

PyPHS: An open source Python library dedicated to the generation of passive guaranteed simulation code for multiphysical (audio) systems

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Introduction

Objective : Numerical simulation of multiphysical systems

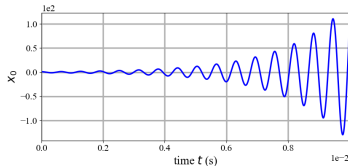
- electronics, mechanics, magnetics, thermics.
- nonlinearities, non ideal behaviors.
- high complexity.

Standard approaches

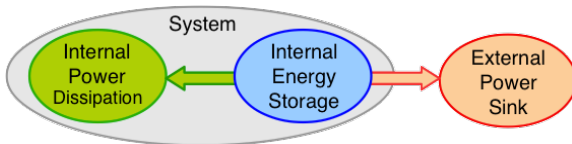
1. Build a set of elementary physical models.
2. Build a system as the connection of these models.
3. Apply *ad-hoc* discretization methods.

Difficulties

- D1 The stability of a single model simulation is not guaranteed.
- D2 This is even worst for the interconnected system.



But physical systems are passive systems



Power-balance $\frac{dE}{dt} + P_D + P_S = 0$

with

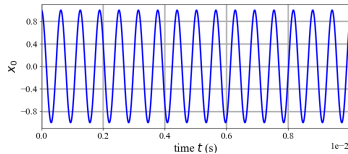
- Energy E (J),
- Dissipated power P_D (W),
- Sink Power P_S (W).

Our approach

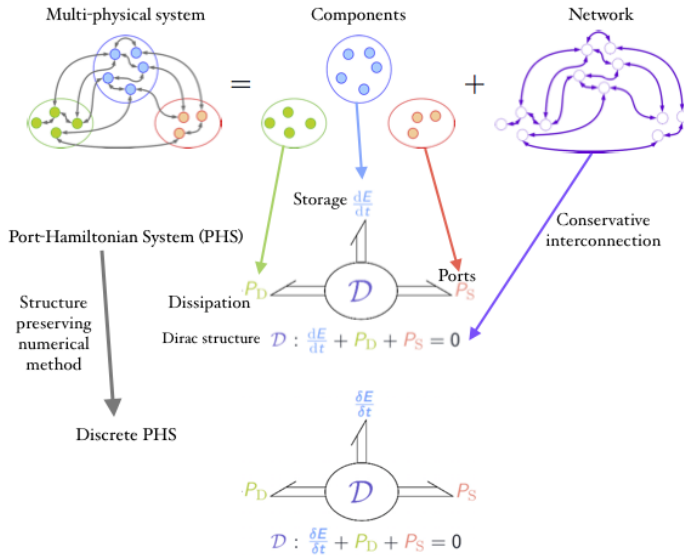
1. Structure physical models according to energy flows
2. Build a system as the structure preserving connection of these models
3. Apply a structure preserving discretization method

Result

- D1 The stability of a single model simulation is guaranteed.
- D2 The interconnected system inherits from this property.



Encoding of passivity in PyPHS



PyPHS : everything is formal

Networks are formal graph structures

- Use of NETWORKX¹ Python package.
- Creation and manipulation of graphs structures.

Model equations in symbolic form

- Use of SYMPY² Python package.
- A posteriori manipulation of system's equations.
- Automated generation of L^AT_EX documentation.

Numerical method is derived formally

- Also use SYMPY Python package.
- Symbolic optimization of the update equations.
- Easy analysis of the signal flow → Code generation.

1. see <https://networkx.github.io/>

2. see <http://www.sympy.org/en/index.html>

Main tools

- Port-Hamiltonian Systems (PHS) formalism³
- Graph theory⁴

2012→2016

- ANR project HaMecMoPSys⁵.
- PhD thesis of Antoine Falaize⁶ in the team S3AM⁷ at IRCAM - UMR STMS 9912 founded by EDITE.

2016→ . . .

- Implementation of the scientific results obtained between 2012 and 2016.
- Further scientific developments.

3. MASCHKE, VAN DER SCHAFT et BREEDVELD, "An intrinsic Hamiltonian formulation of network dynamics : Non-standard Poisson structures and gyrators", 1992.

4. DESOER et KUH, Basic circuit theory, 2009.

5. see <https://hamecmopsys.ens2m.fr/>

6. FALAIZE, "Modélisation, simulation, génération de code et correction de systèmes multi-physiques audios : Approche par réseau de composants et formulation Hamiltonienne à Ports", 2016.

7. see <http://s3am.ircam.fr/?lang=en>

Table of contents

1. Network

PyPHS inputs : Graph and Netlist.

2. Components

PyPHS dictionary elements : Graph objects.

3. Port-Hamiltonian Systems

PyPHS Core object : Passive-guaranteed structure.

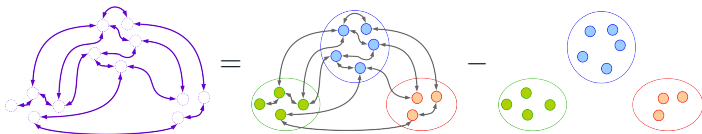
4. Numerical Method

PyPHS Method object : Structure preserving numerical scheme.

5. Code generation

PyPHS outputs : PYTHON, C++, JUCE and FAUST.

Network



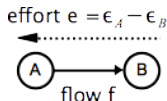
System representation paradigm : Power graphs

Directed graphs with self loops

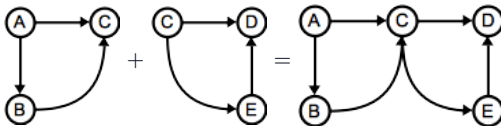
- Set of nodes $\mathbf{N} = \{N_1, \dots, N_n\}$.
- Set of edges $\mathbf{B} = \{B_1, \dots, B_n\}$ with $B_i = (n, m) \in \mathbf{N}^2$.
- Direction : $B_i \equiv n \rightarrow m$

Receiver convention

- Each edge \equiv two power variables : Flow and Effort
- Flow f : defined through the edges.
- Effort e : defined across the edges as the difference of two quantities.
- Power received by the edge : $P = f e$ (W).



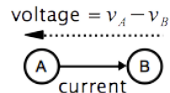
Connection \equiv Nodes identification



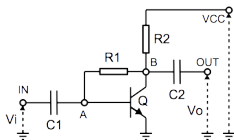
Electrical graphs

Physical quantities

Flow = Current (A), Effort = Voltage (V), ϵ = Potential (V)

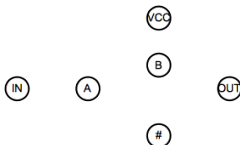


Example system



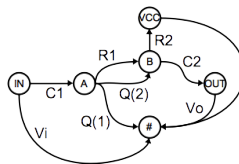
- 2 Capacitors $C1$ and $C2$,
- 2 Resistors $R1$ and $R2$,
- 1 BJ transistor Q ,
- 3 Ports V_i , V_o and V_c .

Nodes



Graph nodes = Circuit nodes
Ground = Reference node $\#$

Graph

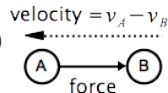


Graph edges = Circuit components
Note $Q \equiv 2$ edges

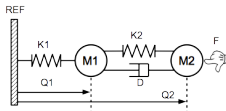
Mechanical graphs

Physical quantities

Flow = Force (N), Effort = Velocity (m/s), ϵ = point velocity (m/s)



Example system



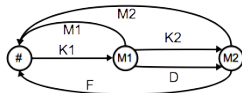
- 2 Masses M1 and M2,
- 2 Springs K1 and K2,
- 1 Damper,
- 1 Port F.

Nodes



Graph nodes = unique velocities
Reference velocity = node #

Graph

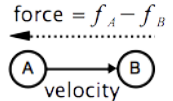


Graph edges = components

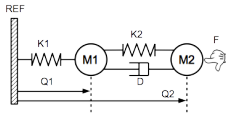
Mechanical graphs (dual)

Physical quantities

Flow = Velocity (m/s), Effort = force (N), ϵ = some force (N)

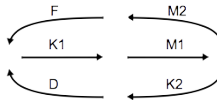


Example system



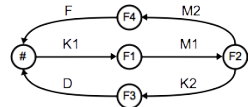
2 Masses M1 and M2,
2 Springs K1 and K2,
1 Damper,
1 Port F.

Edges



Serial edges = same velocity

Graph

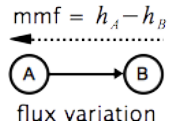


Add nodes to close the graph

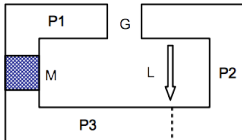
Magnetical graphs

Physical quantities

Flow = flux variation (V), Effort = magnetomotive force (A), ϵ = some mmf (A)

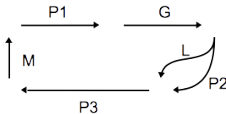


Example system



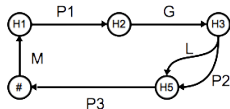
- 3 metal pieces P1, P2, P3,
- 1 Air gap G,
- 1 Flux leakage L,
- 1 Port M (magnet).

Edges



Serial = same magnetic flux

Graph

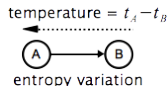


Add nodes to close the graph

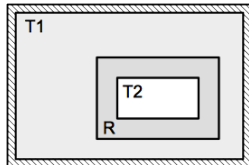
Thermal graphs

Physical quantities

Flow = entropy variation (W/K), Effort = temperature (K), ϵ = temperature (K)



Example system



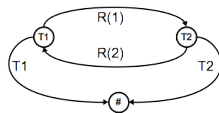
2 Heat capacities T1 and T2,
1 Heat transfer R,

Nodes



Graph nodes = temperatures
Reference temperature = node #

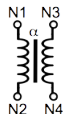
Graph



Graph edges = components
Note R = 2 edges (irreversibility)

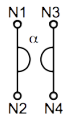
Multiphysical graphs : connectors

Transformer



$$\begin{aligned}e_{3 \rightarrow 4} &= \frac{1}{\alpha} e_{1 \rightarrow 2}, \\f_{3 \rightarrow 4} &= -\alpha f_{1 \rightarrow 2}, \\[\alpha] &= \frac{[f_{3 \rightarrow 4}]}{[e_{1 \rightarrow 2}]}.\end{aligned}$$

Gyrator



$$\begin{aligned}e_{3 \rightarrow 4} &= \alpha f_{1 \rightarrow 2}, \\f_{3 \rightarrow 4} &= -\frac{1}{\alpha} e_{1 \rightarrow 2}, \\[\alpha] &= \frac{[e_{3 \rightarrow 4}]}{[f_{1 \rightarrow 2}]}.\end{aligned}$$

Conserving connection

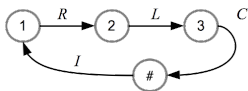
In each case : $P_{3 \rightarrow 4} = -P_{1 \rightarrow 2}$

Kirchhoff laws on graphs

Incidence Matrix

$$[\Gamma]_{n,b} = \begin{cases} 1 & \text{if edge } b \text{ is ingoing node } n, \\ -1 & \text{if edge } b \text{ is outgoing node } n. \end{cases}$$

Example : RLC



$$\Gamma = \begin{array}{c} \begin{array}{cccc} B_R & B_L & B_C & B_I \end{array} \\ \begin{pmatrix} 0 & 0 & +1 & -1 \\ -1 & 0 & 0 & 0 \\ +1 & -1 & 0 & 0 \\ 0 & +1 & -1 & +1 \end{pmatrix} \begin{array}{l} \# \\ N_1 \\ N_2 \\ N_3 \end{array} \end{array}$$

Reduced incidence Matrix

Arbitrary reference node #

$$\Gamma = \begin{array}{c} \begin{array}{ccc} B_1 & \dots & B_{n_B} \end{array} \\ \begin{pmatrix} \gamma_0 \\ \gamma \end{pmatrix} \begin{array}{l} \# \\ N_1 \\ \vdots \\ N_{n_N} \end{array} \end{array},$$

Generalized Kirchhoff's laws

- Efforts $\mathbf{e} \in \mathbb{R}^{n_B}$, flows $\mathbf{f} \in \mathbb{R}^{n_B}$.
- Node quantities $\mathbf{p} \in \mathbb{R}^{n_N}$.
- $\gamma^T \mathbf{p} = \mathbf{e}$, (KVL).
- $\gamma \mathbf{f} = \mathbf{0}$, (KCL).

Dirac structure \mathcal{D} = Kirchhoff laws on graphs

Edges splitting

Depends on the components

Flow controlled $f \rightarrow \text{edge} \rightarrow e$.

Effort controlled $e \rightarrow \text{edge} \rightarrow f$.

Outputs $a \in \mathbb{R}^{n_B}$.

Inputs $b \in \mathbb{R}^{n_B}$.

RLC example

B_L is e -controlled, B_R, B_C, B_I are f -controlled.

$$\left(\begin{array}{c|c} \gamma_0 & \gamma_f \end{array} \right) = \left(\begin{array}{c|ccc} B_L & B_R & B_C & B_I \\ \hline 0 & 0 & +1 & -1 \\ 0 & -1 & 0 & 0 \\ -1 & +1 & 0 & 0 \\ +1 & 0 & -1 & +1 \end{array} \right) \begin{array}{l} N_0 \\ N_1 \\ N_2 \\ N_3 \end{array}.$$

Realizability criterion

If γ_f is invertible, then $\exists! J$ s.t.

$$b = J \cdot a.$$

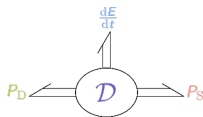
$$\underbrace{\begin{pmatrix} e_b \\ f_b \end{pmatrix}}_b = \underbrace{\begin{pmatrix} 0 & \gamma_{ef}^T \\ -\gamma_{ef} & 0 \end{pmatrix}}_J \underbrace{\begin{pmatrix} f_a \\ e_a \end{pmatrix}}_a.$$

J is skew-symmetric $\Rightarrow a^T \cdot b = a^T \cdot J \cdot a = 0$.

This is the Tellegen's theorem :

$$\sum_n^{n_B} e_n f_n = \sum_n^{n_B} P_n = 0.$$

1. $e_b = \gamma_e^T \cdot p$ and $e_a = \gamma_f^T \cdot p$,
2. $\gamma_e f_a = -\gamma_f \cdot f_b$,
3. $\gamma_{ef} = \gamma_f^{-1} \cdot \gamma_e$,



Automated construction of the Dirac structure

Algorithme⁸

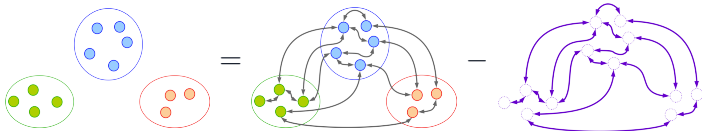
Data A **netlist** and a **dictionary** of components.

Résult

- If realizable :
 1. partition $B = [B_e, B_f]$,
 2. structure $b = J \cdot a$.
- Else : Realizability fault detection \rightarrow the user correct the netlist.

8. FALAIZE et HÉLIE, "Passive guaranteed simulation of analog audio circuits : A port-Hamiltonian approach", 2016.

Components



Storage components (definitions)

Constitutive relation for component s

Storage function (Hamiltonian) H_s of the state x_s .

Stored energy $E_s(t) = H_s(x_s(t)) \geq 0$.

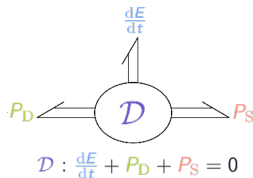
Received power $\frac{dE_s}{dt} = H'_s(x_s) \frac{dx_s}{dt}$

Power variables for component s

Received power $\frac{dE_s}{dt} = e_s f_s$.

e -controlled $e_s = \frac{dx_s}{dt} \implies f_s = H'_s(x_s)$.

f -controlled $f_s = \frac{dx_s}{dt} \implies e_s = H'_s(x_s)$.



Total energy stored in n_E storage edges

- $\mathbf{x} = (x_1, \dots, x_{n_E})$.
- $E = H(\mathbf{x}) = \sum_{s=1}^{n_E} H_s(x_s) \geq 0$.
- $\frac{dE}{dt} = \nabla H^T \frac{d\mathbf{x}}{dt} = \sum_{s=1}^{n_E} \frac{dH_s}{dx_s} \frac{dx_s}{dt}$.

Storage components (examples)

Mass (flow=velocity, effort=force)

State momentum $x_m = m v_m$.

Hamiltonian kinetic energy $H_m(x_m) = \frac{x_m^2}{2m}$.

Flow mass velocity $f_m = H'_m(x_m) = \frac{x_m}{m}$.

Effort inertial force $e_m = \frac{dx_m}{dt} = m \frac{dv_m}{dt}$.

Capacitor

State charge q_C .

Hamiltonian electrostatic energy $H_C(x_C) = \frac{x_C^2}{2C}$.

Flow current $f_C = \frac{dx_C}{dt} = \frac{dq_C}{dt}$.

Effort voltage $e_C = H'_C(x_C) = \frac{x_C}{C}$.

Dissipative components (definitions)

Constitutive relation for component d

Dissipation function z_d of the variable w_d .

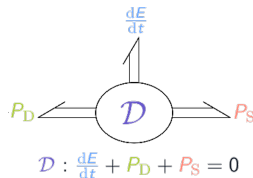
Received (dissipated) power $P_{Dd}(t) = z_d(w_d(t)) \geq 0$.

Power variables for component d

Received power $P_{Dd}(t) = e_d f_d \geq 0$

e -controlled $e_d = w_d \implies f_d = z_d(w_d)$.

f -controlled $f_d = w_d \implies e_d = z_d(w_d)$.



Total power dissipated in n_D dissipative edges

- $\mathbf{w} = (w_1, \dots, w_{n_D})$.
- $\mathbf{z}(\mathbf{w}) = (z_1(w_1), \dots, z_{n_D}(w_{n_D}))$.
- $P_D = \mathbf{z}(\mathbf{w})^T \cdot \mathbf{w} = \sum_{d=1}^{n_D} z_d(w_d) w_d \geq 0$.

Dissipative components (examples)

Dashpot (flow=force, effort=velocity)

Variable elongation velocity $w_D = v_D$.

Function resistance force $z_D(w_D) = D w_D$, with $D > 0$.

Flow force $f_D = z_D(w_D) = D v_D$.

Effort velocity $e_D = w_D = v_D$.

Dissipated Power $P_D = f_D e_D = R v_D^2$

Resistor

Variable current $w_R = i_R$.

Function resistance voltage $z_R(w_R) = R i_R$, with $R > 0$.

Flow current $f_R = w_R = i_R$.

Effort voltage $e_R = z_R(w_R) = R i_R$.

Dissipated Power $P_D = f_R e_R = R i_R^2$

Ports (definitions)

Input and output on port p

Actuated quantity u (input) and Observed quantity y (output).

Received Power $P_{Sp}(t) = u_p(t) y_p(t)$.

The power P_{Sp} is the power that goes out of the system on port p .

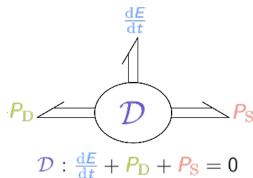
Ports are power sink.

Power variables for port p

Received power $P_{Sp}(t) = \epsilon_p f_p$

ϵ -controlled $\epsilon_p = y_p \implies f_p = u_p$ (flow source).

f -controlled $f_p = y_p \implies \epsilon_p = u_p$ (effort source).



Total power on n_S port edges

- $\mathbf{u} = (u_1, \dots, u_{n_S})$.
- $\mathbf{y} = (y_1, \dots, y_{n_S})$.
- $P_S = \mathbf{u}^T \cdot \mathbf{y} = \sum_{p=1}^{n_S} u_p y_p$.

Ports (examples)

Voltage source

Input voltage $u_U = v_U$.

Output current $y_U = i_U$.

Flow current $f_U = y_U$.

Effort voltage $e_U = u_U$.

Received Power $P_S = f_U e_U = v_U i_U$.

Imposed force (flow=force, effort=velocity)

Input force $u_U = f_U$.

Output velocity $y_U = v_U$.

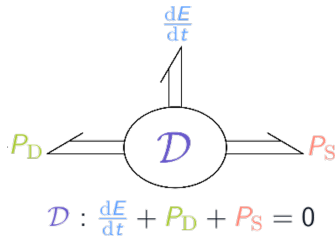
Flow force $f_U = u_U$.

Effort velocity $e_U = y_U$.

Received Power $P_S = f_U e_U = f_U v_U$.

- **Mechanics (1D)** : masses, springs lin./nonlin. (cubic, saturating, etc.), lin./nonlin. damping, visco-elastic (fractional derivatives).
- **Electronics** : batteries, coils and lin./nonlin. capacitors, resistors, transistors, diodes, triodes.
- **Magnetics** : Magnets, lin./nonlin capacitors, resisto-inductor (fractional integrators).
- **Thermics** : heat sources, capacitors.
- **Connections** : electromagnetic couplings, electromechanic coupling, irreversible transfers, gyrators, transformers.

3. Port-Hamiltonian Systems



Putting all together

Components

Storage $\mathbf{b}_x = \frac{dx}{dt}$, $\mathbf{a}_x = \nabla H(\mathbf{x})$

Dissipation $\mathbf{b}_w = \mathbf{w}$, $\mathbf{a}_w = \mathbf{z}(\mathbf{w})$

Ports $\mathbf{b}_y = \mathbf{y}$, $\mathbf{b}_y = \mathbf{u}$

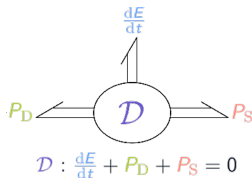
This encodes the power balance

$$\begin{aligned} 0 &= \mathbf{a}^T \cdot \mathbf{b} \\ &= \underbrace{\nabla H(\mathbf{x})^T \cdot \frac{dx}{dt}}_{\frac{dE}{dt}} + \underbrace{\mathbf{z}(\mathbf{w}) \cdot \mathbf{w}}_{P_D} + \underbrace{\mathbf{u}^T \cdot \mathbf{y}}_{P_S} \end{aligned}$$

Network (Dirac structure)

$$\mathbf{b} = \begin{pmatrix} \mathbf{b}_x \\ \mathbf{b}_w \\ \mathbf{b}_y \end{pmatrix} \text{ and } \mathbf{a} = \begin{pmatrix} \mathbf{a}_x \\ \mathbf{a}_w \\ \mathbf{a}_y \end{pmatrix}$$

with $\mathbf{b} = \mathbf{J} \cdot \mathbf{a}$ and $\mathbf{J}^T = -\mathbf{J}$.



Port-Hamiltonian structure

$$\underbrace{\begin{matrix} \text{Storage} \\ \text{Dissipation} \\ \text{Ports} \end{matrix} \begin{pmatrix} \frac{dx}{dt} \\ \mathbf{w} \\ \mathbf{y} \end{pmatrix}}_{\mathbf{b}} = \underbrace{\begin{pmatrix} +\mathbf{J}_{xx} & +\mathbf{J}_{xw} & +\mathbf{J}_{xy} \\ -\mathbf{J}_{xw}^T & +\mathbf{J}_{ww} & +\mathbf{J}_{wy} \\ -\mathbf{J}_{xy}^T & -\mathbf{J}_{wy}^T & +\mathbf{J}_{yy} \end{pmatrix}}_{\mathbf{J}} \cdot \underbrace{\begin{pmatrix} \nabla H(\mathbf{x}) \\ \mathbf{z}(\mathbf{w}) \\ \mathbf{u} \end{pmatrix}}_{\mathbf{a}}$$

Reduction of the linear dissipative structure⁹

Splitting of \mathbf{z}

\mathbf{Z}_1 a diagonal matrix and \mathbf{z}_{nl} a collection of nonlinear functions

$$\mathbf{w} = \begin{pmatrix} \mathbf{w}_1 \\ \mathbf{w}_{nl} \end{pmatrix}, \quad \mathbf{z}(\mathbf{w}) = \begin{pmatrix} \mathbf{Z}_1 \cdot \mathbf{w}_1 \\ \mathbf{z}_{nl}(\mathbf{w}_{nl}) \end{pmatrix},$$

New Port-Hamiltonian structure

$$\underbrace{\begin{pmatrix} \frac{dx}{dt} \\ \mathbf{w}_{nl} \\ \mathbf{y} \end{pmatrix}}_{\hat{\mathbf{b}}} = \underbrace{(\hat{\mathbf{J}} - \mathbf{R})}_{\mathbf{M}} \cdot \underbrace{\begin{pmatrix} \frac{\nabla H(\mathbf{x})}{\mathbf{z}_{nl}(\mathbf{w}_{nl})} \\ \mathbf{u} \end{pmatrix}}_{\hat{\mathbf{a}}}$$

Interpretation

- $\hat{\mathbf{J}} \rightarrow$ reduced conservative interconnection,
- $\mathbf{R} \succeq 0 \rightarrow$ resistive interconnection (includes the coefficients from \mathbf{Z}_1).

9. FALAIZE et HÉLIE, "Passive guaranteed simulation of analog audio circuits : A port-Hamiltonian approach", 2016.

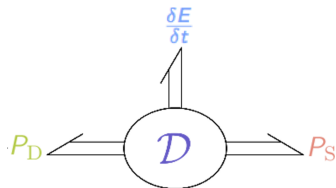
PyPHS Port-Hamiltonian structure

$$\underbrace{\begin{pmatrix} \frac{dx}{dt} \\ \mathbf{w} \\ \mathbf{y} \end{pmatrix}}_{\mathbf{b}} = \underbrace{\begin{pmatrix} M_{xx} & M_{xw} & M_{xy} \\ M_{wx} & M_{ww} & M_{wy} \\ M_{yx} & M_{yw} & M_{yy} \end{pmatrix}}_{\mathbf{M}} \cdot \underbrace{\begin{pmatrix} \nabla H(\mathbf{x}) \\ \mathbf{z}(\mathbf{w}) \\ \mathbf{u} \end{pmatrix}}_{\mathbf{a}}$$

with

$$\mathbf{M} = \underbrace{\begin{pmatrix} +\mathbf{J}_{xx} & +\mathbf{J}_{xw} & +\mathbf{J}_{xy} \\ -\mathbf{J}_{xw}^T & +\mathbf{J}_{ww} & +\mathbf{J}_{wy} \\ -\mathbf{J}_{xy}^T & -\mathbf{J}_{wy}^T & +\mathbf{J}_{yy} \end{pmatrix}}_{\mathbf{J}} - \underbrace{\begin{pmatrix} \mathbf{R}_{xx} & \mathbf{R}_{xw} & \mathbf{R}_{xy} \\ \mathbf{R}_{xw}^T & \mathbf{R}_{ww} & \mathbf{R}_{wy} \\ \mathbf{R}_{xy}^T & \mathbf{R}_{wy}^T & \mathbf{R}_{yy} \end{pmatrix}}_{\mathbf{R}}$$

4. Numerical method



$$\mathcal{D} : \frac{\delta E}{\delta t} + P_D + P_S = 0$$

Structure preserving numerical method 1

Objective

Discrete time power balance : $\frac{\delta E}{\delta T}[k] + P_D[k] + P_S[k] = 0$.

Choice

- $\frac{\delta E[k]}{\delta T} = \frac{E[k+1]-E[k]}{\delta T} = \frac{H(x[k+1])-H(x[k])}{\delta T}$
- Mono-variate case :

$$\frac{E[k+1] - E[k]}{\delta T} = \sum_n \frac{H_n(x_n[k+1]) - H_n(x_n[k])}{x_n[k+1] - x_n[k]} \cdot \frac{x_n[k+1] - x_n[k]}{\delta T}$$

Solution :

$$\begin{aligned} \frac{dx}{dt} &\longrightarrow \frac{\delta x[k]}{\delta T} = \frac{x[k+1]-x[k]}{\delta T} \\ \nabla H(x) &\longrightarrow \nabla^d H(x[k], \delta x[k]) \triangleq \text{discrete gradient}^{10} \end{aligned}$$

with

$$\left[\nabla^d H(x, \delta x) \right]_n = \frac{H_n([x + \delta x]_n) - H_n([x]_n)}{[\delta x]_n} \xrightarrow{[\delta x]_n \rightarrow 0} \frac{dH_n}{dx_n}(x_n).$$

10. ITOH et ABE, "Hamiltonian-conserving discrete canonical equations based on variational difference quotients",

Structure preserving numerical method 2

Solution

$$\begin{aligned}\frac{dx}{dt} &\longrightarrow \frac{\delta x[k]}{\delta T} = \frac{x[k+1]-x[k]}{\delta T} \\ \nabla H(\mathbf{x}) &\longrightarrow \nabla^d H(\mathbf{x}[k], \delta \mathbf{x}[k])\end{aligned}$$

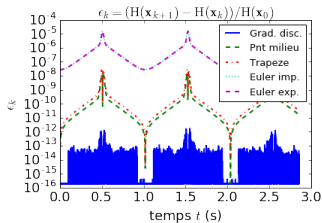
Discret PHS

$$\begin{pmatrix} \frac{\delta x[k]}{\delta T} \\ \mathbf{w}[k] \\ \mathbf{y}[k] \end{pmatrix} = \mathbf{M} \cdot \begin{pmatrix} \nabla^d H(\mathbf{x}[k], \delta \mathbf{x}[k]) \\ \mathbf{z}(\mathbf{w}[k]) \\ \mathbf{u}[k] \end{pmatrix}.$$

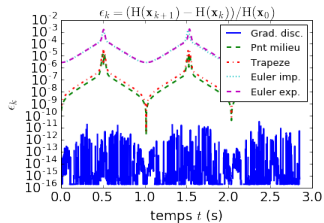
PHS structure is preserved in discrete time \Rightarrow numerical passivity.

Relative error on the power balance (PyPHS in blue)

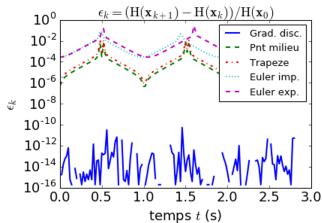
$$f_e = 5000\text{Hz}$$



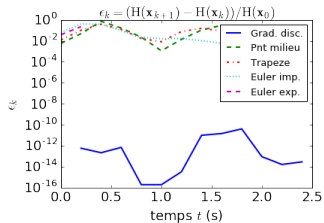
$$f_e = 500\text{Hz}$$



$$f_e = 50\text{Hz}$$

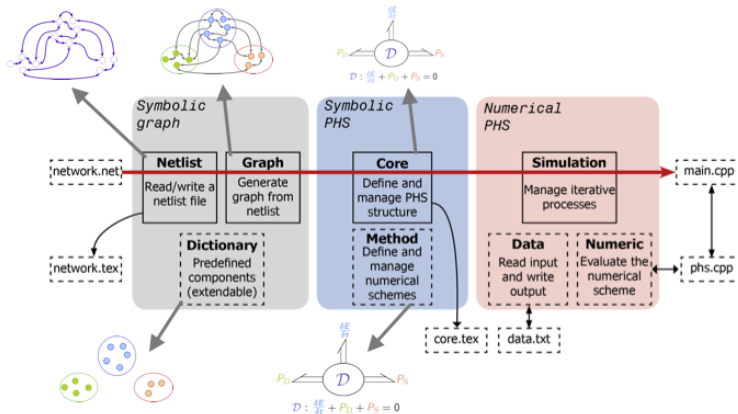


$$f_e = 5\text{Hz}$$



5. Code generation

PyPHS : an overview



Formal Method object to numerical Simulation object

1. Parameters are substituted in the discrete PHS.
2. Each symbolic expression is simplified and transformed into a Python function.
3. Updates of internal variables is defined by a message passing system.

Perform simulation

- Inputs are :
 1. A sequence of input values,
 2. A sequence of control parameters values.
- Apply each update sequentially.
- Results are stored on disk to avoid memory overload.

Formal Method object to C++ code

1. Parameters are associated to pointers → can be changed after generation.
2. Each symbolic expression is simplified and transformed into a C++ function.
3. Same message passing system.

Perform simulation

- Inputs are :
 1. the sample rate,
 2. a sequence of input values,
 3. a sequence of control parameters values.
- Apply each update sequentially.
- Results are stored on disk → call back into Python for post processing.

Only for Juce audio FX

1. Call the generated C++ object into Juce Template.
2. Generation of a set of snippets → copy/past into Juce template.
3. The control parameters are automatically associate with sliders → real-time control.
4. Still experimental.

Yield AU/VST real-time audio plugins

- Can be used in most Digital Audio Workstations.

11. <https://juce.com/>

Only for FAUST audio FX

- Dedicated Method object : Symbolic pre-inversion of every matrices.
- Fixed number of nonlinear solvers iteration → duplicate of a single iteration.
- A complete iteration is built and encompassed in a dedicated feedback system.
- Control parameters are associated with sliders.
- Still experimental.

Yield VST real-time audio plugins

- Automated optimization of the signal flow.
- Can be used in most Digital Audio Workstations.
- Several compilation targets.

12. <http://faust.grame.fr/>

Last word

- Open source Library on a GITHUB repository¹³.
- Licence CECILL (CEA-CNRS-INRIA Logiciels libres).
- PYTHON 2.7 & 3.5 supported, Mac OSX, Windows 10 and Linux.
- Multiphysical components dictionary.
- Automated graph analysis.
- Automated derivation of the PHS structure and L^AT_EX code generation.
- Passive guaranteed simulations.
- Automated generation of C++, JUCE and FAUST code.

13. <https://pyphs.github.io/pyphs/>

Scientific results to be implemented

- Anti-aliasing observer (PhD Remy Müller).
- PHS in scattering variables (\rightsquigarrow Wave Digital PHS).
- Piecewise Linear constitutive laws (\rightsquigarrow cope with realizability faults).
- Improve Nonlinear solver (\neq Newton-Raphson).
- Automated derivation of command laws (feedforward + feedback).
- ...

Accelerate development

CALL FOR DEVELOPERS

Improve robustness

CALL FOR USERS

Thank you for your attention

Contact : `antoine.falaize@gmail.com`