

# DLC

The PyPHS\* development team<sup>1</sup>

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## 1 System netlist

line	label	dictionary.component	nodes	parameters
$\ell_1$	in	electronics.source	('n#', 'n1')	{ type voltage
$\ell_2$	D	electronics.diode	('n1', 'n2')	{ v0 ('v0', 0.026)
$\ell_3$	L	electronics.inductor	('n2', 'n3')	{ mu ('mu', 1.7)
$\ell_4$	C	electronics.capacitor	('n3', 'n#')	{ Is ('Is', 2e-09)
				{ R ('Rd', 0.5)
				{ L ('L', 0.05)
				{ C ('C', 2e-06)

## 2 System dimensions

$\dim(\mathbf{x}) = n_{\mathbf{x}} = 2;$   
 $\dim(\mathbf{w}) = n_{\mathbf{w}} = 3;$   
 $\dim(\mathbf{y}) = n_{\mathbf{y}} = 1;$   
 $\dim(\mathbf{p}) = n_{\mathbf{p}} = 0;$

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\*<https://github.com/afalaize/pyphs>

<sup>†</sup><http://s3.ircam.fr>

### 3 System variables

State variable  $\mathbf{x} = \begin{pmatrix} x_L \\ x_C \end{pmatrix};$

Dissipation variable  $\mathbf{w} = \begin{pmatrix} w_D \\ w_{D_R} \\ w_{D_{gmin}} \end{pmatrix};$

Input  $\mathbf{u} = \begin{pmatrix} u_{in} \end{pmatrix};$

Output  $\mathbf{y} = \begin{pmatrix} y_{in} \end{pmatrix};$

### 4 Constitutive relations

Hamiltonian  $\mathbb{H}(\mathbf{x}) = \frac{0.5}{L} \cdot x_L^2 + \frac{0.5}{C} \cdot x_C^2;$

Hamiltonian gradient  $\nabla \mathbb{H}(\mathbf{x}) = \begin{pmatrix} \frac{1.0}{L} \cdot x_L \\ \frac{1.0}{C} \cdot x_C \end{pmatrix};$

Dissipation function  $\mathbf{z}(\mathbf{w}) = \begin{pmatrix} \mu \cdot v_0 \cdot \log\left(\frac{1}{I_s} \cdot (I_s + w_D)\right) \\ Rd \cdot w_{D_R} \\ \frac{w_{D_{gmin}}}{gmin} \end{pmatrix};$

Jacobian of dissipation function  $\mathcal{J}_{\mathbf{z}}(\mathbf{w}) = \begin{pmatrix} \frac{\mu \cdot v_0}{I_s + w_D} & 0 & 0 \\ 0 & Rd & 0 \\ 0 & 0 & \frac{1}{gmin} \end{pmatrix};$

### 5 System parameters

#### 5.1 Constant

parameter	value (SI)
C :	2e-06
v0 :	0.026
L :	0.05
mu :	1.7
gmin :	1e-12
Is :	2e-09
Rd :	0.5

## 6 System structure

$$\mathbf{M} = \begin{pmatrix} 0 & -1.0 & 0 & -1.0 & -1.0 & -1.0 \\ 1.0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1.0 & 0 \\ 1.0 & 0 & 0 & 0 & 0 & 0 \\ 1.0 & 0 & -1.0 & 0 & 0 & 0 \\ 1.0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix};$$

$$\mathbf{M}_{\mathbf{xx}} = \begin{pmatrix} 0 & -1.0 \\ 1.0 & 0 \end{pmatrix};$$

$$\mathbf{M}_{\mathbf{xw}} = \begin{pmatrix} 0 & -1.0 & -1.0 \\ 0 & 0 & 0 \end{pmatrix};$$

$$\mathbf{M}_{\mathbf{xy}} = \begin{pmatrix} -1.0 \\ 0 \end{pmatrix};$$

$$\mathbf{M}_{\mathbf{wx}} = \begin{pmatrix} 0 & 0 \\ 1.0 & 0 \\ 1.0 & 0 \end{pmatrix};$$

$$\mathbf{M}_{\mathbf{ww}} = \begin{pmatrix} 0 & 0 & 1.0 \\ 0 & 0 & 0 \\ -1.0 & 0 & 0 \end{pmatrix};$$

$$\mathbf{M}_{\mathbf{wy}} = \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix};$$

$$\mathbf{M}_{\mathbf{yx}} = \begin{pmatrix} 1.0 & 0 \end{pmatrix};$$

$$\mathbf{M}_{\mathbf{yw}} = \begin{pmatrix} 0 & 0 & 0 \end{pmatrix};$$

$$\mathbf{M}_{\mathbf{yy}} = \begin{pmatrix} 0 \end{pmatrix};$$

$$\mathbf{J} = \begin{pmatrix} 0 & -1.0 & 0 & -1.0 & -1.0 & -1.0 \\ 1.0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1.0 & 0 \\ 1.0 & 0 & 0 & 0 & 0 & 0 \\ 1.0 & 0 & -1.0 & 0 & 0 & 0 \\ 1.0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix};$$

$$\mathbf{J}_{\mathbf{xx}} = \begin{pmatrix} 0 & -1.0 \\ 1.0 & 0 \end{pmatrix};$$

$$\mathbf{J}_{\mathbf{xw}} = \begin{pmatrix} 0 & -1.0 & -1.0 \\ 0 & 0 & 0 \end{pmatrix};$$

$$\mathbf{J}_{\mathbf{xy}} = \begin{pmatrix} -1.0 \\ 0 \end{pmatrix};$$

$$\mathbf{J}_{\mathbf{w}\mathbf{w}} = \begin{pmatrix} 0 & 0 & 1.0 \\ 0 & 0 & 0 \\ -1.0 & 0 & 0 \end{pmatrix};$$

$$\mathbf{J}_{\mathbf{w}\mathbf{y}} = \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix};$$

$$\mathbf{J}_{\mathbf{y}\mathbf{y}} = \begin{pmatrix} 0 \end{pmatrix};$$

$$\mathbf{R} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix};$$

$$\mathbf{R}_{\mathbf{x}\mathbf{x}} = \begin{pmatrix} 0 & 0 \\ 0 & 0 \end{pmatrix};$$

$$\mathbf{R}_{\mathbf{x}\mathbf{w}} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix};$$

$$\mathbf{R}_{\mathbf{x}\mathbf{y}} = \begin{pmatrix} 0 \\ 0 \end{pmatrix};$$

$$\mathbf{R}_{\mathbf{w}\mathbf{w}} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix};$$

$$\mathbf{R}_{\mathbf{w}\mathbf{y}} = \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix};$$

$$\mathbf{R}_{\mathbf{y}\mathbf{y}} = \begin{pmatrix} 0 \end{pmatrix};$$