

Question 1

Consider the function $f(x) = \frac{\sqrt{1+x} - 1}{x}$.

- (a) Use Matlab to evaluate the function value (without changing the form of the function) at $x = 0.1, 0.01, 0.001, \dots, 10^{-20}$.
- (b) Plot $f(x)$ using the function values in Part (a). You might use logarithm scale for the x-axis to clearly present the curve.
- (c) Is the above calculation consistent with $\lim_{x \rightarrow 0} f(x)$ and how do you explain it?
- (d) Rewrite the function as, $f(x) = \frac{1}{\sqrt{1+x} + 1}$, then redo the calculation (a)–(c).