

Indian Institute of Technology Kharagpur  
Department of Mathematics  
MA11004 - Linear Algebra, Numeircal and Complex Analysis  
Problem Sheet - Answers/Hints- 5  
Spring 2021

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1. **Hint:**  $\Delta \log f(x) = \log f(x+h) - \log f(x)$
2. **Hint:** Use the basic error formula of interpolation.
3. **Ans:**  $x^3 + x^2 - 3x + 1$
4. **Ans:** 48  
**Hint:** Use Newton's forward interpolation formula
5. **Ans:** 96.6352 thousands  
**Hint:** Use Newton's backward interpolation formula
6. **Ans:**  $f(5) = 32.9333$   
**Hint:** Use Lagrange's interpolation formula for five nodal points.
7. **Ans:**  $\frac{5}{2(x-1)} - \frac{15}{(x-2)} + \frac{31}{2(x-3)}$   
**Hint:** Take  $f(x) = 3x^2 + x + 1$  and use Lagrange's interpolation formula for  $f(x)$ .
8. **Hints:** Use Lagrange's formula for the arguments -3, -1, 1, 3 and then put  $x = 0$ .
9. **Ans:** 4.07152
10. **Ans:** 9855 feet  
**Hint:** Use trapezoidal formula for  $n = 14$ .
11. **Ans:**  $h \leq 0.0047$   
**Hint:** Error,  $E = -\frac{(b-a)h^2}{12} f''(\zeta)$ ,  $\zeta \in (a, b)$
12. **Hint:** Actual area =  $\int_{-h}^h y \, dx$
13. **Ans:** 1.8278472