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1 Introduction

1.1 Notation

1. $f : \mathbb{R}^p \rightarrow \mathbb{R}^q$ really means $f : \mathbf{dom} f \rightarrow \mathbb{R}^q$

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