

Indian Institute of Information Technology Sri City (IIITS)

Name of the Exam: PS_MID - I

Duration: 1.5 hrs

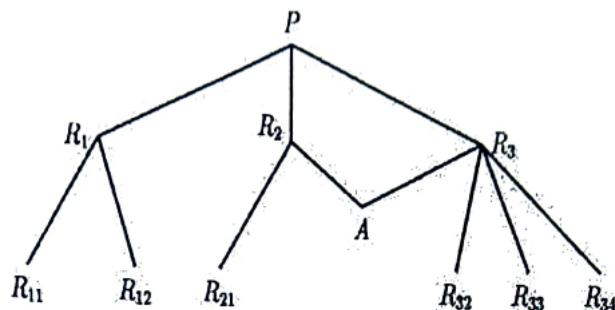
Max. Marks: 20

Instructions:

1. All questions are mandatory.
 2. Marks are indicated in [] after each question.
 3. Rough Work should be done separately, not in the answer sheet.
 4. Answers should be reasoned and derived clearly, not a single word answer.
 5. Preferably use a ballpoint pen.
 6. You can use a calculator.
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1. An integer is chosen at random from 1 to 200. What is the probability that the integer divisible by 6 or 8 ? [2 M]
2. It is estimated that 50% of emails are spam emails. Some software has been applied to filter these spam emails before they reach your inbox. A certain brand of software claims that it can detect 99% of spam emails, and the probability for a false positive (a non-spam email detected as spam) is 5%. Now if an email is detected as spam, then what is the probability that it is in fact a non-spam email? [3 M]
3. If A, B and C are mutually independent events show that $(A \cup B)$ and C are also independent. [2M]
4. The random variable X has the probability density function $f(x) = a e^{-bx}$, $-\infty < x < \infty$. Find the relation between a and b. [2M]
5. If a random variable X has a binomial distribution with mean 4 and the variance $\frac{4}{3}$. Find $P(X \geq 1)$. Comment upon the nature of the distribution (skewness and kurtosis). [3M]

6. Esow Alben is an Indian bicyclist who leaves a point P (see Figure), choosing one of the roads PR₁, PR₂, PR₃ at random. At each subsequent crossroad, he again chooses an available road at random.



What is the probability that he will arrive at point A?

[3 M]

7. The probability density function of the age of babies, "x" years, being brought to a clinic is given by

$$\begin{aligned} f(x) &= \frac{3}{4}x(2-x) \quad \text{if } 0 < x < 2 \\ &= 0 \quad \text{otherwise} \end{aligned}$$

If 60 babies are brought in on a particular day, how many are expected to be under 8 months old?

[3 M]

8. Suppose the moment generating function of the random variable X is given by

$$M_X(t) = 0.1 e^t + 0.2 e^{2t} + 0.3 e^{3t} + 0.4 e^{4t}.$$

(a). Find the Distribution Function of X.

[1 M]

(b). Find Var [X].

[0.5 M]

(c). Find the Median of X.

[0.5 M]

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