# Secure Computing of Table with FLUTE

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# Lookup Table

#### LUT (Lookup Table)

 $\delta$ -to- $\sigma$  lookup table T is a function T:  $\{0,1\}^{\delta} \to \{0,1\}^{\sigma}$ .

$x_1$	$x_2$	$x_3$	у	Coal	Given secret sha
0	0	0	1	GOal	and $x_3$ , we want
0		1	0		secret shares of $\frac{1}{2}$
0	1	0	0		
0	1		1	Question	What secret sha
1	0	0	0		should we use?
1	0	1	1	Question	How can we opt
1	1	0	0		and setup cost?
1	1	1	0		per LUT caculat
			•		phase!)

Example 3-to-1 LUT T

ares of  $x_1, x_2,$ t to compute the  $T(x_1, x_2, x_3)$ .

aring scheme

timize the online (Up to  $2\sigma$  bits tion in the online Secret Sharing Scheme

# [·] Secret Sharing

 $P_0$ ,  $P_1$ : parties

## [·] Secret Sharing

A bit  $v \in \mathbb{Z}_2$  is said to be  $[\cdot]$ -shared between  $P_0$  and  $P_1$  if  $P_i$  holds  $[v]_i$  such that

$$\nu = [\nu]_0 \oplus [\nu]_1.$$

# [·] Secret Sharing

The  $\lceil \cdot \rceil$ -sharing is *linear* in the sense that:

• For  $[\cdot]$ -shared  $u, v \in \mathbb{Z}_2$ ,  $[\cdot]$ -sharing of  $u \oplus v$  can be locally computed by:

$$[u \oplus v]_i = [u]_i \oplus [v]_i$$
 for each  $i \in \{0, 1\}$ .

② For  $[\cdot]$ -shared  $v \in \mathbb{Z}_2$  and public  $b \in \mathbb{Z}_2$ ,  $[\cdot]$ -sharing of bv can be locally computed by:

$$[bv]_i = b[v]_i$$
 for each  $i \in \{0, 1\}$ .

§ For  $[\cdot]$ -shared  $v \in \mathbb{Z}_2$  and public  $b \in \mathbb{Z}_2$ ,  $[\cdot]$ -sharing of  $v \oplus b$  can be locally computed by:

$$[v \oplus b]_i = [v]_i \oplus ib$$
 for each  $i \in \{0, 1\}$ .

In particular,  $\lceil \cdot \rceil$ -sharing of  $\overline{v} = v \oplus 1$  can be locally computed.

## Multiplication of [·]-shared Values

### Beaver's Multiplication Triple

Suppose  $P_0$  and  $P_1$  have  $[\cdot]$ -shares of  $u, v \in \mathbb{Z}_2$ . Suppose additionally that they have  $[\cdot]$ -shares of a, b, c where c = ab.

- P<sub>i</sub> computes  $[u \oplus a]_i$  and  $[v \oplus b]_i$ , and sends them to  $P_{1-i}$ .
- 2  $P_0$  and  $P_1$  now know  $d := u \oplus a$  and  $e := v \oplus b$ .
- $P_i$  computes  $[z]_i = i \cdot de \oplus d[b]_i \oplus e[a]_i \oplus [c]_i$ .
- **①** Then,  $[z]_0$  ⊕  $[z]_1 = z = uv$ .

With the prepared multiplication triple, a  $[\cdot]$ -share of uv is calculated with the cost of four bits in a single round.

$$z = uv = (d \oplus a)(e \oplus b)$$

$$= \underbrace{de}_{\text{public}} \oplus db \oplus ea \oplus \underbrace{ab}_{=c}$$

# ⟨·⟩ Secret Sharing

## ⟨·⟩ Secret Sharing

A bit  $v \in \mathbb{Z}_2$  is said to be  $\langle \cdot \rangle$ -shared if:

- **1** A value  $\lambda_{\nu} \in \mathbb{Z}_2$  is [·]-shared between  $P_0$  and  $P_1$ .
  - $[\lambda_{v}]_{i}$ 's are locally set arbitrarily.
- ② A value  $m_v \in \mathbb{Z}_2$  is known to both parties.
- $\circ$   $\nu = m_{\nu} \oplus \lambda_{\nu}$

The  $\langle \cdot \rangle$ -share of  $\nu$  is denoted  $\langle \nu \rangle_i = (m_{\nu}, [\lambda_{\nu}]_i)$ .

# ⟨·⟩ Secret Sharing

The  $\langle \cdot \rangle$ -sharing is *linear* in the sense that:

**1** For  $\langle \cdot \rangle$ -shared  $u, v \in \mathbb{Z}_2$ ,  $\langle \cdot \rangle$ -sharing of  $u \oplus v$  can be locally computed by:

$$\mathsf{m}_{u\oplus v}=\mathsf{m}_u\oplus \mathsf{m}_v$$
 and  $[\lambda_{u\oplus v}]_i=[\lambda_u]_i\oplus [\lambda_v]_i$ 

 $\bullet$  For  $\langle \cdot \rangle$ -shared  $v \in \mathbb{Z}_2$  and public  $b \in \mathbb{Z}_2$ ,  $\langle \cdot \rangle$ -sharing of bv can be locally computed by:

$$\mathbf{m}_{b\nu} = b\mathbf{m}_{\nu}$$
 and  $[\lambda_{b\nu}]_i = b[\lambda_{\nu}]_i$ .

**3** For  $\langle \cdot \rangle$ -shared  $v \in \mathbb{Z}_2$  and public  $b \in \mathbb{Z}_2$ ,  $\langle \cdot \rangle$ -sharing of  $v \oplus b$  can be locally computed by:

$$\mathsf{m}_{v\oplus b}=\mathsf{m}_v\oplus b$$
.

In particular,  $\langle \cdot \rangle$ -sharing of  $\overline{\nu} = \nu \oplus 1$  can be locally computed.

## **LUT** Revisited

$x_1$	$x_2$	$x_3$	у
0	0	0	1
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	0
1	1	1	0

Example 3-to-1 LUT T

$$(\overline{x_1} \wedge \overline{x_2} \wedge \overline{x_3})$$

$$\vee (\overline{x_1} \wedge x_2 \wedge x_3)$$

$$\vee (x_1 \wedge \overline{x_2} \wedge x_3)$$

DNF representation of T

$$(\overline{x_1} \wedge \overline{x_2} \wedge \overline{x_3})$$

$$\oplus (\overline{x_1} \wedge x_2 \wedge x_3)$$

$$\oplus (x_1 \wedge \overline{x_2} \wedge x_3)$$

An equivalent circuit.

$$y = \begin{pmatrix} \overline{x_1} \\ \overline{x_1} \\ x_1 \end{pmatrix} \odot \begin{pmatrix} \overline{x_2} \\ \underline{x_2} \\ \overline{x_2} \end{pmatrix} \odot \begin{pmatrix} \overline{x_3} \\ x_3 \\ x_3 \end{pmatrix}$$

"Multi-Fan-In Inner Product"

Building Blocks: Multiplication

# Multiplication of $\langle \cdot \rangle$ -shared Values

$$z = uv = (\mathsf{m}_u \oplus \lambda_u)(\mathsf{m}_v \oplus \lambda_v)$$
$$= \underbrace{\mathsf{m}_u \mathsf{m}_v}_{\mathsf{public}} \oplus \mathsf{m}_u \lambda_v \oplus \mathsf{m}_v \lambda_u \oplus \underbrace{\lambda_u \lambda_v}_{=\lambda_{uv}}$$

#### Multiplication of $\langle \cdot \rangle$ -shared Values

Input  $\langle \cdot \rangle$ -shares of  $u, v \in \mathbb{Z}_2$  and  $[\cdot]$ -shares of  $\lambda_{uv} := \lambda_u \lambda_v$ .

Output  $\langle \cdot \rangle$ -shares of uv.

- ①  $P_i$  computes  $[z]_i = i \cdot m_{ii} m_{ij} \oplus m_{ij} [\lambda_{ij}]_i \oplus m_{ij} [\lambda_{ij}]_i \oplus [\lambda_{iii}]_i$ .
- $P_i$  randomly chooses  $[\lambda_z]_i \in \mathbb{Z}_2$ .
- 3  $P_i$  computes  $[m_z]_i = [z]_i \oplus [\lambda_z]_i$  and sends it to  $P_{i-1}$ .
- 1 Then,  $P_0$  and  $P_1$  have  $\langle \cdot \rangle$ -shares of z = uv.

With the prepared multiplication triple, a  $\langle \cdot \rangle$ -share of uv is calculated with the cost of two bits in a single round.

# Inner Product of $\langle \cdot \rangle$ -shared Values

### Inner Product of $\langle \cdot \rangle$ -shared Values

Input  $\langle \cdot \rangle$ -shares of  $u^1, \cdots, u^N, v^1 \cdots, v^N \in \mathbb{Z}_2$  and  $[\cdot]$ -shares of  $\lambda_{u^1} \lambda_{v^1}, \cdots, \lambda_{u^N} \lambda_{v^N}$ .

Output  $\langle \cdot \rangle$ -shares of  $z = \bigoplus_{k=1}^{N} u^k v^k$ .

- $P_i$  computes  $[u^k v^k]_i$  for  $k \in [N]$  as before.
- $P_i$  randomly chooses  $[\lambda_z]_i \in \mathbb{Z}_2$ .
- **3**  $P_i$  computes  $[m_z]_i = [\lambda_z]_i \oplus \bigoplus_{k=1}^N [u^k v^k]_i$  and sends it to  $P_{1-i}$ .
- Then,  $P_0$  and  $P_1$  have  $\langle \cdot \rangle$ -shares of  $z = \bigoplus_{k=1}^N u^k v^k$ .

With the prepared N multiplication triples, a  $\langle \cdot \rangle$ -share of  $\bigoplus_{k=1}^N u^k v^k$  is calculated with the cost of two bits in a single round.

# Multi-Fan-In Product of $\langle \cdot \rangle$ -shared Values

## Multi-Fan-In Product of ⟨·⟩-shared Values

Input  $\langle \cdot \rangle$ -shares of  $u_1, \dots, u_M \in \mathbb{Z}_2$  and ???.

Output  $\langle \cdot \rangle$ -shares of  $\bigwedge_{i=1}^{M} u_i$ .

Let Q be a set of  $\langle \cdot \rangle$ -shared values (wires). We use the following notation:

$$\mathsf{m}_{\mathcal{Q}}\triangleq\bigwedge\nolimits_{u\in\mathcal{Q}}\mathsf{m}_{u}\quad\text{and}\quad\lambda_{\mathcal{Q}}\triangleq\bigwedge\nolimits_{u\in\mathcal{Q}}\lambda_{u}.$$

#### Observation

Preliminaries

Building Blocks: Multi-Fan-In Product

$$\bigwedge_{j=1}^M u_j = \bigwedge_{j=1}^M (\mathsf{m}_{u_j} \oplus \lambda_{u_j}) = \bigoplus_{\mathcal{Q} \subseteq \mathcal{I}} (\mathsf{m}_{\mathcal{Q}} \cdot \lambda_{\mathcal{I} \setminus \mathcal{Q}})$$

where  $\mathcal{I} := \{u_1, u_2, \cdots, u_M\}.$ 

## Multi-Fan-In Product of $\langle \cdot \rangle$ -shared Values

Input  $\langle \cdot \rangle$ -shares of  $u_1, \dots, u_M \in \mathbb{Z}_2$  and  $[\cdot]$ -shares of  $\lambda_O$  for each  $Q \subseteq \mathcal{I}$  with |Q| > 1 where  $\mathcal{I} = \{u_1, \dots, u_M\}$ .

Output  $\langle \cdot \rangle$ -shares of  $\bigwedge_{i=1}^{M} u_i$ .

 $\bigcirc$   $P_i$  computes

$$[z]_i = i \cdot \mathsf{m}_{\mathcal{I}} \oplus \bigoplus_{\mathcal{Q} \subsetneq \mathcal{I}} (\mathsf{m}_{\mathcal{Q}} \cdot [\lambda_{\mathcal{I} \setminus \mathcal{Q}}]_i).$$

- $P_i$  randomly chooses  $[\lambda_{\alpha}]_i \in \mathbb{Z}_2$ .
- **3**  $P_i$  computes  $[m_z]_i = [z]_i \oplus [\lambda_z]_i$  and sends it to  $P_{1-i}$ .
- Then,  $P_0$  and  $P_1$  have  $\langle \cdot \rangle$ -shares of  $\bigwedge_{i=1}^M u_i$ .

With the prepared  $2^M - M - 1$  multiplication triples, a  $\langle \cdot \rangle$ -share of  $\bigwedge_{i=1}^{M} u_i$  is calculated with the cost of two bits in a single round.

## Multi-Fan-In Inner Product of $\langle \cdot \rangle$ -shared Values

Input  $\langle \cdot \rangle$ -shares of  $\mathbf{u}^1, \dots, \mathbf{u}^M \in (\mathbb{Z}_2)^N$  and  $[\cdot]$ -shares of  $\lambda_{\mathcal{O}}$  for each  $Q \subseteq \mathcal{I}_k$  with |Q| > 1 where  $\mathcal{I}_k = \{\mathbf{u}_k^1, \dots, \mathbf{u}_k^M\}$  for  $k \in [N]$ .

Output  $\langle \cdot \rangle$ -shares of  $\mathbf{u}^1 \odot \cdots \odot \mathbf{u}^N = \bigoplus_{k=1}^N \bigwedge_{i=1}^M \mathbf{u}_k^j$ .

 $\bigcirc$   $P_i$  computes

$$[z]_i = i \cdot igoplus_{k=1}^N \mathsf{m}_{\mathcal{I}_k} \oplus igoplus_{k=1}^N igoplus_{\mathcal{Q} \subset \mathcal{I}_k} (\mathsf{m}_{\mathcal{Q}} \cdot [\lambda_{\mathcal{I} \setminus \mathcal{Q}}]_i).$$

- ②  $P_i$  randomly chooses  $[\lambda_{\alpha}]_i \in \mathbb{Z}_2$ .
- **3**  $P_i$  computes  $[m_z]_i = [z]_i \oplus [\lambda_z]_i$  and sends it to  $P_{1-i}$ .
- Then,  $P_0$  and  $P_1$  have  $\langle \cdot \rangle$ -shares of  $\mathbf{u}^1 \odot \cdots \odot \mathbf{u}^N$ .

With the prepared  $N(2^M - M - 1)$  multiplication triples, a  $\langle \cdot \rangle$ -share of  $\bigcap_{i=1}^{N} \mathbf{u}^{j}$  is calculated with the cost of two bits in a single round.

Input  $\langle \cdot \rangle$ -shares of  $\mathbf{u}^1, \cdots, \mathbf{u}^M \in (\mathbb{Z}_2)^N$  and  $[\cdot]$ -shares of  $\lambda_{\mathcal{Q}}$  for each  $\mathcal{Q} \subseteq \mathcal{I}_k$  with  $|\mathcal{Q}| > 1$  where  $\mathcal{I}_k = \{\mathbf{u}_k^1, \cdots, \mathbf{u}_k^M\}$  for  $k \in [N]$ .

Output  $\langle \cdot \rangle$ -shares of  $\mathbf{u}^1 \odot \cdots \odot \mathbf{u}^N = \bigoplus_{k=1}^N \bigwedge_{j=1}^M \mathbf{u}_k^j$ .

With the prepared  $N(2^M-M-1)$  multiplication triples, a  $\langle \cdot \rangle$ -share of  $\bigcirc_{j=1}^N \mathbf{u}^j$  is calculated with the cost of two bits in a single round.

$$y = \begin{pmatrix} \overline{x_1} \\ \overline{x_1} \\ x_1 \end{pmatrix} \odot \begin{pmatrix} \overline{x_2} \\ \overline{x_2} \\ \overline{x_2} \end{pmatrix} \odot \begin{pmatrix} \overline{x_3} \\ x_3 \\ x_3 \end{pmatrix} \qquad \qquad \begin{aligned} & \text{For } \delta\text{-to-1 LUT,} \\ & N \leq 2^{\delta-1} \text{ and } M = \delta?? \\ & 2^{\delta-1}(2^{\delta} - \delta - 1) \text{ triples??} \end{aligned}$$

We now exploit the fact that elements of  $\mathbf{u}^j$  are closely related.

 $\lambda_{v}$  is unchanged when calculating shares of  $\overline{v}$ !

### Calculating LUT

#### **Some Definitions**

Fix a  $\delta$ -to- $\sigma$  LUT T.

$x^1$	$x^2$	$x^3$	$y^1$	$y^2$
0	0	0	1	0
0	0	1	0	0
0	1	0	0	0
0	1	1	1	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	0
_1	1	1	0	1
$\mathbf{e}^1$	$\mathbf{e}^2$	$e^3$	$\mathbf{y}^1$	$\mathbf{y}^2$

For instance, in this example,

$$\mathbf{e}^{2} = \begin{pmatrix} 0 \\ 0 \\ 1 \\ 1 \\ 0 \\ 0 \\ 1 \\ 1 \end{pmatrix} \quad \text{and} \quad \mathbf{y}^{1} = \begin{pmatrix} 1 \\ 0 \\ 0 \\ 1 \\ 1 \\ 0 \\ 0 \\ 0 \end{pmatrix}$$

## **Expressing LUT with Multi-Fan-In Inner Product**

Now, in the previous example, note that:

$$\mathbf{z}^{1} = \begin{pmatrix} \overline{x^{1}} \\ \overline{x^{1}} \\ x^{1} \end{pmatrix} \odot \begin{pmatrix} \overline{x^{2}} \\ x^{2} \\ \overline{x^{2}} \end{pmatrix} \odot \begin{pmatrix} \overline{x^{3}} \\ x^{3} \\ x^{3} \end{pmatrix}$$

$$= \begin{pmatrix} \overline{x^{1}} \\ \overline{x^{1}} \\ \overline{x^{1}} \\ \vdots \end{pmatrix} \odot \begin{pmatrix} \overline{x^{2}} \\ \overline{x^{2}} \\ x^{2} \\ x^{2} \\ \vdots \end{pmatrix} \odot \begin{pmatrix} \overline{x^{3}} \\ x^{3} \\ \overline{x^{3}} \\ x^{3} \\ \vdots \end{pmatrix} \odot \begin{pmatrix} 1 \\ 0 \\ 0 \\ 1 \\ \vdots \end{pmatrix}$$

$$= (\overline{x^{1}} \oplus \mathbf{e}^{1}) \odot \cdots \odot (\overline{x^{3}} \oplus \mathbf{e}^{3}) \odot \mathbf{y}^{1}$$

 $<sup>\</sup>overline{x^j} \oplus \mathbf{e}^j$  is an element-wise addition.

## **Expressing LUT with Multi-Fan-In Inner Product**

Fixing a  $\delta$ -to- $\sigma$  LUT T, and given  $\langle \cdot \rangle$ -shares of  $x^1, \dots, x^{\delta}$ , let

$$\mathbf{u}^j \coloneqq \overline{x^j} \oplus \mathbf{e}^j \in (\mathbb{Z}_2)^{2^\delta}$$

for  $j \in [\delta]$  so that

$$\langle \mathbf{u}_k^j \rangle_i = \left( \overline{\mathsf{m}_{x^j}} \oplus \mathbf{e}_k^j, [\lambda_{x^j}]_i \right)$$

gives a  $\langle \cdot \rangle$ -sharing of  $\mathbf{u}_{k}^{j}$  for  $j \in [\delta]$ ,  $k \in [2^{\delta}]$ .

With this, we have

$$\lambda_{\mathbf{u}_{k_1}^{j_1}\cdots\mathbf{u}_{k_n}^{j_n}}=\lambda_{\chi^{j_1}\cdots\chi^{j_n}}!$$

## Expressing LUT with Multi-Fan-In Inner Product

As previously shown, the w-th output  $\mathbf{z}^w$  can be calculated by

$$\mathbf{z}^{w} = (\overline{x^{1}} \oplus \mathbf{e}^{1}) \odot \cdots \odot (\overline{x^{\delta}} \oplus \mathbf{e}^{\delta}) \odot \mathbf{y}^{w}$$

$$= \mathbf{u}^{1} \odot \cdots \odot \mathbf{u}^{\delta} \odot \mathbf{y}^{w}$$

$$= \bigoplus_{k=1}^{2^{\delta}} \left[ \left( \bigwedge_{j=1}^{\delta} \mathbf{u}_{k}^{j} \right) \wedge \mathbf{y}_{k}^{w} \right]$$

$$= \bigoplus_{k=1}^{2^{\delta}} \left[ \left( \bigwedge_{j=1}^{\delta} \left( \mathbf{m}_{\mathbf{u}_{k}^{j}} \oplus \lambda_{\mathbf{u}_{k}^{j}} \right) \right) \wedge \mathbf{y}_{k}^{w} \right]$$

$$= \bigoplus_{k=1}^{2^{\delta}} \bigoplus_{Q_{k} \subseteq \mathcal{I}_{k}} \left( \mathbf{m}_{Q_{k}} \cdot \mathbf{y}_{k}^{w} \cdot \lambda_{\mathcal{I}_{k} \setminus Q_{k}} \right).$$

# Calculating LUT

Calculating LUT

#### Calculating $\delta$ -to- $\sigma$ LUT

Input A  $\delta$ -to- $\sigma$  LUT T,  $\langle \cdot \rangle$ -shares of  $x^1, \dots, x^{\delta} \in \mathbb{Z}_2$ , and [·]-shares of  $\lambda_{\mathcal{Q}}$  for each  $\mathcal{Q} \subseteq \mathcal{I}$  with  $|\mathcal{Q}| > 1$  where  $\mathcal{I} = \{x^1, \cdots, x^{\delta}\}.$ 

Output  $\langle \cdot \rangle$ -shares of  $\mathsf{T}(x^1, \cdots, x^\delta)$ .

- **1** P<sub>i</sub> computes its share of  $\mathbf{u}_{k}^{j} = \overline{x^{j}} \oplus \mathbf{e}_{k}^{j}$  for  $j \in [\delta]$  and  $k \in [2^{\delta}]$ .
- ②  $P_i$  computes, for each  $w \in [\sigma]$ ,

$$[\mathbf{z}_w]_i = i \cdot \bigoplus_{k=1}^{2^\delta} (\mathsf{m}_{\mathcal{I}_k} \cdot \mathbf{y}_k^w) \oplus \bigoplus_{k=1}^{2^\delta} \bigoplus_{\mathcal{Q}_k \subsetneq \mathcal{I}_k} \left( \mathsf{m}_{\mathcal{Q}_k} \cdot \mathbf{y}_k^w \cdot [\lambda_{\mathcal{I}_k \setminus \mathcal{Q}_k}]_i \right).$$

- **3**  $P_i$  randomly chooses  $[\lambda_{\mathbf{z}_{m}}]_i \in \mathbb{Z}_2$  for  $w \in [\sigma]$ .
- $P_i$  computes  $[\mathbf{m}_{\mathbf{z}_w}]_i = [\mathbf{z}_w]_i \oplus [\lambda_{\mathbf{z}_w}]_i$  for  $w \in [\sigma]$  and sends them to  $P_{1-i}$ .
- **5** Then,  $P_0$  and  $P_1$  have  $\langle \cdot \rangle$ -shares of  $\mathbf{z} = \mathsf{T}(x^1, \dots, x^\delta)$ .

## Calculating LUT

### Calculating $\delta$ -to- $\sigma$ LUT

Input A  $\delta$ -to- $\sigma$  LUT T,  $\langle \cdot \rangle$ -shares of  $x^1, \cdots, x^\delta \in \mathbb{Z}_2$ , and  $[\cdot]$ -shares of  $\lambda_{\mathcal{Q}}$  for each  $\mathcal{Q} \subseteq \mathcal{I}$  with  $|\mathcal{Q}| > 1$  where  $\mathcal{I} = \{x^1, \cdots, x^\delta\}$ .

Output  $\langle \cdot \rangle$ -shares of  $\mathsf{T}(x^1, \cdots, x^\delta)$ .

With the prepared  $2^{\delta} - \delta - 1$  multiplication triples, a  $\langle \cdot \rangle$ -share of  $\mathsf{T}(x^1, \cdots, x^{\delta})$  is calculated with the cost of  $2\sigma$  bits in a single round.

Preliminaries Pros and Cons

### **Pros and Cons**

#### Pros

 Any complex circuit can be represented by a interconnection of small LUTs.

Calculating LUT

- Evaluation does not depend on the internal logic.
- Setup does not depend on the number of outputs.

#### Cons

- Exponential setup time/communication.
- Exponential internal calculation.

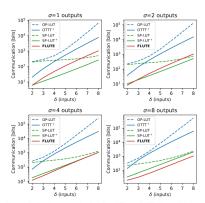


Figure 7: Total communication for different LUT sizes with  $2 \le \delta \le 8$  inputs and  $\sigma \in \{1,2,4,8\}$  outputs.

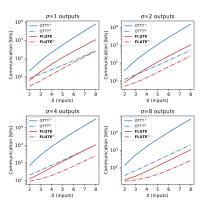
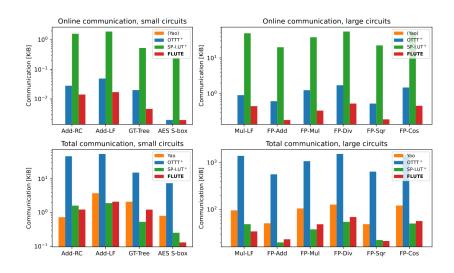


Figure 8: Total communication for different LUT sizes with  $2 \le \delta \le 8$  inputs and  $\sigma \in \{1,2,4,8\}$  outputs using a helper server  $S_{\mathcal{H}}$  (cf. §C).

# Online/Total Communication Compared with Other Protocols



#### References

Brüggemann, A., Hundt, R., Schneider, T., Suresh, A., & Yalame, H. (2023). Flute: Fast and secure lookup table evaluations. 2023 IEEE Symposium on Security and Privacy (SP).

https://doi.org/10.1109/sp46215.2023.10179345