## Big List Problems $(9\frac{3}{4})$ :

## On Uniform Continuity and Parametrizations

- 1. Find parametrizations (in either 1 or 2 variables, whichever is appropriate) of the following surfaces in  $\mathbb{R}^3$ : (i) The "double cone" obtained by rotating the line y=x in the plane around the y-axis (ii) the intersection of the cone from part (i) with the sphere  $x^2+y^2+z^2=1$  and (iii) an infinitely long cylinder of radius r.
- **2.** (i) Find a continuous function  $\gamma: \mathbb{R} \to \mathbb{R}^2$  whose image is the set formed by the circle of radius 1 along with the square with vertices  $(\pm 1, \pm 1)$ . (In other words, find a parametrization of this set). (ii) Describe the image of the following curve in  $\mathbb{R}^3$ :  $\gamma(t) = (\cos t, \sin t, t)$
- **3.** Show that if  $f:A\to B$  is uniformly continuous on A, and  $g:B\to C$  is uniformly continuous on B, then  $g\circ f$  is uniformly continuous on A.
- **4.** If f and g are uniformly continuous and bounded, show that fg is uniformly continuous. Find a counterexample to this statement if we omit of boundedness hypothesis.