aggregation, defuzzification methods, algorithms for computing the area and centroid of any linguistic term, and the number of samples that are drawn from any linguistic term to be used by the algorithm.

This class has an static default FuzzyOperator instance that can be obtained using the method fl::FuzzyOperator::DefaultFuzzyOperator() anywhere and anytime. The defaults for this operator are the following

• **T-Norm:** FuzzyAndMin.

• **S-Norm:** FuzzyOrMax.

• **Modulation:** FuzzyModClip.

• **Aggregation:** FuzzyOrMax.

• **Defuzzifier:** CoGDefuzzifier.

• Algorithm: TriangulationAlgorithm.

• Number of samples: 100.

These defaults may be changed at any moment from anywhere, but consider that this is an instance that is shared among all instances from many classes, so be careful about changing these values. Nevertheless, if you need to, you may use different instances among all those classes composed by FuzzyOperator.

2.1.2 FuzzyOperation

This is the interface shared by all T-Norms, S-Norms, and methods for modulation and aggregation. If you want to implement your own operations, you may do so by implementing this interface. The operations included in FuzzyLite v1.5 are:

- T-Norm: minimum (FuzzyAndMin), product (FuzzyAndProd), and bounded difference (FuzzyAndBDiff).
- S-Norm: maximum (FuzzyOrMax), sum (FuzzyOrSum), bounded sum (FuzzyOrBSum).
- Modulation: clipping (FuzzyModClip), scaling (FuzzyModScale).
- Aggregation: maximum (FuzzyOrMax), sum (FuzzyOrSum), bounded sum (FuzzyOrBSum).

2.1.3 FuzzyDefuzzifier

This is the interface shared by all defuzzifiers. If you want to implement a different defuzzifier, you may do so by implementing this interface. The defuzzifiers included in FuzzyLite v1.5 are: Centre of Gravity (CoGDefuzzifier) for Mamdani rules, and TakagiSugenoDefuzzifier for Takagi-Sugeno rules.

2.1.4 AreaAndCentroidAlgorithm

This is an interface used for computing the area and centroid of linguistic terms. The algorithms included in FuzzyLite v1.5 are: TriangulationAlgorithm which is a triangulation algorithm appropriate for terms that can be easily triangulated, and IntegrationAlgorithm which is a regular integration algorithm. The algorithm should be chosen according to the shape of the fuzzy partitions. You may also create your own algorithm by implementing this interface.

2.2 Linguistic variables and terms

Figure 2.2 shows the class diagram for the linguistic variables and terms included in FuzzyLite v1.5.

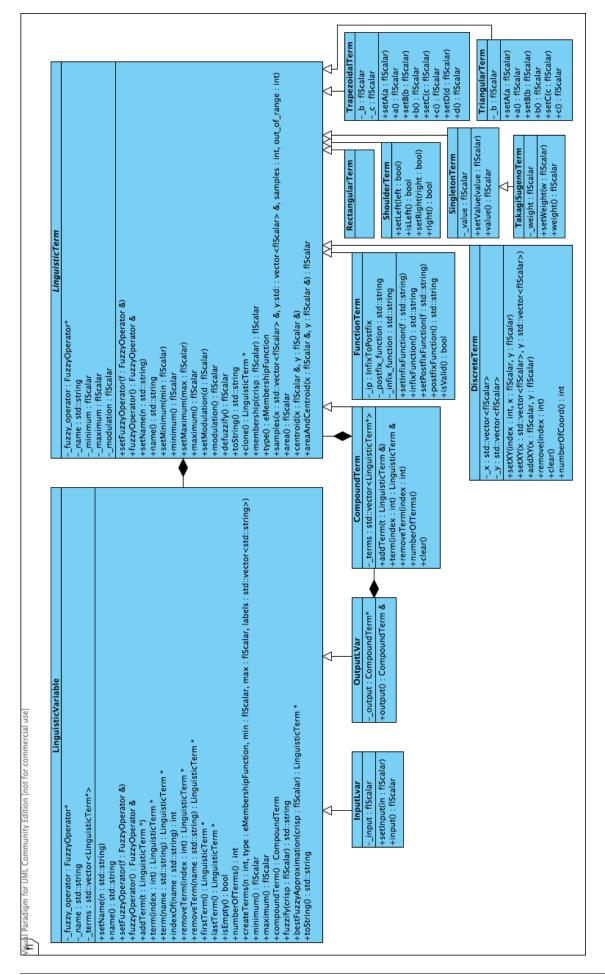


Figure 2.2: Class diagram: Linguistic variables and terms

2.2.1 LinguisticVariable

Linguistic variables are composed of a vector of LinguisticTerms. This is an abstract class that is used as base for input variables (InputLVar) and output variables (OutputLVar). Each input variable has an input value that should be the input received by the system, and each output variable has a compound linguistic term composed by all the linguistic terms added by the activation of the different rules given the input values of the input variables and their respective processing.

2.2.2 LinguisticTerm

Linguistic terms, also known as fuzzy partitions, define the shape of each label. Each linguistic term has a minimum and maximum that are used to define the limits of the area it covers. Several linguistic terms are included in FuzzyLite v1.5:

- TriangularTerm: is the well known triangular term, it is defined by its three vertices a, b, and c, where a and c are wrappers of minimum() and maximum(), respectively.
- RectangularTerm: is a simple rectangular term delimited by the minimum and maximum of its parent class LinguisticTerm.
- TrapezoidalTerm: defines a trapezoid by its four vertices a, b, c, and d, where a and d are wrappers of minimum() and maximum(), respectively.
- SingletonTerm: defines a singleton for the value v delimited by $v \delta_{low}$ and $v + \delta_{hi}$ where δ_{low} and δ_{hi} are very small values in order to be able to create samples of this term.
- ShoulderTerm: defines a trapezoid that extends to $\pm \infty$ depending on whether it is left $(-\infty)$ or right $(+\infty)$.
- DiscreteTerm: is a term composed of a vector of (x, y) coordinates. It is important to note that when sampling this type of term, the result of membership (flScalar crisp) is the value of y for the closest x given the value of crisp.
- FunctionTerm: is a term that is defined as a function f(x) which accepts several mathematical and trigonometrical operations over a given function, for example: $\operatorname{setInfixFunction}($ " ($\operatorname{sin} \times$) / \times "). It is very important to remark that the parser used to parse infix functions may not function as expected (e.g. $\sin(x)/x$ is different of $(\sin x)/x$, the latter one gives the result one expects). When in doubt, test your expression by converting it to postfix.
- CompoundTerm: is a term composed of a list of LinguisticTerms. This is used in OutputLVar in order to aggregate all the linguistic terms that were added by the activation of rules, but it may be used as well to create more complex partitions.
- TakagiSugenoTerm: is a term used when dealing with TakagiSugenoRules, it extends from SingletonTerm so it has a value, and it includes a weight as well, both necessary for this kind of system.

Finally, figure 2.3 shows examples of the linguistic terms, obtained by printing the window from the GUI developed for FuzzyLite v1.5.

2.3 Fuzzy rules

Figure 2.4 shows the class diagram for fuzzy rules and all its related classes included in FuzzyLite v1.5.

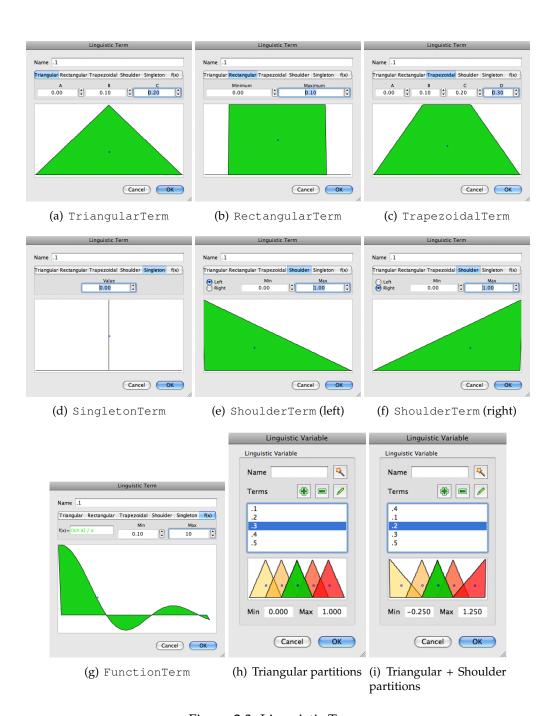


Figure 2.3: Linguistic Terms

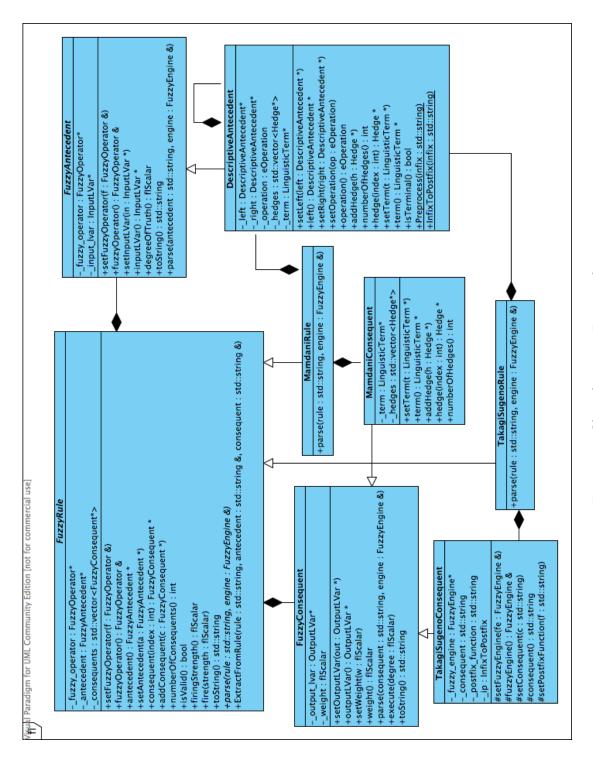


Figure 2.4: Class diagram: Fuzzy rules

2.3.1 FuzzyRule

This abstract class is the base for MamdaniRules and TakagiSugenoRules. It is composed by an antecedent (FuzzyAntecedent) and a list of consequents (FuzzyConsequents). There are two methods that are worth mentioning here: firingStrength() which determines the activation degree of the rule given the inputs in the InputLVars, and fire(flScalar d) which fires the rule with a degree d. When firing the rule, the consequents are modulated according to d and then added to the OutputLVars with the respective weight of the rule. It is also important to remark that parsing the rules is case-sensitive.

FuzzyAntecedent and FuzzyConsequent

These abstract classes represent the antecedent and consequent of a rule, respectively. FuzzyAntecedent has a pointer to the input variable to which it is related in order to access the value of the respective InputLVar, similarly, FuzzyConsequent has a pointer to the output variable to which it is related in order to aggregate the respective modulated linguistic term to the output.

DescriptiveAntecedent

This class is based on FuzzyAntecedent and it is a red-black tree that relates two propositions with an operator, for example, input-1 is LOW and input-2 is GOOD is separated into a left antecedent (input-1 is LOW), an operator (and), and a right antecedent (input-2 is GOOD). Given the recursion of this model, it is possible to create rules of any depth, as it is evaluated bottom-up. This is the class used by MamdaniRule and TakagiSugenoRule.

Hedge

Hedges are modifiers of the propositions (antecedent) and actions (consequent). All hedges must implement the interface <code>Hedge</code>, and must be included when configuring the <code>FuzzyEngine</code>. <code>FuzzyLite v1.5</code> includes four hedges: not (<code>HedgeNot</code>), somewhat (<code>HedgeSomewhat</code>), very (<code>HedgeVery</code>), any (<code>HedgeAny</code>). In order to use <code>HedgeAny</code>, it is necessary to include a <code>dummy</code> linguistic term to comply with the general form of the rules (i.e. <code>input-1</code> is any <code>LOW</code>); this hedge will always return 1.0, so it does not matter the linguistic term as long as it is within the linguistic variable used. Figure 2.5 shows the class diagram regarding hedges.

MamdaniRule and TakagiSugenoRule

These classes represents the type of rules of a system based on Mamdani's rules, and the one based on Takagi-Sugeno rules, respectively. They extend the abstract class FuzzyRule by implementing the parse () method accordingly. Both classes use DescriptiveAntecedent as the antecedent of the rule, but differ in the consequent: MamdaniRule uses MamdaniConsequent, and TakagiSugenoRule uses TakagiSugenoConsequent.

MamdaniConsequent and TakagiSugenoConsequent

The consequent of a Mamdani rule is of the form: OutputLVar is [Hedge*] LinguisticTerm, where [Hedge*] means that none or many hedges may be included.

Conversely, the consequent of a Takagi-Sugeno rule is of the form $\texttt{OutputLVar} = \{expression\}$, where *expression* is a mathematical expression that may include references to the values of the InputLVars, in which case the name of the input variable is used (e.g. "... $\texttt{f_x} = 0.5 * input-1 + (sin input-2)$ "). This implementation also allows to include previously computed outputs, in which case the name of the output should be used instead.

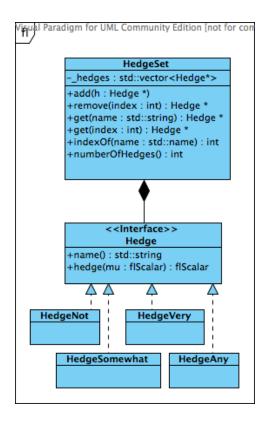


Figure 2.5: Class diagram: Hedges

2.4 Fuzzy engine

The class diagram for this group can be seen in figure 2.6. It contains the class FuzzyEngine which is composed by a FuzzyOperator, a vector of RuleBlocks which contain the FuzzyRules, a HedgeSet that contains the hedges registered in the engine, and a vector of InputLVars and OutputLVars for input and output variables (respectively).

The FuzzyEngine class contains the whole fuzzy control system. The only methods which might require a bit of explanation are process (bool), and process (int, bool). The former receives a boolean parameter that defaults to true and (if true) clears the output of all the output variables. The latter receives an int parameter that determines the index of the RuleBlock to be fired, and a bool that defaults to true which defines whether to clear the output of the output variables.

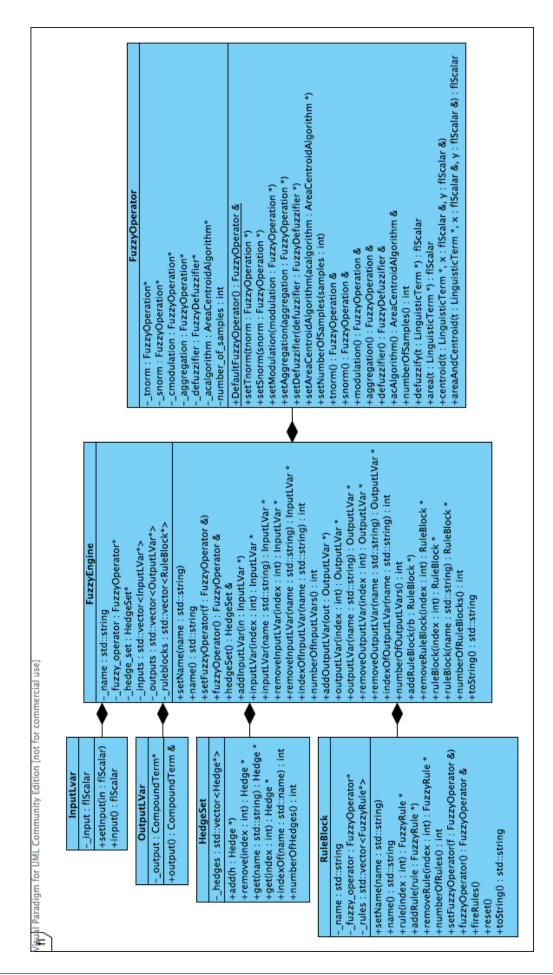


Figure 2.6: Class diagram: Fuzzy engine

2.5 Fuzzy exceptions

This group contains some exceptions that are used within several classes of FuzzyLite v1.5. The class FuzzyException extends the std::exception of the Standard Template Library (STL), and adds additional methods. The other classes derived from FuzzyException also contain some static methods to help a bit with the programming. There is not much to say about these exceptions, except to take a look at the code when using them to become familiar. Figure 2.7 shows the class diagram for this group.

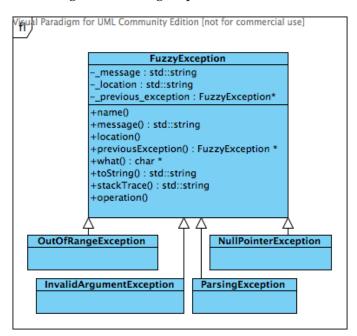


Figure 2.7: Class diagram: Fuzzy exceptions

Chapter 3

Examples

3.1 Example #1: Basic FIS

This is a basic FIS composed of one input variable and one output variable.

```
fl::FuzzyEngine engine;
   engine.hedgeSet().add(new fl::HedgeNot);
   engine.hedgeSet().add(new fl::HedgeSomewhat);
   engine.hedgeSet().add(new fl::HedgeVery);
   fl::InputLVar* energy = new fl::InputLVar("Energy");
   energy->addTerm(new fl::ShoulderTerm("LOW", 0.25, 0.5, true));
   energy->addTerm(new fl::TriangularTerm("MEDIUM", 0.25, 0.75));
   energy->addTerm(new fl::ShoulderTerm("HIGH", 0.50, 0.75, false));
   engine.addInputLVar(energy);
10
   fl::OutputLVar* health = new fl::OutputLVar("Health");
11
   health->addTerm(new fl::TriangularTerm("BAD", 0.0, 0.50));
12
   health->addTerm(new fl::TriangularTerm("REGULAR", 0.25, 0.75));
13
   health->addTerm(new fl::TriangularTerm("GOOD", 0.50, 1.00));
   engine.addOutputLVar(health);
   fl::RuleBlock* block = new fl::RuleBlock();
   block->addRule(new fl::MamdaniRule("if Energy is LOW then Health is BAD", engine));
   block->addRule(new fl::MamdaniRule("if Energy is MEDIUM then Health is REGULAR", engine));
   block->addRule(new fl::MamdaniRule("if Energy is HIGH then Health is GOOD", engine));
   engine.addRuleBlock(block);
```

Once the FIS is configured, the control process may begin anytime by setting the input value to the input variables and processing. For example,

```
for (fl::flScalar in = 0.0; in < 1.1; in += 0.1) {</pre>
22
23
        energy->setInput(in);
24
        engine.process();
        fl::flScalar out = health->output().defuzzify();
25
        FL_LOG("Energy=" << in);</pre>
26
        FL_LOG("Energy is " << energy->fuzzify(in));
        FL_LOG("Health=" << out);</pre>
        FL_LOG("Health is " << health->fuzzify(out));
29
        FL_LOG("--");
30
```

The previous code would yield the following results in console (assuming that FL_USE_LOG was defined):

```
1 Energy=0
2 Energy is 1.000/LOW + 0.000/MEDIUM + 0.000/HIGH
3 Health=0.249902
4 Health is 1.000/BAD + 0.000/REGULAR + 0.000/GOOD
5 --
6 Energy=0.1
```

```
7 Energy is 1.000/LOW + 0.000/MEDIUM + 0.000/HIGH
8 Health=0.249902
9 Health is 1.000/BAD + 0.000/REGULAR + 0.000/GOOD
11 Energy=0.2
12 Energy is 1.000/LOW + 0.000/MEDIUM + 0.000/HIGH
13 Health=0.249902
14 Health is 1.000/BAD + 0.000/REGULAR + 0.000/GOOD
16 Energy=0.3
17 Energy is 0.800/LOW + 0.200/MEDIUM + 0.000/HIGH
18 Health=0.309985
19 Health is 0.760/BAD + 0.240/REGULAR + 0.000/GOOD
20 -
21 Energy=0.4
22 Energy is 0.400/LOW + 0.600/MEDIUM + 0.000/HIGH
23 Health=0.394929
24 Health is 0.420/BAD + 0.580/REGULAR + 0.000/GOOD
25 --
26 Energy=0.5
27 Energy is 0.000/LOW + 1.000/MEDIUM + 0.000/HIGH
28 Health=0.499902
29 Health is 0.000/BAD + 1.000/REGULAR + 0.000/GOOD
31 Energy=0.6
32 Energy is 0.000/LOW + 0.600/MEDIUM + 0.400/HIGH
33 Health=0.604537
34 Health is 0.000/BAD + 0.582/REGULAR + 0.418/GOOD
35 --
36 Energy=0.7
37 Energy is 0.000/LOW + 0.200/MEDIUM + 0.800/HIGH
38 Health=0.689444
39 Health is 0.000/BAD + 0.242/REGULAR + 0.758/GOOD
41 Energy=0.8
42 Energy is 0.000/LOW + 0.000/MEDIUM + 1.000/HIGH
43 Health=0.749902
44 Health is 0.000/BAD + 0.000/REGULAR + 1.000/GOOD
45 --
46 Energy=0.9
47 Energy is 0.000/LOW + 0.000/MEDIUM + 1.000/HIGH
48 Health=0.749902
49 Health is 0.000/BAD + 0.000/REGULAR + 1.000/GOOD
50 --
51 Energy=1
52 Energy is 0.000/LOW + 0.000/MEDIUM + 1.000/HIGH
53 Health=0.749902
54 Health is 0.000/BAD + 0.000/REGULAR + 1.000/GOOD
55 --
```

3.2 Example #2: 3D Pole Balancing

A simulation video of this fuzzy system implemented with FuzzyLite v1.5 as shown below is available at http://www.youtube.com/watch?v=YOKk8G_5aRA.

```
1 FuzzyEngine engine("pole-balancing-3d");
2
3 InputLVar* anglex = new InputLVar("AngleX");
4 std::vector<std::string> labels;
5 labels.push_back("NEAR_0");
6 labels.push_back("NEAR_45");
7 labels.push_back("NEAR_90");
```

```
8 labels.push_back("NEAR_135");
9 labels.push_back("NEAR_180");
10 anglex->createTerms(5, LinguisticTerm::MF_SHOULDER, 0, 180, labels);
11 engine.addInputLVar(anglex);
13 InputLVar* anglez = new InputLVar("AngleZ");
14 labels.clear();
15 labels.push_back("NEAR_0");
16 labels.push_back("NEAR_45");
17 labels.push_back("NEAR_90");
18 labels.push_back("NEAR_135");
19 labels.push_back("NEAR_180");
20 anglez->createTerms(5, LinguisticTerm::MF_SHOULDER, 0, 180, labels);
21 engine.addInputLVar(anglez);
23 OutputLVar* forcex = new OutputLVar("ForceX");
24 labels.clear();
25 labels.push_back("NL");
26 labels.push_back("NS");
27 labels.push_back("ZR");
28 labels.push_back("PS");
29 labels.push_back("PL");
30 forcex->createTerms(5, LinguisticTerm::MF_TRIANGULAR, -1, 1, labels);
31 engine.addOutputLVar(forcex);
33 OutputLVar* forcez = new OutputLVar("ForceZ");
34 labels.clear();
35 labels.push_back("NL");
36 labels.push_back("NS");
37 labels.push_back("ZR");
38 labels.push_back("PS");
39 labels.push_back("PL");
40 forcez->createTerms(5, LinguisticTerm::MF_TRIANGULAR, -1, 1, labels);
41 engine.addOutputLVar(forcez);
43 RuleBlock* ruleblock = new RuleBlock("Rules");
44 ruleblock->addRule(new MamdaniRule("if AngleX is NEAR_180 then ForceX is NL", engine));
45 ruleblock->addRule(new MamdaniRule("if AngleX is NEAR_135 then ForceX is NS", engine));
46 ruleblock->addRule(new MamdaniRule("if AngleX is NEAR_90 then ForceX is ZR", engine));
47 ruleblock->addRule(new MamdaniRule("if AngleX is NEAR_45 then ForceX is PS", engine));
48 ruleblock->addRule(new MamdaniRule("if AngleX is NEAR_0 then ForceX is PL", engine));
50 ruleblock->addRule(new MamdaniRule("if AngleZ is NEAR_180 then ForceZ is NL", engine));
51 ruleblock->addRule(new MamdaniRule("if AngleZ is NEAR_135 then ForceZ is NS", engine));
52 ruleblock->addRule(new MamdaniRule("if AngleZ is NEAR_90 then ForceZ is ZR", engine));
53 ruleblock->addRule(new MamdaniRule("if AngleZ is NEAR_45 then ForceZ is PS", engine));
54 ruleblock->addRule(new MamdaniRule("if AngleZ is NEAR_0 then ForceZ is PL", engine));
55 engine.addRuleBlock(ruleblock);
57 FL_LOG(engine.toString());
```

The output from the previous block of code exports the fuzzy system to text using the Fuzzy Controller Language (FCL) as shown below.

```
1 FUNCTION_BLOCK pole-balancing-3d
2
3 VAR_INPUT
4 AngleX: REAL;
5 AngleZ: REAL;
6 END_VAR
7
8 FUZZIFY AngleX
9 TERM NEAR_0 := Shoulder left(0 60);
10 TERM NEAR_45 := Triangular (30 60 90);
```

3.2. EXAMPLE #2: 3D POLE BALANCING

```
11 TERM NEAR_90 := Triangular (60 90 120);
12 TERM NEAR_135 := Triangular (90 120 150);
13 TERM NEAR_180 := Shoulder right (120 180);
14 END FUZZIFY
16 FUZZIFY AngleZ
17 TERM NEAR_0 := Shoulder left(0 60);
18 TERM NEAR_45 := Triangular (30 60 90);
19 TERM NEAR_90 := Triangular (60 90 120);
20 TERM NEAR_135 := Triangular (90 120 150);
21 TERM NEAR_180 := Shoulder right (120 180);
22 END_FUZZIFY
24 VAR_OUTPUT
25 ForceX: REAL
26 ForceZ: REAL
27 END_VAR
29 DEFUZZIFY ForceX
30 TERM NL := Triangular (-1 -0.666667 -0.333333);
31 TERM NS := Triangular (-0.666667 -0.333333 5.96046e-08);
32 TERM ZR := Triangular (-0.333333 5.96046e-08 0.333333);
33 TERM PS := Triangular (5.96046e-08 0.333333 0.666667);
34 TERM PL := Triangular (0.333333 0.666667 1);
35 END_DEFUZZIFY
37 DEFUZZIFY ForceZ
38 TERM NL := Triangular (-1 - 0.666667 - 0.3333333);
39 TERM NS := Triangular (-0.666667 -0.333333 5.96046e-08);
40 TERM ZR := Triangular (-0.333333 5.96046e-08 0.333333);
41 TERM PS := Triangular (5.96046e-08 0.333333 0.666667);
42 TERM PL := Triangular (0.333333 0.666667 1);
43 END_DEFUZZIFY
45 RULEBLOCK Rules
46 RULE 1: if AngleX is NEAR_180 then ForceX is NL;
47 RULE 2: if AngleX is NEAR_135 then ForceX is NS;
48 RULE 3: if AngleX is NEAR_90 then ForceX is ZR;
49 RULE 4: if AngleX is NEAR_45 then ForceX is PS;
50 RULE 5: if AngleX is NEAR_0 then ForceX is PL;
51 RULE 6: if AngleZ is NEAR_180 then ForceZ is NL;
52 RULE 7: if AngleZ is NEAR_135 then ForceZ is NS;
53 RULE 8: if AngleZ is NEAR_90 then ForceZ is ZR;
54 RULE 9: if AngleZ is NEAR_45 then ForceZ is PS;
55 RULE 10: if AngleZ is NEAR_O then ForceZ is PL;
56 END_RULEBLOCK
58 END_FUNCTION_BLOCK
```

3.3 Example 3: Approximating a function

It is also possible to create a fuzzy system to approximate a function. For example, if we were to approximate the function sin(x)/x, we could do so by using the with the following code.

```
1 FuzzyOperator& op = FuzzyOperator::DefaultFuzzyOperator();
2 op.setDefuzzifier(new TakagiSugenoDefuzzifier);
3 FuzzyEngine engine("approximation", op);
4
5 fl::InputLVar* x = new fl::InputLVar("x");
6 x->addTerm(new fl::TriangularTerm("NEAR_1", 0, 2));
7 x->addTerm(new fl::TriangularTerm("NEAR_2", 1, 3));
8 x->addTerm(new fl::TriangularTerm("NEAR_3", 2, 4));
```

```
9 x->addTerm(new fl::TriangularTerm("NEAR_4", 3, 5));
10 x->addTerm(new fl::TriangularTerm("NEAR_5", 4, 6));
11 x->addTerm(new fl::TriangularTerm("NEAR_6", 5, 7));
12 x->addTerm(new fl::TriangularTerm("NEAR_7", 6, 8));
13 x->addTerm(new fl::TriangularTerm("NEAR_8", 7, 9));
14 x->addTerm(new fl::TriangularTerm("NEAR_9", 8, 10));
15 engine.addInputLVar(x);
17 fl::OutputLVar* f_x = new fl::OutputLVar("f_x");
18 f_x->addTerm(new fl::FunctionTerm("function", "(sin x) / x", 0, 10));
19 engine.addOutputLVar(f_x);
21 fl::RuleBlock* block = new fl::RuleBlock();
22 block->addRule(new fl::TakagiSugenoRule("if x is NEAR_1 then f_x=0.84", engine));
23 block->addRule(new fl::TakagiSugenoRule("if x is NEAR_2 then f_x=0.45", engine));
24 block->addRule(new fl::TakagiSugenoRule("if x is NEAR_3 then f_x=0.04", engine));
25 block->addRule(new fl::TakagiSugenoRule("if x is NEAR_4 then f_x=-0.18", engine));
26 block->addRule(new fl::TakagiSugenoRule("if x is NEAR_5 then f_x=-0.19", engine));
27 block->addRule(new fl::TakagiSugenoRule("if x is NEAR_6 then f_x=-0.04", engine));
28 block->addRule(new fl::TakagiSugenoRule("if x is NEAR_7 then f_x=0.09", engine));
29 block->addRule(new fl::TakagiSugenoRule("if x is NEAR_8 then f_x=0.12", engine));
30 block->addRule(new fl::TakagiSugenoRule("if x is NEAR_9 then f_x=0.04", engine));
32 engine.addRuleBlock(block);
34 int n = 40;
35 flScalar mse = 0;
36 for (fl::flScalar in = x->minimum(); in < x->maximum();
          in += (x->minimum() + x->maximum()) / n) {
37
38
      x->setInput(in);
      engine.process();
39
      flScalar expected = f_x->term(0)->membership(in);
40
      flScalar obtained = f_x->output().defuzzify();
41
      flScalar se = (expected - obtained) * (expected - obtained);
      mse += isnan(se) ? 0 : se;
      FL_LOG("x=" << in << "\texpected_out=" << expected << "\tobtained_out=" << obtained
              << "\tse=" << se);
45
46 }
47 FL_LOG("MSE=" << mse / n);
```

The output of this piece of code is the following.

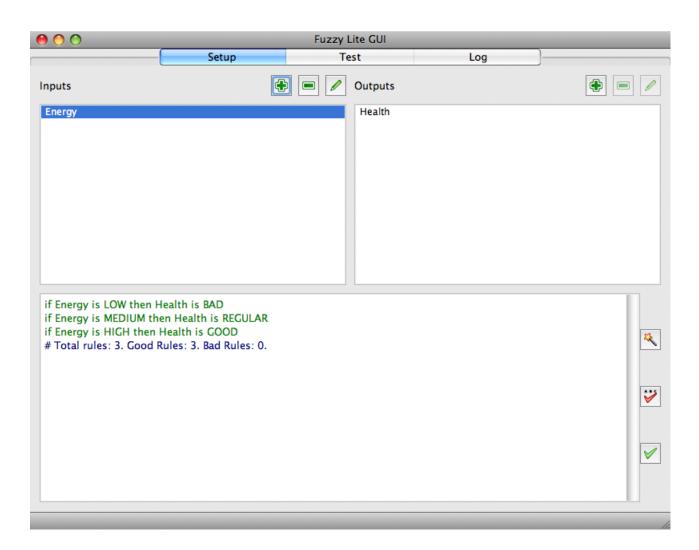
x=0.000	expected_out=nan	obtained_out=nan	se=nan
x=0.250	expected_out=0.990	obtained_out=0.840	se=0.022
x=0.500	expected_out=0.959	obtained_out=0.840	se=0.014
x=0.750	expected_out=0.909	obtained_out=0.840	se=0.005
x=1.000	expected_out=0.841	obtained_out=0.840	se=0.000
x=1.250	expected_out=0.759	obtained_out=0.743	se=0.000
x=1.500	expected_out=0.665	obtained_out=0.645	se=0.000
x=1.750	expected_out=0.562	obtained_out=0.547	se=0.000
x=2.000	expected_out=0.455	obtained_out=0.450	se=0.000
x=2.250	expected_out=0.346	obtained_out=0.347	se=0.000
x=2.500	expected_out=0.239	obtained_out=0.245	se=0.000
x=2.750	expected_out=0.139	obtained_out=0.142	se=0.000
x=3.000	expected_out=0.047	obtained_out=0.040	se=0.000
x=3.250	expected_out=-0.033	obtained_out=-0.015	se=0.000
x=3.500	expected_out=-0.100	obtained_out=-0.070	se=0.001
x=3.750	expected_out=-0.152	obtained_out=-0.125	se=0.001
x=4.000	expected_out=-0.189	obtained_out=-0.180	se=0.000
x=4.250	expected_out=-0.211	obtained_out=-0.183	se=0.001

x=4.500	$\alpha_{\text{whost}} = 0$ $\alpha_{\text{whost}} = 0$ $\alpha_{\text{whost}} = 0$	obtained_out=-0.185	se=0.001
	expected_out=-0.217		
x=4.750	expected_out=-0.210	obtained_out=-0.188	se=0.001
x=5.000	expected_out=-0.192	obtained_out=-0.190	se=0.000
x=5.250	expected_out=-0.164	obtained_out=-0.153	se=0.000
x=5.500	expected_out=-0.128	obtained_out=-0.115	se=0.000
x=5.750	expected_out=-0.088	obtained_out=-0.078	se=0.000
x=6.000	expected_out=-0.047	obtained_out=-0.040	se=0.000
x = 6.250	expected_out=-0.005	obtained_out=-0.007	se=0.000
x=6.500	expected_out=0.033	obtained_out=0.025	se=0.000
x=6.750	expected_out=0.067	obtained_out=0.058	se=0.000
x=7.000	expected_out=0.094	obtained_out=0.090	se=0.000
x=7.250	expected_out=0.114	obtained_out=0.098	se=0.000
x=7.500	expected_out=0.125	obtained_out=0.105	se=0.000
x=7.750	expected_out=0.128	obtained_out=0.112	se=0.000
x=8.000	expected_out=0.124	obtained_out=0.120	se=0.000
x=8.250	expected_out=0.112	obtained_out=0.100	se=0.000
x=8.500	expected_out=0.094	obtained_out=0.080	se=0.000
x=8.750	expected_out=0.071	obtained_out=0.060	se=0.000
x=9.000	expected_out=0.046	obtained_out=0.040	se=0.000
x=9.250	expected_out=0.019	obtained_out=0.040	se=0.000
x=9.500	expected_out=-0.008	obtained_out=0.040	se=0.002
x=9.750	expected_out=-0.033	obtained_out=0.040	se=0.005
MSE=0.001			

Appendix

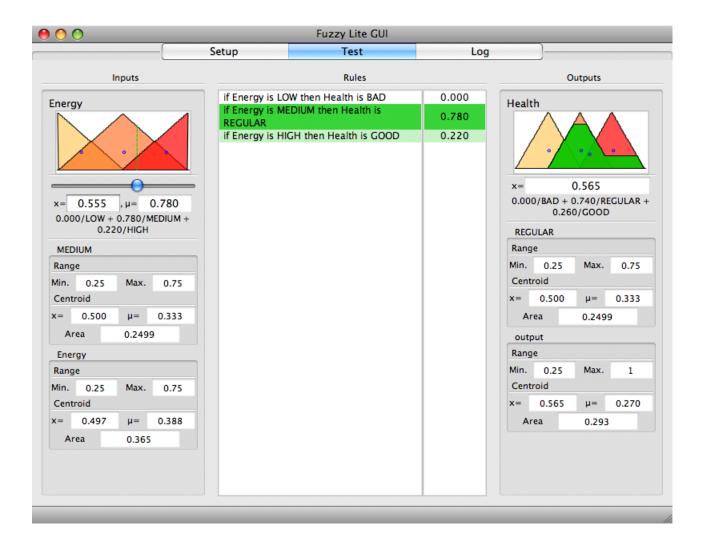
GUI Setup

The following figure shows the Setup part of the GUI build for FuzzyLite v1.5.



GUI Setup

The following figure shows the Setup part of the GUI build for FuzzyLite v1.5.



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