

# Indian Institute of Information Technology Sri City, Chittoor

Theory of Computation – Spring 2023

Mid 2 Examination

Duration: 90 Minutes

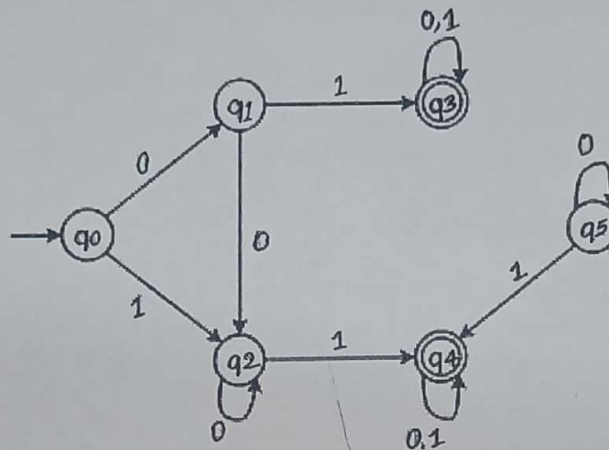
Date: 11/03/2023

Maximum Marks : 60

- It is a closed book exam.
- No electronic devices, books, any kind of material is allowed.

Q1. Answer the following:

Q1.(a). Apply Myhill-Nerode Theorem (the Table Filling Method) to minimize the following DFA. In the given DFA,  $Q = \{q_0, q_1, q_2, q_3, q_4, q_5\}$ ,  $F = \{q_3, q_4\}$ , and  $\Sigma = \{0, 1\}$ . [8 Marks]



Q1.(b) Convert the following CFG to CNF (Chomsky Normal Form). [10 Mark]

$$S \rightarrow ASB, A \rightarrow aAS|a| \epsilon, B \rightarrow SbS|A|bb$$

Q1.(c) Consider the following languages ( $L_1$ ,  $L_2$ ,  $L_3$ , and  $L_4$ ) over  $\Sigma = \{0, 1\}$ . For which of the following languages, we can construct DPDA accepted by an empty stack? [2 mark]

- (i)  $L_1 = 0^*$  (ii)  $L_2 = 0^*1$  (iii)  $L_3 = \{0^n 1^n \mid n \geq 0\}$  (iv)  $L_4 = \{0^n 1^n \mid n \geq 1\}$

Q2. For the given CFG apply CYK algorithm to find whether the strings (i) *abbabab* and (ii) *baabab* are in the language of the CFG or not. Students should strictly use the table filling algorithm given by the CYK method.

$$S \rightarrow XB|YA, X \rightarrow a, Y \rightarrow b, B \rightarrow b|YS|CB, C \rightarrow XB, A \rightarrow a|XS|DA, D \rightarrow YA \quad [10+10 = 20\text{Marks}]$$

**Q3.** Let  $\Sigma = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9\}$  be an alphabet. We know that the operation  $(\text{mod } 3)$  is an equivalence relation and it divides the strings into three equivalence classes, denoted as  $[0]$ ,  $[1]$ ,  $[2]$ . We define each class as  $[x] = \{y \in \Sigma^* \mid y (\text{mod } 3) = x\}$ , where  $x \in \{0, 1, 2\}$ , for example,  $[0] = \{0, 3, 6, 9, 12, 15, \dots\}$ . Assume that the strings  $w$  over  $\Sigma$  are identified as equivalent non-negative integers. If a string  $w = 001232$ , then the machine should skip (but, not avoid reading symbols from string) the starting 0s, that is,  $w$  will be identified as equivalent to number 1232 by the machine.

Finding the remainder using the number division method is defined with operation  $[x].y = xy (\text{mod } 3)$ , where  $x \in \{0, 1, 2\}$  and  $y \in \Sigma$ . We find the value of  $857 (\text{mod } 3)$  as follows. Note that we read strings from left to right.

- **Read 8 (first symbol):**  $8 = 08 = [0].8 = 08 (\text{mod } 3) = 2$ , this implies,  $8 \in [2]$
- **Read 5:**  $85 = [2].5 = 25 (\text{mod } 3) = 1$ , this implies,  $25 \in [1]$
- **Read 7:**  $857 = [1].7 = 17 (\text{mod } 3) = 2$ , this implies,  $857 \in [2]$

Assume “\$” is stack start symbol and the language is defined as  $L = \{w \in \Sigma^* \mid w \text{ contains at least two non-overlapping substrings } s, \text{ with } s (\text{mod } 3) = 1 \text{ and } |s| > 0\}$ . For example, consider the string **220392072** is in the language  $L$ . Then, **22** and **207** are two non-overlapping substrings yielding remainder 1 ( $\text{mod } 3$ ).

Using above theory, answer the following questions:

- Q3.(a). Explain clearly the logic step-wise to develop PDA to recognize the language  $L$ . [5M]  
 Q3.(b). Draw state transition diagram of PDA  $N(P)$ , accepting by empty stack, for the language  $L$ . [10M]  
 Q3.(c). Give all execution states that show the string 220392072 will accept by  $N(P)$ . [5M]

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