

Exercise 13.1.18

Construct phrase-structure grammars to generate each of these sets.

We create a grammar $G = (V, T, S, P)$.

Vocabulary: $V = \{0, 1, S, A\}$

Terminals: $T = \{0, 1\}$

Starting symbol: S

Productions: P will be different for each task.

a) $\{01^{2n} \mid n \geq 0\}$

$$P = \begin{cases} S \rightarrow 0A \\ A \rightarrow 11A \\ A \rightarrow \lambda \end{cases}$$

b) $\{0^n 1^{2n} \mid n \geq 0\}$

$$P = \begin{cases} S \rightarrow \lambda \\ S \rightarrow 0S11 \end{cases}$$

c) $\{0^n 1^m 0^n \mid m \geq 0 \text{ and } n \geq 0\}$

$$P = \begin{cases} S \rightarrow A \\ S \rightarrow 0S0 \\ A \rightarrow 1A \\ A \rightarrow \lambda \end{cases}$$

Exercise 13.4.6

Express each of these sets using a regular expression.

a) The set containing all strings with zero, one, or two bits
 $(\lambda \cup 0 \cup 1)(\lambda \cup 0 \cup 1)(\lambda \cup 0 \cup 1)$

b) The set of strings of two 0s, followed by zero or more 1s, and ending with a 0
 001^*0

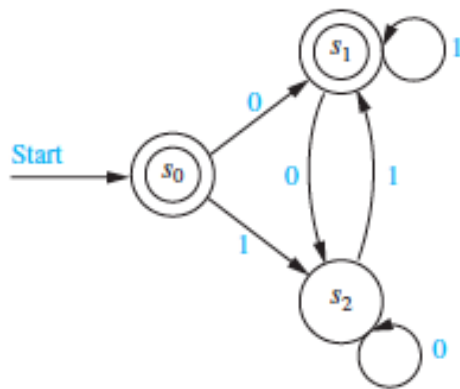
c) The set of strings with every 1 followed by two 0s
 $(0 \cup 100)^*$

d) The set of strings ending in 00 and not containing 11
 $(1 \cup \lambda)(0 \cup 01)^*00$

e) The set of strings containing an even number of 1s
 $(0 \cup 11)^*$

Exercise 13.4.16

Construct a regular grammar $G = (V, T, S, P)$ that generates the language recognized by the given finite-state machine.



We have the grammar $G = (V, T, S, P)$ where:

Vocabulary: $V = \{0, 1, S, A, B\}$

Terminals: $T = \{0, 1\}$

Starting symbol: S

Productions:

$$P = \begin{cases} S \rightarrow \lambda \\ S \rightarrow 0A \\ S \rightarrow 1B \\ A \rightarrow \lambda \\ A \rightarrow 1A \\ A \rightarrow 0B \\ B \rightarrow 0B \\ B \rightarrow 1A \end{cases}$$

To explain the many productions;

From our starting symbol S we can do one of three things: Either terminate using the empty string or use a 0 and go to the final state (we call it A) or to the non-final state using a 1 (we call it B)

Whenever we are in the final state (A), we can use a 1 and stay in the final state or we can use a 0 and go to the state B . We can also terminate by using the empty string.

Whenever we are in the non-final state B , we can either use a 1 to go the final state A or we can use a 0 and stay in the non-final state B .