

**Indian Institute of Information Technology Sri City (IIITS)**

Name of the Exam: PS\_MID - I

Duration: 1.5 hrs

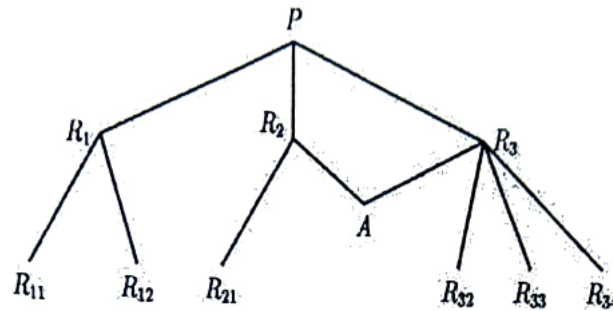
Max. Marks: 20

**Instructions:**

1. All questions are mandatory.
2. Marks are indicated in [ ] after each question.
3. Rough Work should be done separately, not in the answer sheet.
4. Answers should be reasoned and derived clearly, not a single word answer.
5. Preferably use a ballpoint pen.
6. You can use a calculator.

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1. An integer is chosen at random from 1 to 200. What is the probability that the integer is divisible by 6 or 8 ? [2 M]
  2. It is estimated that 50% of emails are spam emails. Some software has been applied to filter these spam emails before they reach your inbox. A certain brand of software claims that it can detect 99% of spam emails, and the probability for a false positive (a non-spam email detected as spam) is 5%. Now if an email is detected as spam, then what is the probability that it is in fact a non-spam email? [3 M]
  3. If A, B and C are mutually independent events show that  $(A \cup B)$  and C are also independent. [2M]
  4. The random variable X has the probability density function  $f(x) = a e^{-b|x|}$ ,  $-\infty < x < \infty$ . Find the relation between a and b. [2M]
  5. If a random variable X has a binomial distribution with mean 4 and the variance  $\frac{4}{3}$ . Find  $P(X \geq 1)$ . Comment upon the nature of the distribution (skewness and kurtosis). [3M]

6. Esow Alben is an Indian bicyclist who leaves a point P (see Figure), choosing one of the roads PR1 , PR2 , PR3 at random. At each subsequent crossroad, he again chooses an available road at random.



What is the probability that he will arrive at point A?

[3 M]

7. The probability density function of the age of babies, "x" years, being brought to a clinic is given by

$$f(x) = \frac{3}{4}x(2 - x) \text{ if } 0 < x < 2$$

$$= 0 \text{ otherwise}$$

If 60 babies are brought in on a particular day, how many are expected to be under 8 months old?

[3 M]

8. Suppose the moment generating function of the random variable X is given by

$$M_X(t) = 0.1 e^t + 0.2 e^{2t} + 0.3 e^{3t} + 0.4 e^{4t}.$$

(a). Find the Distribution Function of X.

[1 M]

(b). Find Var [X].

[0.5 M]

(c). Find the Median of X.

[0.5 M]

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