Introduction to Artificial Intelligence using Python

Week 3 of 4

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Course Overview

- ► Goal of this course is to introduce you to artificial intelligence (AI).
- Learn how to implement various AI algorithms in Python.
- Four weeks program.
 - 1. Python programming
 - 2. Data wrangling and visualization
 - 3. Machine learning
 - 4. Neural networks and deep learning
- ► AI project in parallel the course





Overview of week 3:

I What is Machine Learning?

II Linear vs Logistic regression

III Introduction to Clustering

IV Classification algorithms I

V Classification algorithms II





Day 1: What is Machine Learning?

- ▶ What does it mean to learn for a machine?
- Supervised vs Unsupervised Learning.
- Regression vs Classification problems.
- MSE, Accuracy, Precision and Recall.
- ► Training and testing datasets.





What does it mean to learn for a machine?

- Machines learn by acquiring knowledge or skills from data or experience.
- Learning enables machines to generalize from examples and make predictions or decisions on new data.
- Machine learning algorithms detect patterns in data to make informed decisions or predictions.
- Learning involves optimizing model parameters based on feedback or evaluation metrics.
- Learning for machines can be supervised, unsupervised, or reinforcement-based.





What does it mean to learn for a machine?

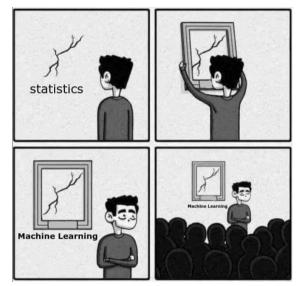




Fig. 1: Machine learning in a nutshell.



Supervised vs Unsupervised Learning.

- Supervised Learning: Uses labeled data to train a model and predict unseen inputs.
 - Requires labeled data.
 - Focuses on prediction.
 - Evaluation using metrics like accuracy or mean squared error.
 - Examples: Classification, Regression.
- ► **Unsupervised Learning**: Uses unlabeled data to discover patterns and relationships in the data.
 - Works with unlabeled data.
 - Focuses on discovering hidden patterns.
 - Evaluation can be subjective.
 - Examples: Clustering, Dimensionality Reduction.





Supervised vs Unsupervised Learning.

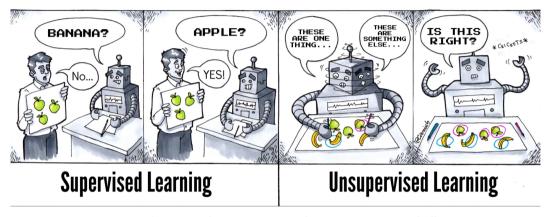


Fig. 2: Supervised vs Unsupervised Learning in a nutshell.





Regression vs Classification Problems

- **Regression**: Predicts continuous numerical values.
 - Utilizes algorithms like Linear Regression, Polynomial Regression.
 - Descrive: Minimize the difference between predicted and actual values.
 - Examples: Predicting house prices, estimating sales revenue.
 - $\{(X_i, Y_i)\}_{i=1}^n, \quad X_i \in \mathbb{R}^n, \quad Y_i \in \mathbb{R}^n$
- Classification: Predicts discrete categories or classes.
 - Utilizes algorithms like Logistic Regression, Decision Trees.
 - Descrive: Assign the correct class label to each input.
 - Examples: Email spam detection, image classification.
 - $\{(X_i, Y_i)\}_{i=1}^n, X_i \in \mathbb{R}^n, Y_i \in \{0, 1, \dots, C-1\}$





MSE, Accuracy, Precision, and Recall

Mean Squared Error (MSE):
Measures the average squared
difference between predicted and
actual values in regression problems.

$$MSE = \frac{1}{n} \sum_{i=1}^{n} (y_i - \hat{y_i})^2$$

► **Accuracy**: Measures the proportion of correctly classified instances in classification problems.

$$Accuracy = \frac{TP + TN}{TP + TN + FP + FN}$$

► **Precision**: Measures the proportion of true positive predictions among the predicted positive instances.

$$Precision = \frac{TP}{TP + FP}$$

Recall: Measures the proportion of true positive predictions among the actual positive instances.

$$Recall = \frac{TP}{TP + FN}$$





Training and Testing Datasets

Data Split:

- The training dataset typically comprises 80% of the data.
- The testing dataset typically comprises 20% of the data.
- This split helps evaluate the model's performance on unseen data.
- Training Dataset: Used to train the machine learning model.
 - Contains labeled data with input features (X) and corresponding target labels (y).
 - Used to estimate model parameters and learn patterns.
- **Testing Dataset**: Used to evaluate the performance of the trained model.
 - Contains unlabeled data with input features (X).
 - Model predictions are compared against the true target labels to assess performance metrics.
 - Ensures the model generalizes well to unseen data.





Day 2: Linear vs Logistic regression

- ► What is linear regression?
- ► MSE as a loss function
- ► How can we learn the model parameters?
- What is logistic regression?
- Log likelihood as a loss function
- ► How can we learn the model parameters?





- ► **Simplicity**: Straightforward to understand and implement.
- ▶ **Interpretability**: Coefficients provide clear interpretations of feature importance.
- Efficiency: Relatively low computational complexity.
- **Baseline Model**: Serves as a baseline to compare with advanced algorithms.





$$y_{1} = x_{1,1}\theta_{1} + x_{1,2}\theta_{2} + \dots + x_{1,p}\theta_{p} + \epsilon_{1}$$

$$y_{2} = x_{2,1}\theta_{1} + x_{2,2}\theta_{2} + \dots + x_{2,p}\theta_{p} + \epsilon_{2}$$

$$\vdots$$

$$y_{n} = x_{n,1}\theta_{1} + x_{n,2}\theta_{2} + \dots + x_{n,p}\theta_{p} + \epsilon_{n}$$





Notation:

$$\mathbf{Y} = \begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_n \end{bmatrix}, \quad \mathbf{X} = \begin{bmatrix} x_{11} & x_{12} & \dots & x_{1\rho} \\ x_{21} & x_{22} & \dots & x_{2\rho} \\ \vdots & \vdots & \ddots & \vdots \\ x_{n1} & x_{n2} & \dots & x_{n\rho} \end{bmatrix}, \quad \theta = \begin{bmatrix} \theta_1 \\ \theta_2 \\ \vdots \\ \theta_{\rho} \end{bmatrix}, \quad \mathbf{E} = \begin{bmatrix} \epsilon_1 \\ \epsilon_2 \\ \vdots \\ \epsilon_n \end{bmatrix}$$

This notation is used to represent the linear regression model components:

- Y: The $n \times 1$ vector of target variable (class) values.
- ightharpoonup X: The $n \times p$ matrix of feature values.
- ▶ θ : The $p \times 1$ vector of model parameters (coefficients).
- \triangleright E: The $n \times 1$ vector of error terms (residuals).





Linear Equation:

$$Y = X\theta + E$$

Optimization Problem:

$$\min_{\theta} J(\theta) = \frac{1}{2n} \|\mathbf{Y} - \mathbf{X}\theta\|_{2}^{2}$$

Cost Function (MSE):

$$J(\theta) = \frac{1}{2n} \|\mathbf{Y} - \mathbf{X}\theta\|_2^2$$

Gradient Function:

$$\nabla J(\theta) = -\frac{1}{n} \mathbf{X}^T (\mathbf{Y} - \mathbf{X}\theta)$$





Algorithm 1 Gradient Descent for Multivariate Linear Regression

Require: Training data: (X,y) where X is an $n \times p$ matrix and y is an $n \times 1$ vector

Require: Learning rate: α

Require: Number of iterations: *N*

Ensure: Model parameters: θ

1: Initialize parameters θ with small random values or zeros.

2: **for** k = 0 to N - 1 **do**

3: Calculate the gradient of the cost function: $\nabla J(\theta_k) = -\frac{1}{n}X^T(Y - X\theta_k)$.

4: Update the parameters: $\theta_{k+1} = \theta_k - \alpha \cdot \nabla J(\theta_k)$.

5: Calculate and save the cost function: $J(\theta_{k+1}) = \frac{1}{2n}||Y - X\theta_{k+1}||_2^2$.

6: **end for**

7: Output the final parameter values θ .





- **Binary Classification**: Logistic regression is used for binary classification problems where the target variable can take only two possible classes.
- ▶ **Probabilistic Output**: Unlike linear regression, logistic regression outputs probabilities in the range [0, 1], representing the likelihood of the input belonging to a particular class.
- ▶ **Decision Boundary**: Logistic regression uses a decision boundary to separate the two classes based on the estimated probabilities.
- ► **Interpretability**: Coefficients still provide insights into feature importance, indicating how each feature influences the probability of a certain class.





Logistic Regression Equation:

$$p_{1} = \mathbb{P}(y_{1} = 1 | x_{1,1}, x_{1,2}, \dots, x_{1,p}) = \sigma(x_{1,1}\theta_{1} + x_{1,2}\theta_{2} + \dots + x_{1,p}\theta_{p} + \epsilon_{1})$$

$$p_{2} = \mathbb{P}(y_{2} = 1 | x_{2,1}, x_{2,2}, \dots, x_{2,p}) = \sigma(x_{2,1}\theta_{1} + x_{2,2}\theta_{2} + \dots + x_{2,p}\theta_{p} + \epsilon_{2})$$

$$\vdots$$

$$p_{n} = \mathbb{P}(y_{n} = 1 | x_{n,1}, x_{n,2}, \dots, x_{n,p}) = \sigma(x_{n,1}\theta_{1} + x_{n,2}\theta_{2} + \dots + x_{n,p}\theta_{p} + \epsilon_{n})$$

Where:

$$\sigma(z) = \frac{1}{1 + e^{-z}}$$

 p_i is the probability of the *i*-th observation.

 y_i is the class of of the *i*-th observation. Given its features \mathbf{x}_i , the logistic function $\sigma(z)$ maps the linear combination of features and coefficients to the range [0, 1], making it suitable for binary classification.





Log-Odds Ratio: The log-odds ratio, also known as the logit function, is expressed as a linear function of the features and coefficients in logistic regression. It is given by:

$$\sigma^{-1}(p_i) = \log\left(\frac{p_i}{1 - p_i}\right) = x_{i,1}\theta_1 + x_{i,2}\theta_2 + \dots + x_{i,p}\theta_p + \epsilon_i$$

The $\sigma^{-1}(.)$ is called the logit function and it maps the probabilities p_i to a continuous range from negative infinity to positive infinity.





Notation:

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This notation is used to represent the logistic regression model components:

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- ▶ θ : The $p \times 1$ vector of model parameters (coefficients).
- E: The $n \times 1$ vector of error terms (residuals).





Logistic Function:

$$p = \sigma(X\theta + E)$$

Optimization Problem:

$$\min_{\theta} J(\theta)$$

Cost Function (Negative Log-Likelihood):

Gradient Function:

$$\nabla J(\theta) = -\frac{1}{n} X^T (Y - \sigma(X\theta))$$

 $J(\theta) = -\frac{1}{\pi} \left(Y^T \log(\sigma(X\theta)) + (\mathbb{1} - Y)^T \log(\mathbb{1} - \sigma(X\theta)) \right)$





Algorithm 2 Gradient Descent for Logistic Regression

Require: Training data: (X, y) where X is an $n \times p$ matrix and y is an $n \times 1$ vector

Require: Learning rate: α

Require: Number of iterations: *N*

Ensure: Model parameters: θ

- 1: Initialize parameters θ with small random values or zeros.
- 2: **for** k = 0 to N 1 **do**
- 3: Calculate the predicted probabilities using θ_k : $p = \sigma(X\theta_k)$.
- 4: Calculate the gradient of the cost function: $\nabla J(\theta_k) = -\frac{1}{n}X^T(Y \sigma(X\theta_k))$.
- 5: Update the parameters: $\theta_{k+1} = \theta_k \alpha \cdot \nabla J(\theta_k)$.
- 6: Calculate and save the cost function: $J(\theta_{k+1})$.
- 7: end for
- 8: Output the final parameter values θ .





Day 3: Introduction to Clustering

- ▶ What kind of learning is clustering?
- ▶ Why do we need to cluster data?
- k-Means algorithm
- ► HCA algorithm





Key Ideas Behind Clustering

- ► **Group Similar Data**: Clustering groups data points with similar characteristics.
- ▶ **Distance Metrics**: Clustering uses distance metrics to measure data similarity.
- ▶ **Unsupervised Learning**: Clustering does not require labeled data.
- Number of Clusters: The number of clusters is often predetermined or determined using evaluation metrics.
- ▶ **Pattern Discovery**: Clustering discovers underlying patterns and structures in the data.





Applications of Clustering

- ▶ **Marketing**: Customer segmentation for targeted strategies.
- ► **Image Segmentation**: Grouping pixels for object detection.
- ► **Anomaly Detection**: Identifying unusual patterns in data.
- **Recommendation Systems:** Personalized item/user grouping.
- **Bioinformatics**: Categorizing genes, proteins, patients.





k-Means Clustering

▶ **Objective**: Partition data into K clusters, minimizing the within-cluster sum of squares.

Algorithm:

- 1. Randomly initialize K centroids.
- 2. Assign each data point to the nearest centroid.
- 3. Update centroids as the mean of the points in each cluster.
- 4. Repeat steps 2-3 until convergence.





k-Means Clustering

- ▶ **Distance Metric**: Euclidean distance is commonly used to measure point-to-centroid distance.
- ▶ **Optimization**: k-Means aims to minimize the Within-Cluster Sum of Squares (WCSS) as follows:

$$WCSS = \sum_{i=1}^{K} \sum_{x \in C_i} ||x - \text{centroid}_i||^2$$

- ▶ **Initialization**: The algorithm's final result can be sensitive to initial centroid placement.
- ▶ **Elbow Method**: Select K by finding the "elbow" point in the WCSS plot.





k-Means Clustering with scikit-learn

```
from sklearn.cluster import KMeans
# Create a KMeans object with the desired number of clusters
kmeans = KMeans(n clusters=3)
# Fit the model to the data
kmeans.fit(X)
# Get the cluster centers and labels
ccs = kmeans.cluster centers
labels = kmeans.labels
# Plot the data points with color-coded clusters
plt.scatter(X[:, 0], X[:, 1], c=labels, cmap='viridis')
plt.scatter(ccs[:, 0], ccs[:, 1], c='red', marker='X', s=200)
plt.xlabel('Feature 1')
plt.ylabel('Feature 2')
plt.title('k-Means Clustering')
plt.legend()
plt.show()
```

Advantages, Disadvantages, and Applications of k-Means Clustering:

Advantages:

- Fast and scalable for large datasets.
- Simple and easy to implement.
- Works well with well-separated clusters.

Disadvantages:

- Sensitive to initial centroids.
- May converge to local optima.
- Struggles with non-linear or overlapping clusters.

Applications:

- Customer Segmentation.
- Image Compression.
- Anomaly Detection.





Hierarchical Clustering Algorithm (HCA)

- ▶ **Objective**: HCA builds a hierarchy of clusters by recursively merging or splitting them.
- Algorithm:
 - 1. Assign each data point to its own cluster (initially N clusters).
 - 2. Compute the pairwise distance (e.g., Euclidean) between clusters.
 - 3. Merge the two closest clusters into a single cluster.
 - 4. Repeat steps 2-3 until all data points belong to a single cluster.





Hierarchical Clustering Algorithm (HCA)

- ► Linkage Methods: HCA uses different methods to calculate distances between clusters:
 - ▶ Single Linkage: Shortest distance between any two points in the clusters.
 - Complete Linkage: Longest distance between any two points in the clusters.
 - Average Linkage: Average distance between all pairs of points in the clusters.
- **Dendrogram**: HCA visualizes the clustering hierarchy with a dendrogram.





HCA Implementation with scipy

```
from scipy.cluster.hierarchy import linkage, dendrogram
# Compute the linkage matrix using single linkage
linkage matrix = linkage(X, method='single', metric='euclidean')
# Plot the dendrogram
plt.figure(figsize=(10, 6))
dendrogram(linkage matrix)
plt.title('Hierarchical Clustering Dendrogram')
plt.xlabel('Sample Index')
plt.ylabel('Distance')
plt.show()
```





HCA Implementation with scipy

```
from scipy.cluster.hierarchy import fcluster
# Cut the dendrogram to obtain clusters
distance threshold = 0.5  # Set your desired distance threshold here
clusters = fcluster(
    linkage matrix,
    distance threshold,
    criterion='distance'
# Scatter plot the clusters
plt.figure(figsize=(8, 6))
plt.scatter(X[:, 0], X[:, 1], c=clusters, cmap='viridis')
plt.title('Hierarchical Clustering Result')
plt.xlabel('X1')
plt.ylabel('X2')
plt.show()
```

Advantages, Disadvantages, and Applications of HCA:

Advantages:

- Flexibility to choose the number of clusters after dendrogram analysis.
- No need to specify the number of clusters beforehand.
- Captures hierarchical relationships between clusters.

Disadvantages:

- Computationally expensive for large datasets.
- Sensitive to noise and outliers.
- Not suitable for large datasets.

Applications:

- Genetics.
- Image Segmentation.
- Social Sciences.





- K Nearest Neighbors
- Decision trees





k-Nearest Neighbors (k-NNs)

- ▶ **Definition**: k-NN is a simple and popular algorithm for classification and regression.
- ► **Idea**: Classifies a data point by finding the majority class among its k-nearest neighbors.
- ▶ **Distance Metric**: Uses a distance metric (e.g., Euclidean distance) to measure similarity between data points.





k-Nearest Neighbors (k-NNs)

- ► **Choosing K**: The value of K determines the number of neighbors considered for classification.
- ► **Hyperparameter**: K is a hyperparameter tuned using cross-validation or other techniques.
- ▶ **Decision Boundary**: k-NN's boundary can be nonlinear, determined by data point distribution.





k-Nearest Neighbors (k-NN) Implementation with sklearn

```
from sklearn.neighbors import KNeighborsClassifier
# Create k-NN classifier
k = 5
knn classifier = KNeighborsClassifier(n neighbors=k)
# Fit the model using training data
knn classifier.fit(X train, v train)
# Predict the class labels for the test data
y test pred = knn classifier.predict(X test)
# Calculate the accuracy
accuracy = np.mean(y test == y test pred)
print("Accuracy:", accuracy)
```





Advantages, Disadvantages, and Applications of k-NNs:

Advantages:

- ► Simple, intuitive, and easy to implement.
- Effective for a large number of classes and complex decision boundaries.
- Non-parametric nature allows flexibility with data.

Disadvantages:

- Computationally expensive for large datasets.
- Sensitive to irrelevant features, affecting accuracy.
- Description Optimal choice of neighbors (K) impacts performance.

Applications:

- Recommendation systems, collaborative filtering.
- ► Image recognition and object detection.
- ► Anomaly detection and outlier analysis.





Decision Trees (DT)

Definition:

- A decision tree is a supervised machine learning algorithm used for both classification and regression tasks.
- It models decisions as a tree-like structure where each internal node represents a test on a feature, each branch represents an outcome of the test, and each leaf node represents a class label or a numerical value.





TDs Implementation with sklearn

```
from sklearn.tree import DecisionTreeClassifier
# Create Decision Tree classifier
dt classifier = DecisionTreeClassifier()
# Fit the model using training data
dt classifier.fit(X train, v train)
# Predict the class labels for the test data
y test pred = dt classifier.predict(X test)
# Calculate the accuracy
accuracy = np.mean(y test == y test pred)
print("Accuracy:", accuracy)
```





Advantages, Disadvantages, and Applications of DTs:

Advantages:

- Easy to interpret and handle both numerical and categorical data.
- Non-parametric, no assumptions about data distribution needed.
- Performs automatic feature selection.

Disadvantages:

- Prone to overfitting, especially with deep trees and noisy data.
- ▶ Instability: Small data changes can lead to completely different trees.
- ► Greedy nature: Decisions are locally optimal but not always globally.

Applications:

- Classification and regression in medicine, finance, and marketing.
- Predicting house or stock prices.
- Feature engineering and ensemble methods like Random Forests.





- Support Vector Machines.
- Random Forests.





Support Vector Machines (SVM)

Introduction:

- SVM is a powerful supervised learning algorithm used for classification and regression tasks.
- It finds the optimal hyperplane that best separates the data points into different classes.
- SVM is effective for both linearly separable and non-linearly separable data.





How do SVMs work?

Optimization Problem:

Maximize
$$\frac{2}{\|\mathbf{w}\|}$$

subject to $y_i(\mathbf{w} \cdot \mathbf{x}_i + b) \ge 1 \quad \forall i$

Meaning:

- ► The optimization problem seeks to find the maximum margin that separates the two classes represented by +1 and -1.
- The vector **w** is perpendicular to the decision boundary, and its magnitude represents the margin width.
- The equation $\mathbf{w} \cdot \mathbf{x} + b = 0$ defines the decision boundary that separates the two classes.





How do SVMs work?

Soft Margin and Kernel Trick:

- ▶ **Soft Margin**: Allows for misclassification to achieve a more flexible decision boundary.
- ► **Kernel Trick**: Transforms data into a higher-dimensional space to handle non-linear decision boundaries.

Optimization Problem with Soft Margin:

$$\text{Minimize } \frac{1}{2} ||\mathbf{w}||^2 + C \sum_{i=1}^n \xi_i$$

subject to $y_i(\mathbf{w} \cdot \phi(\mathbf{x}_i) + b) \ge 1 - \xi_i$ and $\xi_i \ge 0 \quad \forall i$

Meaning:

- ightharpoonup The parameter C controls margin-maximization vs. classification errors.
- The function $\phi(\mathbf{x})$ maps the data to a higher-dimensional space, allowing for non-linear decision boundaries.





SVM Implementation with sklearn

```
from sklearn.svm import SVC
# Create SVM classifier
svm classifier = SVC(kernel='linear', C=1.0)
# Fit the model using training data
svm classifier.fit(X train, y train)
# Predict the class labels for the test data
y test pred = svm classifier.predict(X test)
# Calculate the accuracy
accuracy = mp.mean(y test == y test pred)
print("Accuracy:", accuracy)
```





Advantages, Disadvantages, and Applications of SVMs:

Advantages:

- Effective in high-dimensional spaces and with non-linear boundaries.
- Robust against overfitting, especially with the soft margin parameter.
- Versatile with various kernel functions to handle non-linear data.

Disadvantages:

- Computationally intensive for large datasets and complex models.
- Sensitive to the choice of hyperparameters, like the kernel and regularization parameter.
- ► Hard to interpret the decision boundaries for highly non-linear data.

Applications:

- Object detection in computer vision.
- Predictive maintenance for industrial equipment.
- Fraud detection in financial transactions.





Random Forests (RF)

- Ensemble method for classification and regression.
- Builds multiple decision trees on random subsets of data and features.
- Combines tree predictions using majority vote or averaging for improved accuracy and generalization.





How do RFs Work?

- ▶ Bootstrap Aggregating (Bagging): Train decision trees on random data subsets with replacement.
- ▶ **Random Feature Selection**: Use random subsets of features for each tree to introduce diversity.
- **Voting (Classification) or Averaging (Regression):** Combine tree predictions using majority vote for classification tasks or averaging for regression tasks.





RF Implementation with sklearn

```
from sklearn.ensemble import RandomForestClassifier
# Create Random Forest classifier
rf classifier = RandomForestClassifier(
    n estimators=100,
    criterion='gini',
    max depth=3
# Fit the model using training data
rf classifier.fit(X train, y train)
# Predict the class labels for the test data
y test pred = rf classifier.predict(X test)
# Calculate the accuracy
accuracy = np.mean(y test == y test pred)
print("Accuracy:", accuracy)
```





Advantages, Disadvantages, and Applications of RFs:

Advantages:

- ► High accuracy from an ensemble of diverse trees.
- Robust to overfitting and noisy data.
- Handles numerical and categorical data.

Disadvantages:

- Computationally more expensive than individual decision trees.
- Difficult to interpret the combined decision-making process.
- May not perform well on imbalanced datasets.

Applications: Feature ranking in various domains, image classification, predictive maintenance, and fraud detection.



