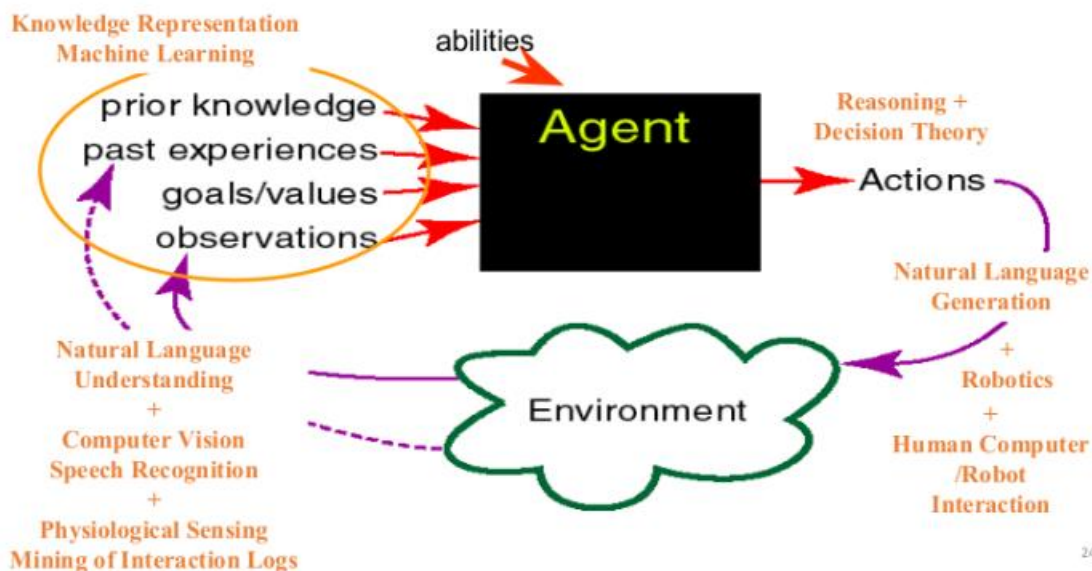


## AI UNIT 1

### At a glance

- Intelligence (AI) is usually defined as the science of making computers do things that require intelligence when done by humans.
- It is the simulation of human intelligence processes by machines, especially computer systems.
- **Four views of AI**
  - Think like human
  - Think Rationally
  - Act like humans
  - Act Rationally
- **Major components of AI**
  - NLP (communicate in language)
  - Knowledge representation (to store what it knows)
  - Automated reasoning (use knowledge to answer questions and draw conclusions)
  - Machine learning (adapt to new circumstances; prediction)
  - Vision
  - Robotics
- **Agent (An entity that interacts with its environment)**

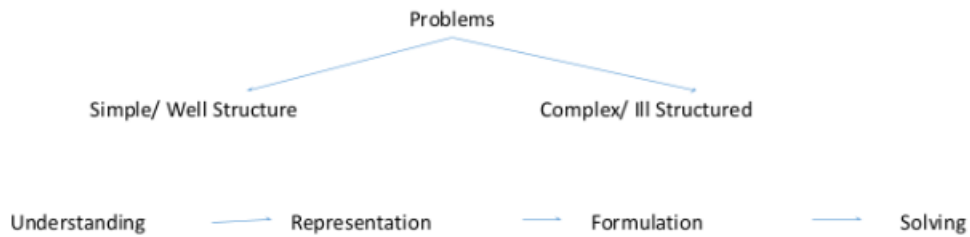


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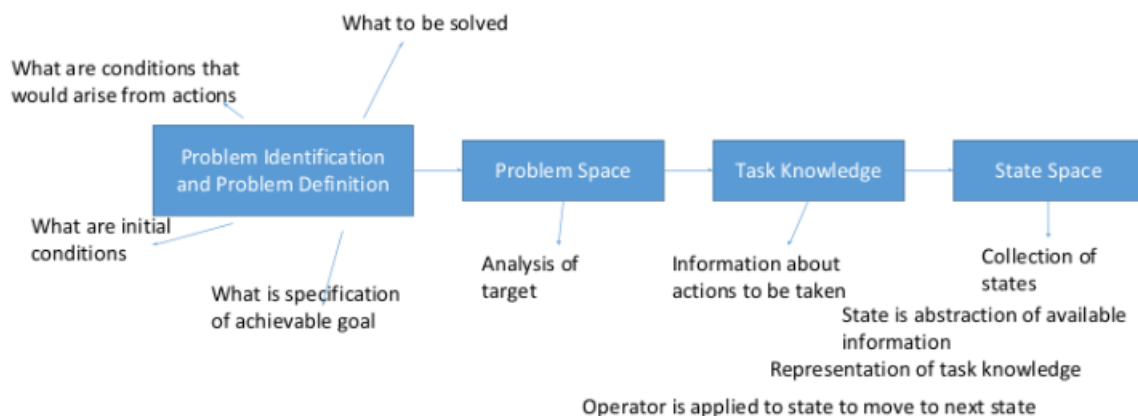
- Robots (Artificial agents having physical presence)
- Software agents (Agents without a physical presence)
- Rational agents (They sense something and do react on it)

- **PEAS (Performance measure, Environment, Actuators, Sensors)**
  - Must first specify the setting for intelligent agent design
  - Example Medical diagnosis system, Part-picking robot, Interactive English tutor
- **Environment (Surrounding)**
  - **Fully observable (accessible)**
    - Agent sensor detects all aspect of environment relevant to choose of action
    - Example Chess
  - **Partially observable (inaccessible)**
    - Environment could be partially observable due to noisy, inaccurate or missing sensors or inability to measure everything which is needed.
    - Example Driving
  - **Deterministic**
    - Deterministic environment is one in which any action has a single guaranteed effect
    - There is no uncertainty
    - Example Internet shopping
  - **non-deterministic (stochastic)**
    - Non-deterministic environments present greater problems for the agent designer
    - Example Taxi Driver
  - **Static**
    - Static environment is one that can be assumed to remain unchanged except by the performance of actions by the agent
    - Example Crossword puzzle
  - **Dynamic**
    - Dynamic environment is one that has other processes operating on it, and which hence changes in ways beyond the agent's control.
    - The physical world is a highly dynamic environment
    - Example Part picking robot
  - **Discrete**
    - An environment is discrete if there are a fixed, finite number of actions and precepts in it
    - Example Chess game
  - **Continuous**
    - Continuous environments have a certain level of mismatch with computer systems
    - Example taxi driving
  - **Single agent**
    - An agent operating by itself in an environment in single agent.
    - Example Part picking robot
  - **Multiagent**
    - Multi agent is when other agents are present (Two or more agents)
    - Example Game playing like chess

- **Problem Solving:**

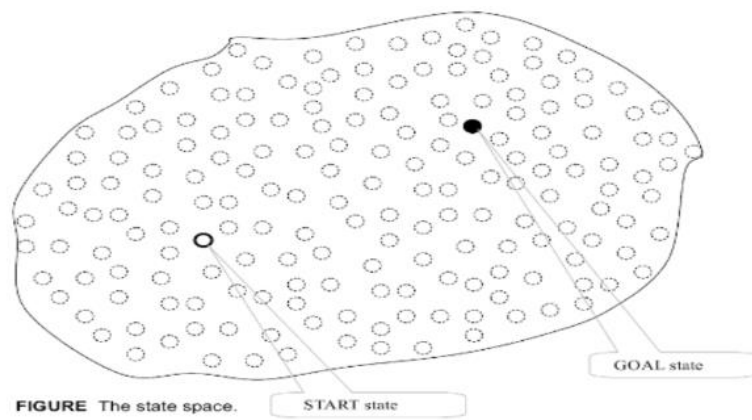


- General Problem-solving techniques involve:
  - Problem Identification
  - Problem analysis and representation
  - Planning
  - Execution
  - Evaluation of solution
  - Consolidating gains
- Problem Formulation



- Problem Analysis and Representation
  - Performance of solution depends on Problem Representation
- PROBLEM DEFINITION should satisfy:
  - Compactness (must be able to restrict and define boundaries clearly)
  - Utility (must be able to restrict and define boundaries clearly)
  - Soundness (should not report false)
  - Completeness (should not lose any information)
  - Generality (should be able to capture maximum instance of problem)
  - Transparency (reasoning with representation efficiently)
- **State Space**
  - A SET, consisting of all possible CONFIGURATIONS of a SYSTEM
  - Can be a finite / infinite set
  - Goes from (start state → goal state)
  - One State can change to its NEIGHBORING State with 1 VALID MOVE
  - Valid moves change a state to its neighbouring state

# State Space



- We can apply this state space to games like Missionaries and Cannibals, Water jug problem

## AI UNIT 2

### At a glance

- **Evaluating Search Strategies**
  - Completeness
  - Time Complexity
  - Space Complexity
  - Optimality/Admissibility
- **Uninformed Search** (easy, very inefficient in most cases of huge search tree)
  - **Breadth-First search** (Expand shallowest unexpanded node)
    - Complete? → Yes, it always reaches goal (if  $b$  is finite)
    - Time complexity →  $O(b^{d+1})$
    - Space complexity →  $O(b^{d+1})$
    - It is optimal only space increases as size of problem increases
  - **Depth-First search** (Expand deepest unexpanded node)
    - Complete? → No: fails in infinite-depth spaces
    - Time complexity →  $O(b^m)$  with  $m$ =maximum depth, terrible if  $m$  is much larger
    - Space complexity →  $O(bm)$
    - It's not optimal
  - **Uniform-Cost search** (queue ordered by path cost Equivalent to breadth-first)
    - Complete? → Yes, if step cost  $\geq \epsilon$
    - Time complexity →  $O(\text{of nodes with path cost} \leq \text{cost of optimal solution})$
    - Space complexity →  $O(\text{of nodes with path cost} \leq \text{cost of optimal solution})$
    - It is optimal for any step cost.
  - **Depth-First Iterative Deepening search** (avoids the infinite depth problem of DFS)
    - Searches nodes up to a depth
    - Complete? → Yes
    - Time complexity →  $O(b^d)$
    - Space complexity →  $O(bd)$
    - It is optimal if step cost = 1 or increasing function of depth.
  - **Bi-Directional Search**
    - Time and space complexity are  $O(b^{d/2})$

Criterion	Breadth-First	Uniform-Cost	Depth-First	Depth-Limited	Iterative Deepening
Complete?	Yes	Yes	No	No	Yes
Time	$O(b^{d+1})$	$O(b^{\lceil C^*/\epsilon \rceil})$	$O(b^m)$	$O(b^l)$	$O(b^d)$
Space	$O(b^{d+1})$	$O(b^{\lceil C^*/\epsilon \rceil})$	$O(bm)$	$O(bl)$	$O(bd)$
Optimal?	Yes	Yes	No	No	Yes

- **Solution to repeated states** (do not create paths containing cycles (loops), never generate a state generated before)
- **Informed Search** (uses problem-specific information to reduce the search tree into a small one)

- **Best First Search**

- Uses an evaluation function,  $f(n)$
- The path cost  $g$  is one of the examples,  $h(n)$  is required
- Note  $f(n) = g(n) + h(n)$
- less space, faster
- Types
  - **A\* Search** (A Star algorithm is a best first graph search algorithm that finds a least cost path from a given initial node to one goal node)
    - Evaluation function  $\rightarrow f(n)=g(n)+h(n)$
    - It stops when  $f(n) == 0$
    - If there is solution A\* will find it, which makes this search algorithm complete
    - It is more accurate than greedy search
    - Use case: Disneyland Paris, 8 Puzzle problem
    - Time Complexity  $\rightarrow$  Exponential with path length
    - Space Complexity  $\rightarrow$  **It is a problem** as it keeps generating the nodes
  - **Greedy Search**
    - Tries to expand the node
    - Just evaluates the node  $n$  by heuristic function:  $f(n) = h(n)$
    - It is good ideally, poor practically
    - Similar to depth-first search, not optimal, incomplete, suffers from the problem of repeated states
    - Time complexity depends on  $h(n)$  in general it is  **$O(bm)$** .
    - **$O(bm)$**  is also **space complexity**

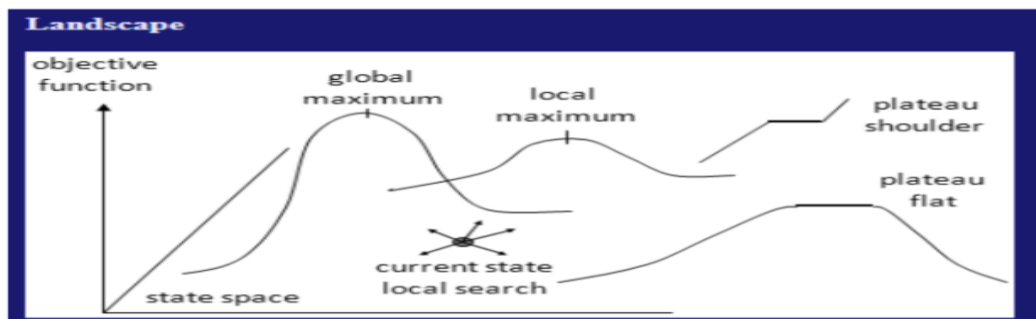
- **Hill climbing** (Hill climbing search is a local search problem. The purpose of the hill climbing search is to climb a hill and reach the topmost peak/ point of that hill)

- From the current state it moves to adjacent states going uphill and the algorithm **ends when** it **reaches** a peak (**local or global maximum**).
- Types of HC
  - Simple hill climbing search
    - The task is to reach the highest peak of the mountain. Here, the movement of the climber depends on his move/steps.
    - If he finds his next step better than the previous one, he continues to move else remain in the same state.
  - Steepest-ascent hill climbing
    - Unlike simple hill climbing search, It considers all the successive nodes, compares them, and choose the node which is closest to the solution.
    - Similar to best-first search

- Stochastic hill climbing
  - Stochastic hill climbing does not focus on all then odes. It selects one node at random and decides whether it should be expanded or search for a better one.
- Random-restart hill climbing
  - Random-restart algorithm is based on try and try strategy.
  - It iteratively searches the node and selects the best one at each step until the goal is not found.
- Limitations of Hill climbing algorithm
  - Local Maxima (Stuck at local maxima)
  - Plateau (If it is stuck at plateau, it is hard for algo to decide where to go)
  - Ridges (Two or more local maxima)
- Applications of HC
  - Marketing
  - Robotics
  - Job Scheduling

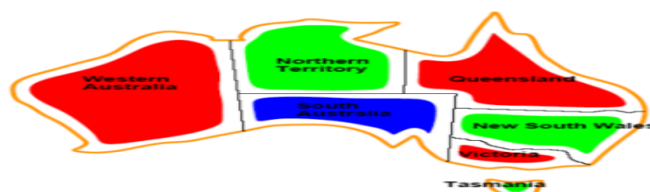
- Beam search
- Algorithm A

- Heuristics-Local Search Algorithms (where the path cost does not matter, and it only focus on solution-state needed to reach the goal node)
  - It uses a single search path of solutions, not a search tree.
  - Local Search often needs to start from an initialized solution



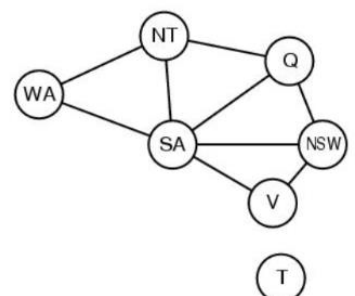
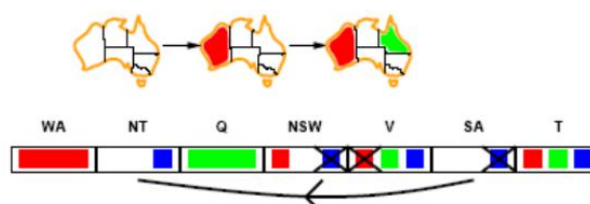
- Optimization-Hill Climbing
- Constraint Satisfaction Problem

- An assignment is complete when every variable is mentioned.
- A solution to a CSP is a complete assignment that satisfies all constraints.
- Example: map colouring



- Solutions are assignments satisfying all constraints, e.g.  
 $\{WA=red, NT=green, Q=red, NSW=green, V=red, SA=blue, T=green\}$

- Applications:
  - Scheduling the time of observations on the Hubble Space Telescope
  - Airline schedules
  - Cryptography
  - Computer Vision
- Types of CSP
  - Discrete variables (Finite domains; size  $d \Rightarrow O(d^n)$  complete assignments)
  - Infinite domains (Infinite solutions exist)
- Varieties of constraints
  - Unary constraints (involve a single variable)
  - Binary constraints (involve pairs of variables)
  - Higher-order (constraints involve 3 or more variables)
- CSP can be expressed as
  - a standard search problem
  - Commutative problem
- Backtracking search for CSP
  - Similar to Depth-first search
  - Chooses values for one variable at a time and backtracks when a variable has no legal values left to assign
- Its efficiency can be improved by heuristics
  - Forward checking (Forward checking idea: keep track of remaining legal values for unassigned variables)
  - Minimum remaining values (choose variable with the fewest legal moves)
- Constraint propagation
  - Techniques like CP and FC are in effect eliminating parts of the search space
  - Constraint propagation goes further than FC by repeatedly enforcing constraints locally
  - It has techniques like
    - Arc consistency
      - Arc consistency detects failure earlier than FC



- K-consistency (As all the inconsistencies are not detected by Arc consistency)

- Trade off of consistency checks
  - Takes more time
  - will reduce branching factor



- Further improvements
    - Checking special constraints
    - Intelligent backtracking
    - Local search for CSPs
- Games vs. Search Problems
  - specifying a move for every possible opponent reply
  - unlikely to find goal
- Mini-Max Terminology
  - Utility (function the function applied to leaf nodes)
  - Backed-up value (Min position or max position)
  - Procedure (search down several levels; at the bottom level apply the utility function, back-up values all the way up to the root node, and that node selects the move)
- Minimax (Perfect play for deterministic games)
  - Logic

**function** MINIMAX-DECISION(*state*) *returns an action*

$v \leftarrow \text{MAX-VALUE}(\text{state})$

**return** the *action* in SUCCESSORS(*state*) with value *v*

---

**function** MAX-VALUE(*state*) *returns a utility value*

**if** TERMINAL-TEST(*state*) **then return** UTILITY(*state*)

$v \leftarrow -\infty$

**for** *a, s* in SUCCESSORS(*state*) **do**

$v \leftarrow \text{MAX}(v, \text{MIN-VALUE}(s))$

**return** *v*

---

**function** MIN-VALUE(*state*) *returns a utility value*

**if** TERMINAL-TEST(*state*) **then return** UTILITY(*state*)

$v \leftarrow \infty$

**for** *a, s* in SUCCESSORS(*state*) **do**

$v \leftarrow \text{MIN}(v, \text{MAX-VALUE}(s))$

**return** *v*

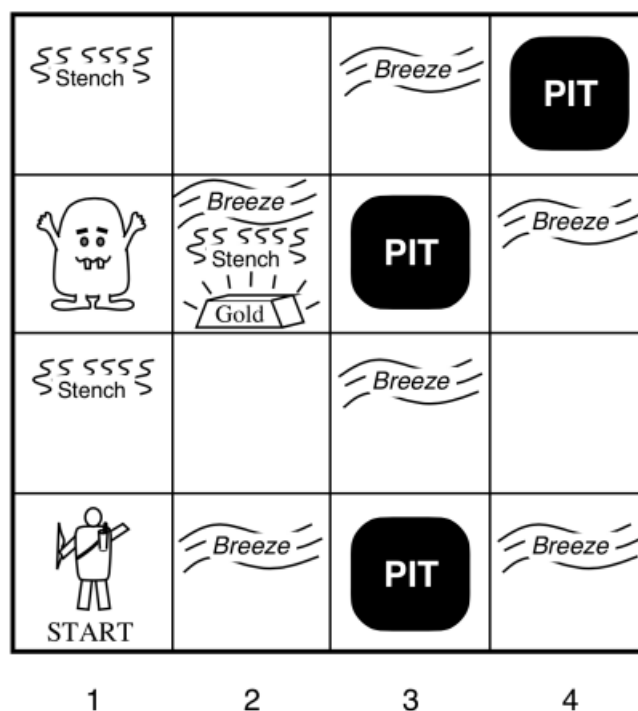
- Properties of Minimax
    - Tree generated is finite
    - Optimal against an optimal opponent
    - Time complexity  $\rightarrow O(b^m)$
    - Space complexity  $\rightarrow O(bm)$  (depth-first exploration)
  - Alpha-Beta Procedure
    - The alpha-beta procedure can speed up a depth-first minimax search.
      - ❖ Alpha: a lower bound on the value that a max node may ultimately be assigned ( $v > \alpha$ ) else we don't consider that nodes
      - ❖ Beta: an upper bound on the value that a minimizing node may ultimately be assigned ( $v < \beta$ ) else we don't consider that nodes

- Pruning does not affect final result.
  - With "perfect ordering," time complexity =  $O(b^{m/2})$ , doubles depth of search
- Additional Refinements
  - Waiting for Quiescence (continue the search until no drastic change occurs from one level to the next)
  - Secondary Search (after choosing a move, search a few more levels beneath it to be sure it still looks good)
  - Book Moves for some parts of the game keep a catalogue of best moves to make.
- Samuel's Checker Player
  - In learning mode (Computer acts as 2 players: A and B)
    - A adjusts its coefficients after every move
    - B uses the static utility function
    - If A wins, its function is given to B
  - A can change function by
    - Coefficient replacement
    - Term Replacement
- Kalah
  - To move, pick up all the stones in one of your holes, and put one stone in each hole, starting at the next one, including your Kalah and skipping the opponent's Kalah.
  - The winner is the player who has the most stones in his Kalah at the end of the game.
- Games
  - Single Agent Games
  - Two-Agent Games
  - Optimal Decisions in Games Min-Max Algorithm Pruning
  - Stochastic Games
- Games of Chance
  - We use minimax here as well
  - Instead of  $O(b^m)$ , it is  $O(b^m n^m)$  where  $n$  is the number of chance outcomes.
  - Since the complexity is higher (both time and space), we cannot search as deeply.

## AI Unit 3

### At a glance

- **Logical Agents** (Agents that can form representations of a complex world, use a process of inference to derive new representations about the world)
- **Knowledge-Based Agents**
  - The central component of a knowledge-based agent is its **knowledge base**, or KB (set of sentences).
  - Each **sentence is** expressed in a language called a **knowledge representation language**.
  - When the sentence is taken as being given without being derived from other sentences, it is called as **axiom**
  - They can do two operations to give inference
    - Tell (Add new sentences)
    - Ask (Query what is known)
- **The Wumpus World**



- **PEAS**
  - Performance measure (gold +1000, death (eaten or falling in a pit) - 1000, -1 per action taken, -10 for using the arrow. The game ends either when the agent dies or comes out of the cave)

- **Environment:**
    - Breeze is near pit
    - Stench is near Wumpus
    - 1000 Gold
  - **Actuators:**
    - Left turn, Right turn, Forward, Grab, Release, Shoot
  - **Sensors:**
    - Stench, Breeze, Glitter, Bump, Scream
  - **Wumpus World properties**
    - Partially observable, Static, Discrete, Single-agent, Deterministic and Sequential
- **Knowledge Representation and Knowledge Base**
  - Example Marcus is a man → man (Marcus)
  - **A good knowledge base has**
    - Representation adequacy (Ability to represent all kinds of knowledge that are needed in the domain)
    - Inferential adequacy (Ability to manipulate representational structures such that new knowledge can be derived/inferred from the old)
    - Inferential efficiency (Ability to incorporate additional information into an existing knowledge base that can be used to focus the attention of inference mechanisms in the most promising direction)
    - Acquisitional efficiency (Ability to easily acquire new information)
  - **Approaches to knowledge Representation**
    - Simple Rational Knowledge
      - ❖ Provide weak inferential ability
    - Inheritable knowledge
      - ❖ Objects are organized into classes and classes are organized in a generalization hierarchy.
      - ❖ **Inheritance** is a **powerful form of inference**, but **not adequate**.
    - Inferential knowledge
      - ❖ Facts represented in a logical form, which facilitates reasoning
      - ❖ An inference engine is required
    - Procedural knowledge
      - ❖ Representation of "how to make it" rather than "what it is".
      - ❖ May have inferential efficiency, but no inferential adequacy and acquisitional efficiency
    - Issues in KR
      - ❖ Important Attributes: Isa and instance attributes.
      - ❖ Relationships among attributes (inverses, existence in a hierarchy, single-valued attributes, techniques for reasoning about values)
      - ❖ Choosing the Granularity (High-level facts may not be adequate for inference. Low-level primitives may require a lot of storage)
      - ❖ Representing Set of Objects
      - ❖ Finding the right structure as needed
- **Logic, Propositional Logic: A Very Simple Logic**
  - **Logics** (are formal languages for representing knowledge to extract conclusions)
    - Syntax (defines well-formed sentences in the language)
    - Semantic (defines the truth or meaning of sentences in a world)

- Propositional logic

- Proposition  $\rightarrow$  declarative sentence
- Properties of statement:
  - Satisfiability (a sentence is satisfiable if there is an interpretation for which it is true)
  - Contradiction (if there is no interpretation for which sentence is true)
  - Validity (a sentence is valid if it is true for every interpretation)
- Inference Rules
  - Commutativity:  $p \wedge q = q \wedge p$ ,  $p \vee q = q \vee p$
  - Associativity:  $(p \wedge q) \wedge r = p \wedge (q \wedge r)$ ,  $(p \vee q) \vee r = p \vee (q \vee r)$
  - Identity element:  $p \wedge \text{True} = p$ ,  $p \vee \text{False} = p$
  - $\neg(\neg p) = p$
  - $p \wedge p = p$ ,  $p \vee p = p$
  - Distributivity  $p \wedge (q \vee r) = (p \wedge q) \vee (p \wedge r)$ ,  $p \vee (q \wedge r) = (p \vee q) \wedge (p \vee r)$
  - $p \wedge (\neg p) = \text{False}$  and  $p \vee (\neg p) = \text{True}$
  - DeMorgan's laws  $\neg(p \wedge q) = (\neg p) \vee (\neg q)$ ,  $\neg(p \vee q) = (\neg p) \wedge (\neg q)$

Modus Ponens	$p \implies q$ $p$ $\therefore q$	Modus Tollens	$p \implies q$ $\sim q$ $\therefore \sim p$
Elimination	$p \vee q$ $\sim q$ $\therefore p$	Transitivity	$p \implies q$ $q \implies r$ $\therefore p \implies r$
Generalization	$p \implies p \vee q$ $q \implies p \vee q$	Specialization	$p \wedge q \implies p$ $p \wedge q \implies q$
Conjunction	$p$ $q$ $\therefore p \wedge q$	Contradiction Rule	$\sim p \implies F$ $\therefore p$

- Given an implication  $p \rightarrow q$ 
  - converse is:  $q \rightarrow p$
  - contrapositive is:  $\neg q \rightarrow \neg p$
  - inverse is:  $\neg p \rightarrow \neg q$

- **Convert to CNF**

- Eliminate implications and biconditionals using formulas
- Apply De-Morgan's Law and reduce NOT symbols so as to bring negations before the atoms
- Use distributive and other laws & equivalent formulas to obtain Normal forms

Q. Convert into CNF :  $((P \rightarrow Q) \rightarrow R)$

Solution:

$$\begin{aligned} \text{Step 1: } ((P \rightarrow Q) \rightarrow R) &\implies ((\neg P \vee Q) \rightarrow R) \\ &\implies \neg(\neg P \vee Q) \vee R \end{aligned}$$

$$\text{Step 2: } \neg(\neg P \vee Q) \vee R \implies (P \wedge \neg Q) \vee R$$

$$\text{Step 3: } (P \wedge \neg Q) \vee R \implies (P \vee R) \wedge (\neg Q \vee R)$$


  
CNF

- **Resolution in propositional logic**

- Proof by Refutation / contradiction
  - ❖ Say we have to prove proposition A Assume A to be false i.e.,  $\neg A$
  - ❖ Continue solving the algorithm starting from  $\neg A$
  - ❖ If you get a contradiction (F) at the end it means your initial assumption i.e.,  $\neg A$  is false and hence proposition A must be true.
  - ❖ Clause: **disjunction of literals is called clause**

- **First-Order Logic** (Theorem deciding is semi decidable)

- Can Represent  $\rightarrow$  Objects and quantification
- Ex Everyone loves john  $\rightarrow \forall x: \text{loves}(\text{Everyone}, x)$  where  $\forall$  is universal quantifier (Represents **all**)
- Also  $\exists$  represents **some** ex somebody kills xyz  $\rightarrow \exists x \text{ kills } (x, \text{xyz})$
- Nested quantifier example
  - ❖ everybody loves somebody  $\rightarrow \forall x: \exists y: \text{loves } (x, y)$

- DeMorgan's rules

$$\begin{aligned}
 \neg \exists x \quad P &\equiv \forall x \quad \neg P & \neg(P \vee Q) &\equiv \neg P \wedge \neg Q \\
 \neg \forall x \quad P &\equiv \exists x \quad \neg P & \neg(P \wedge Q) &\equiv \neg P \vee \neg Q \\
 \forall x \quad P &\equiv \neg \exists x \quad \neg P & P \wedge Q &\equiv \neg(\neg P \wedge \neg Q) \\
 \exists x \quad P &\equiv \neg \forall x \quad \neg P & P \vee Q &\equiv \neg(\neg P \wedge \neg Q).
 \end{aligned}$$

- Knowledge Engineering in First-Order Logic Inferences:
  - ❖ IDENTIFY THE QUESTIONS.
  - ❖ ASSEMBLE THE RELEVANT KNOWLEDGE.
  - ❖ DECIDE ON A VOCABULARY OF PREDICATES, FUNCTIONS, AND CONSTANTS.
  - ❖ ENCODE GENERAL KNOWLEDGE ABOUT THE DOMAIN.
  - ❖ ENCODE A DESCRIPTION OF THE PROBLEM INSTANCE.
  - ❖ POSE QUERIES TO THE INFERENCE PROCEDURE AND GET ANSWERS.
  - ❖ DEBUG AND EVALUATE THE KNOWLEDGE BASE.
- Inference in First-Order Logic (Reduce first-order inference to propositional Inference)
  - ❖ Universal Instantiation/ Elimination
    - In general, the rule of Universal Instantiation says that we can infer any sentence obtained by substituting a ground term (a term without variables) for a universally quantified variable.
  - ❖ Existential Instantiation/ Elimination
    - Basically, the existential sentence says there is some object satisfying a condition, and applying the existential instantiation rule just gives a name to that object.
    - The new name is called a Skolem constant.

❖ Existential Introduction

- example, we no longer need  
 $\exists x \text{ Kill}(x, \text{Victim})$
- once we have added the sentence  
 $\text{Kill}(\text{Murderer}, \text{Victim})$

- ❖ Generalized Modus Ponens (modified form of Modus ponens)
  - we use a single inference rule called Generalized Modus Ponens for the inference process.
  - "P implies Q, and P is declared to be true, hence Q must be true," summarizes Generalized Modus Ponens.
- ❖ Inference Principles
  - Unification & Resolution
    - ✓ Matching procedure that compares two literals and discovers whether there exists a set of substitutions that can make them identical
  - Forward Chaining Rules (Bottom-up process)
    - ✓ From the known facts, it triggers all the rules whose premises are satisfied, adding their conclusions to the known facts.
    - ✓ The process repeats until the query is answered
  - Backward Chaining Rules
    - ✓ Starting from the Goals, chaining through all the rules.
    - ✓ Top-down process

- Steps to be followed for Resolution Inference

- ❖ Eliminate existential quantifiers
- ❖ STANDARDIZE VARIABLES
- ❖ SKOLEMIZE (Skolemization is the process of removing existential quantifiers by elimination)
- ❖ DROP UNIVERSAL QUANTIFIERS
- ❖ DISTRIBUTE  $\vee$  OVER  $\wedge$

- Instance and Isa relationship

- ❖ "Marcus is a man" can be written as  $\text{man}(\text{Marcus})$  or  $\text{instance}(\text{Marcus}, \text{man})$
- ❖ "All Pomerians were Romans" can be written as  $\forall x: \text{Pomerians}(x) \rightarrow \text{Romans}(x)$
- ❖ So,  $\text{instance } \forall x \text{ instance } (x, \text{Pomerians}) \rightarrow \text{instance } (x, \text{Romans})$
- ❖ This can be written as  $\text{Isa}(\text{Pomerians}, \text{Roman})$



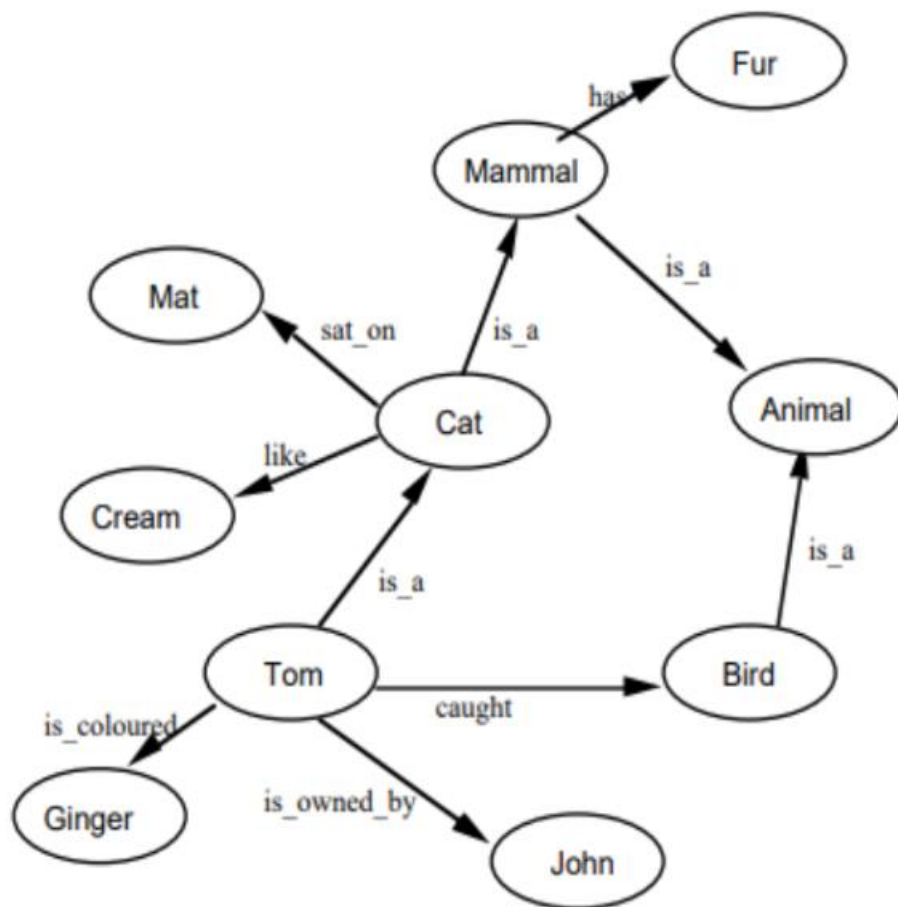
- **Representation-Production**

- **Logical Representation**

- Hierarchical task networks for reasoning about plans
    - Bayesian networks for reasoning with uncertainty
    - Markov models for reasoning over time
    - Deep neural networks for reasoning about images, sounds, and other data

- **Semantic Networks**

- Idea is that we can store our knowledge in the form of a graph, with nodes representing objects in the world, and arcs representing relationships between those objects.
    - Semantic net allows us to perform inheritance reasoning as all members of a class, will inherit all the properties of superclass additional relation.



- **Production Rules**

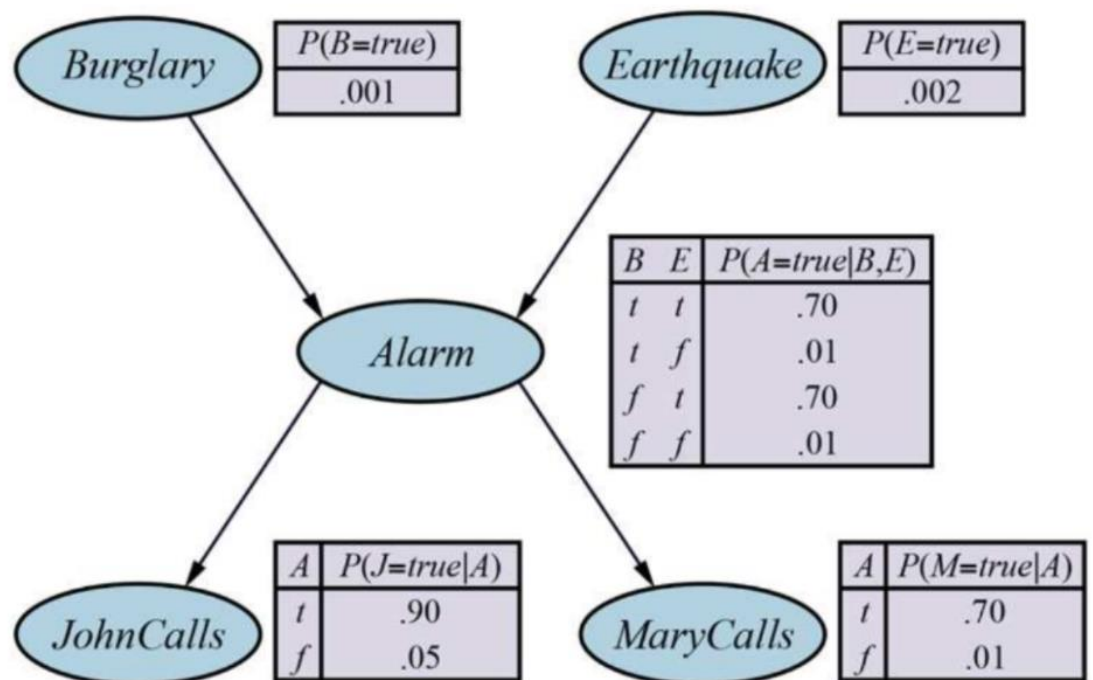
- Like in TOC

- **Frames Representation**

- Means of representing common sense knowledge. Knowledge is organized into small packets called “Frames”.
    - Frame can be defined as a structure that has slots for various objects & a collection of frames consists of expectation for a given situation.
    - Frame are used to represent two types of knowledge viz. declarative/factual and procedural, declarative & procedural Frames

- **Bayesian Belief Net**

- A Bayesian network is a directed graph in which each node is annotated with quantitative probability information.



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- **Dempster – Shafer Theory (DST)**

- DST is a mathematical theory of evidence based on belief functions and plausible reasoning. DST offers an alternative to traditional probabilistic theory for the mathematical representation of uncertainty.
- Bayesian methods are sometimes inappropriate so DST used
- Belief  $\leq$  Plausibility
- Mass function  $m(K)$  (It is an interpretation of  $m(\{K \text{ or } B\})$  i.e.; it means there is evidence for  $\{K \text{ or } B\}$  which cannot be divided among more specific beliefs for  $K$  and  $B$ .)
- Belief in  $K$  (It is an interpretation of  $m(\{K \text{ or } B\})$  i.e.; it means there is evidence for  $\{K \text{ or } B\}$  which cannot be divided among more specific beliefs for  $K$  and  $B$ )
- Plausibility in  $K$  (It is the sum of masses of set that intersects with  $K$ )