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# Lecture Notes for Machine Learning in Python

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Professor Eric Larson  
Week Three, Lecture B

# Class Logistics and Agenda

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- Next Week: Project Work Week
  - and I am out of town all week...
- Finish Dimensionality Reduction
- Common Feature Extraction Methods for Images

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# Dimensionality Reduction (Continued)

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# Dimensionality Reduction: LDA

- PCA tell us variance explained by the data in different directions, but it ignores class labels
- Is there a way to find “components” that will help with **discriminate** between the classes?

$$\arg \max_{comp.} \frac{\sum \text{differences between classes}}{\sum \text{variance within classes}}$$

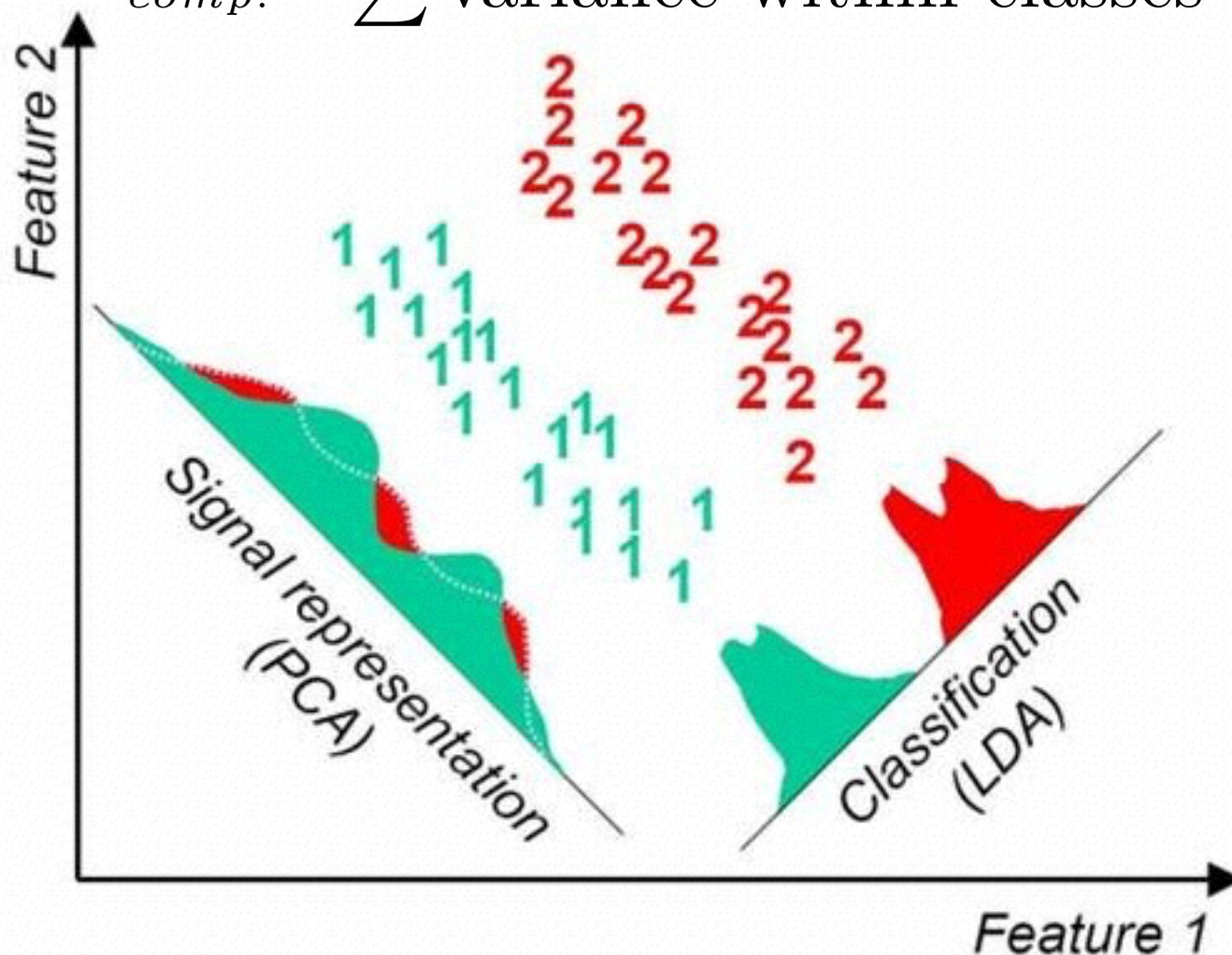
- called Fisher’s discriminant
- ...but we need to solve this using using *Lagrange multipliers* and gradient-based optimization
- which we haven’t covered yet

I invented Lagrange multipliers... and ...*nothing* impresses me...



# Dimensionality Reduction: LDA versus QDA

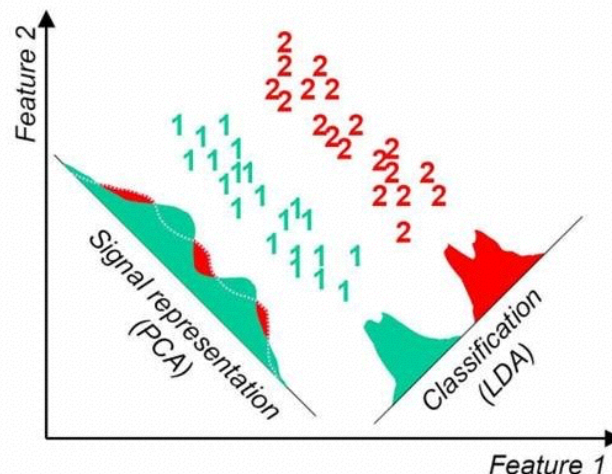
$$\arg \max_{comp.} \frac{\sum \text{differences between classes}}{\sum \text{variance within classes}}$$



# Dimensionality Reduction: LDA versus QDA

$$\arg \max_{comp.} \frac{\sum \text{differences between classes}}{\sum \text{variance within classes}}$$

- “*differences between classes*” is calculated by trying to separate the **mean value** of each **feature** in each **class**
- Linear discriminant analysis:
  - assume the covariance in each class is the same
- Quadrature discriminant analysis:
  - estimate the covariance for each class



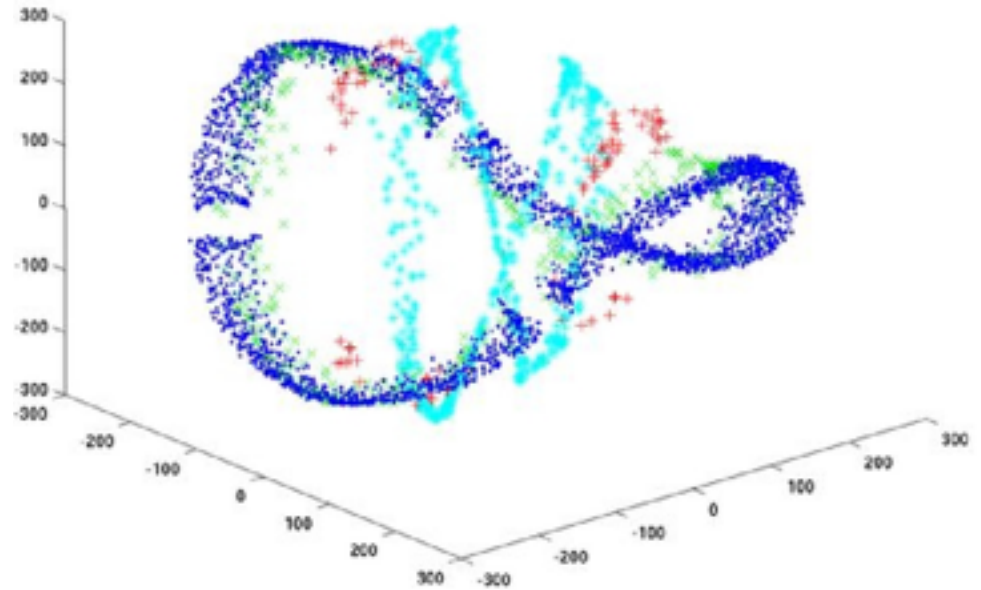
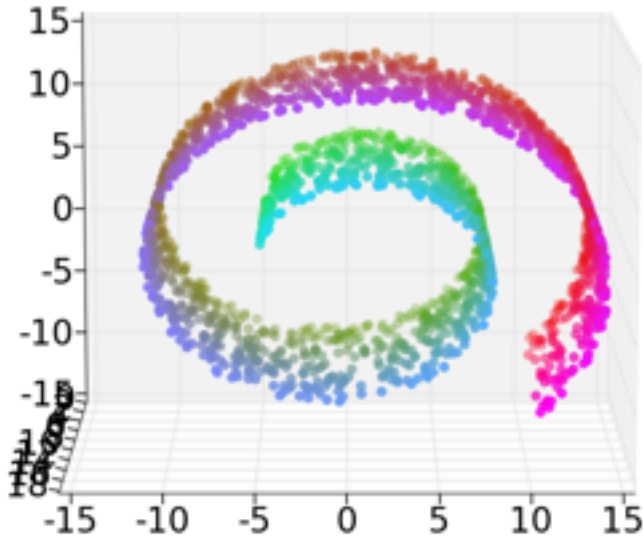
# Self Test ML2b.2

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LDA only allows as many components as there are unique classes in a dataset.

- A. True
- B. False

# Dimensionality Reduction: non-linear

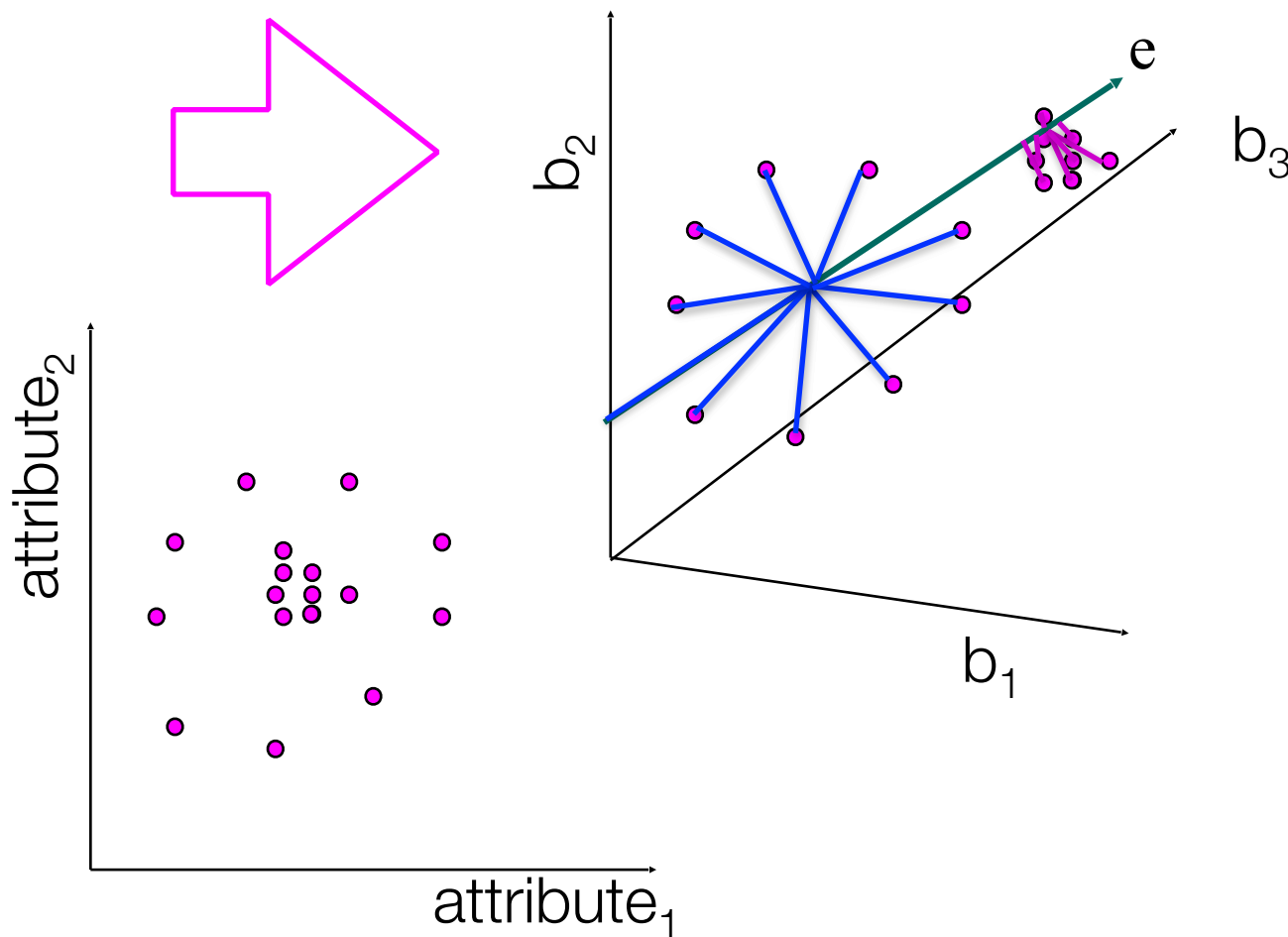


- Sometimes a **linear transform** is not enough
- A powerful non-linear transform has seen a resurgence in past decade: **kernel PCA**



# Kernel PCA

- Project to higher dimensional space
- Employ principal components
- Apply transform in higher dimensional space



|      |      |      |
|------|------|------|
| 37.1 | -6.7 | -3.2 |
| -6.7 | 43.9 | 1.45 |
| -3.2 | 1.45 | 12.1 |

|   | <i>B1</i> | <i>B2</i> | <i>B3</i> |
|---|-----------|-----------|-----------|
| 1 | 66        | 33.6      | 0.3       |
| 2 | 54        | 26.6      | 0.4       |
| 3 | 69        | 23.3      | -4        |
| 4 | 73        | 28.1      | -5.6      |
| 5 | 61        | 43.1      | 0.23      |
| 6 | 62        | 25.6      | -5        |

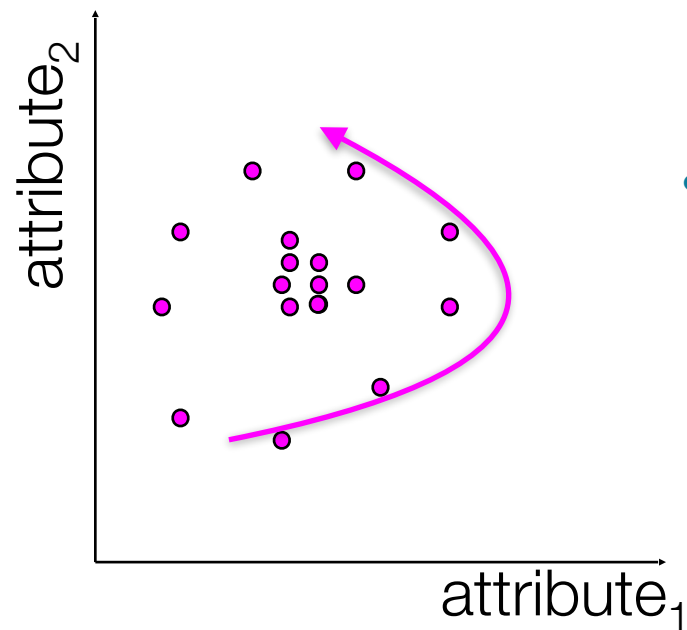
# Kernel PCA

**kernel:** defines what the dot product is in higher dimensional space

some kernels have corresponding transformations with **infinite dimensions!!**

- **Just the dot product**

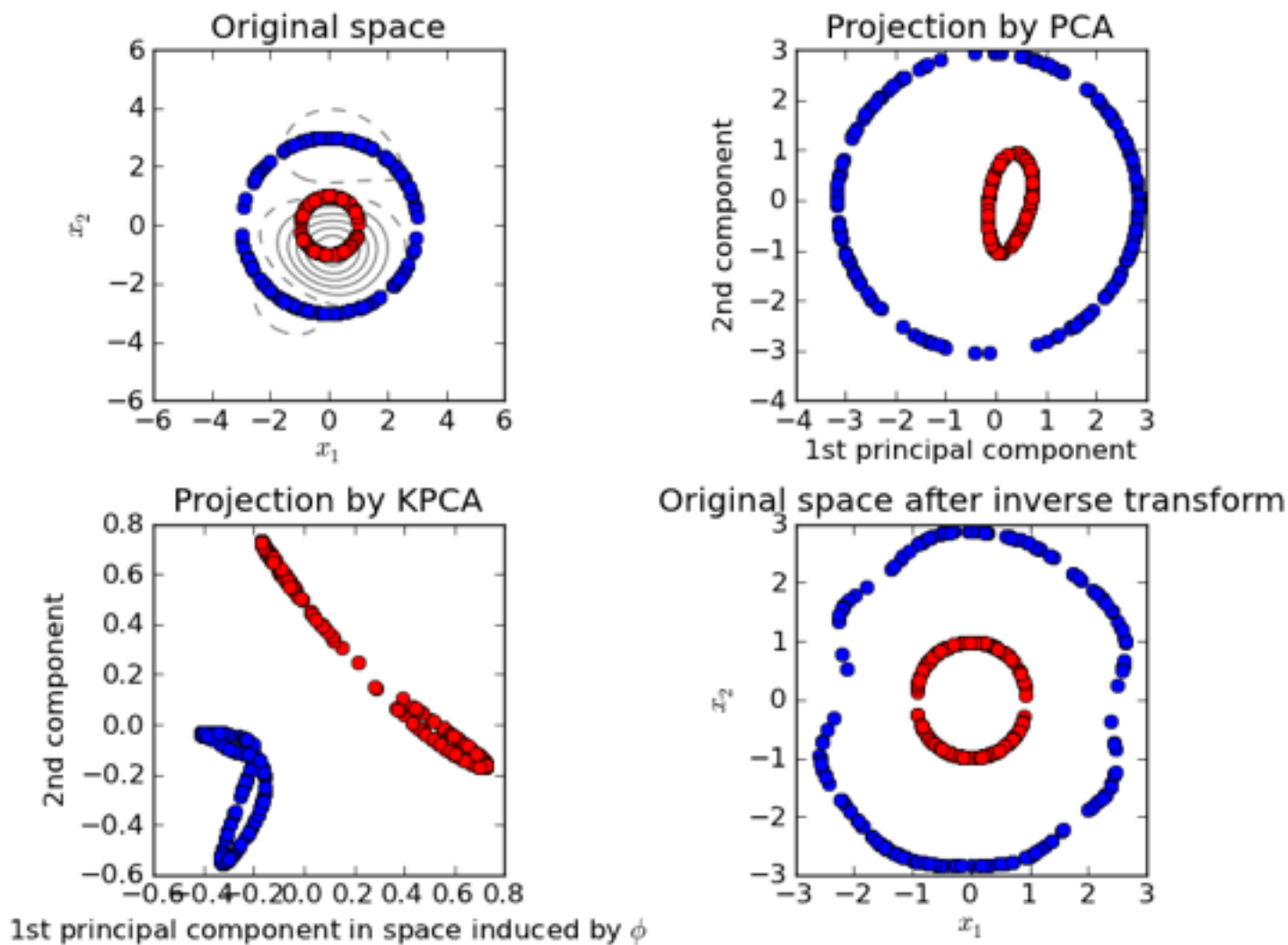
|      |      |      |
|------|------|------|
| 37.1 | -6.7 | -3.2 |
| -6.7 | 43.9 | 1.45 |
| -3.2 | 1.45 | 12.1 |



- **Key insight:** don't need to know the actual transformation vectors

|   | <i>B1</i> | <i>B2</i> | <i>B3</i> |
|---|-----------|-----------|-----------|
| 1 | 66        | 33.6      | 0.3       |
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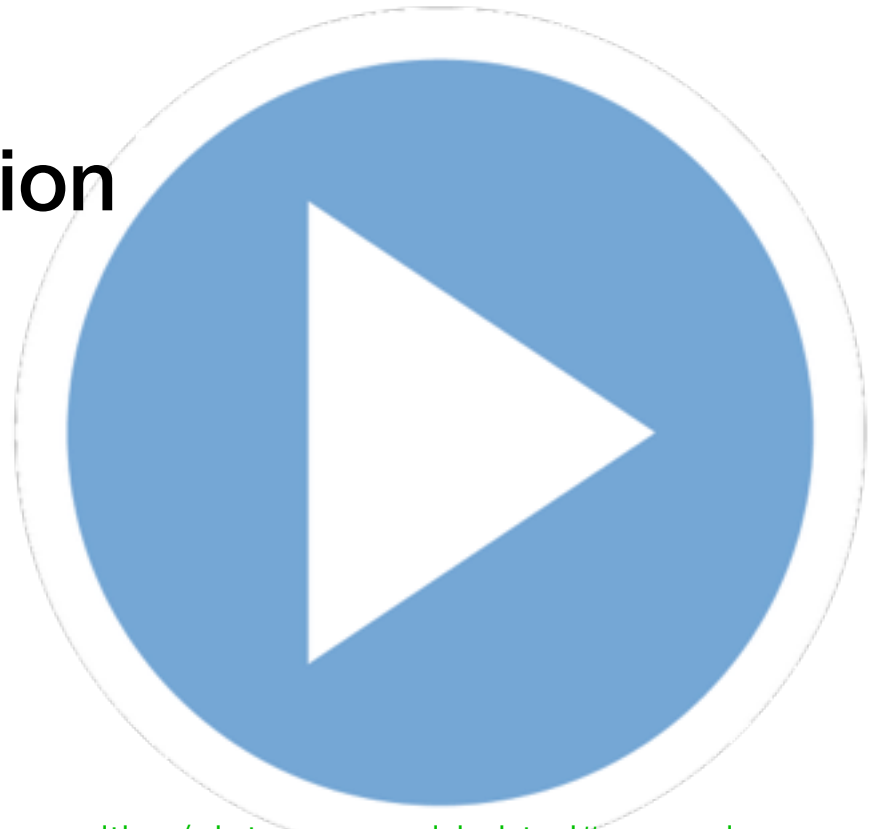
# Kernel PCA



## Dimension Reduction

PCA

LDA



## Other Tutorials:

[http://scikit-learn.org/stable/auto\\_examples/decomposition/plot\\_pca\\_vs\\_lda.html#example-decomposition-plot-pca-vs-lda-py](http://scikit-learn.org/stable/auto_examples/decomposition/plot_pca_vs_lda.html#example-decomposition-plot-pca-vs-lda-py)

<http://nbviewer.ipynb.org/github/ogrisel/notebooks/blob/master/Labeled%20Faces%20in%20the%20Wild%20recognition.ipynb>

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# Image Processing and Representation

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# What is image processing

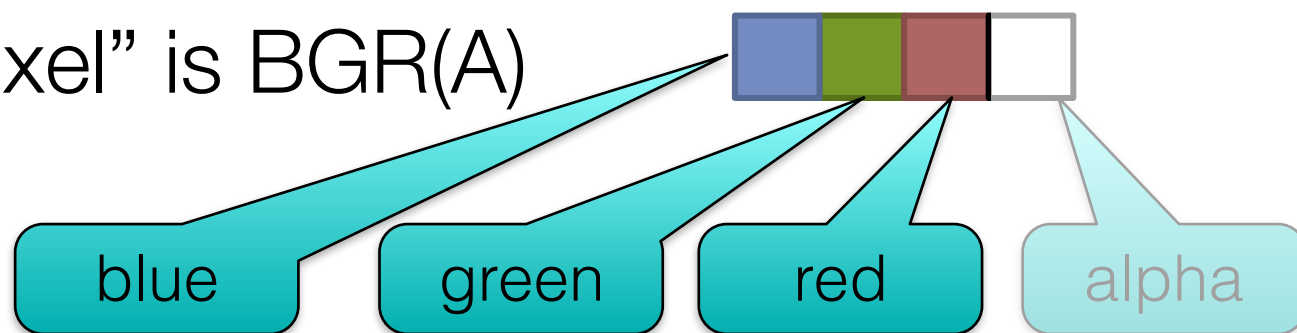
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- the **art** and **science** of manipulating pixels
  - combining images (blending or compositing)
  - enhancing edges and lines
  - adjusting contrast, color
  - warping, transformation
  - filtering
  - features extraction

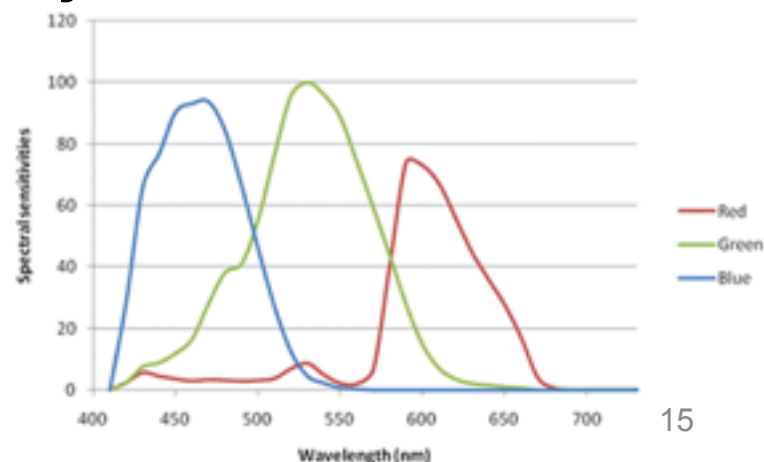
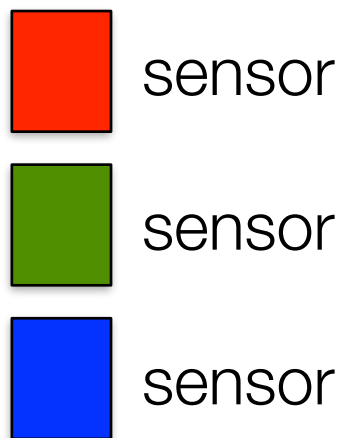
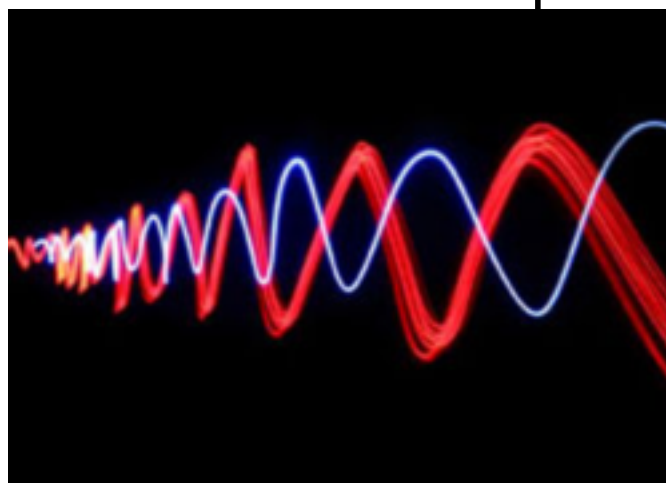
# Images as data

- an image can be represented in many ways
- most common format is a matrix of pixels

- each “pixel” is BGR(A)



- used for capture and display



# Image Representation

- need a compact representation

- **grayscale**

$$0.3 \cdot R + 0.59 \cdot G + 0.11 \cdot B,$$

“luminance”

gray

|   |   |   |   |   |   |
|---|---|---|---|---|---|
| 1 | 4 | 2 | 5 | 6 | 9 |
| 1 | 4 | 2 | 5 | 5 | 9 |
| 1 | 4 | 2 | 8 | 8 | 7 |
| 3 | 4 | 3 | 9 | 9 | 8 |
| 1 | 0 | 2 | 7 | 7 | 9 |
| 1 | 4 | 3 | 9 | 8 | 6 |
| 2 | 4 | 2 | 8 | 7 | 9 |

Numpy Matrix  
`image[rows, cols]`

on

R

G

B

|   |   |   |   |   |   |   |   |  |
|---|---|---|---|---|---|---|---|--|
|   |   | 1 | 4 | 2 | 5 | 6 | 9 |  |
|   | 1 | 4 | 2 | 5 | 6 | 9 | 9 |  |
| 1 | 4 | 2 | 5 | 6 | 9 | 9 | 7 |  |
| 1 | 4 | 2 | 5 | 5 | 9 | 7 | 8 |  |
| 1 | 4 | 2 | 8 | 8 | 7 | 8 | 9 |  |
| 3 | 4 | 3 | 9 | 9 | 8 | 9 | 6 |  |
| 1 | 0 | 2 | 7 | 7 | 9 | 6 | 9 |  |
| 1 | 4 | 3 | 9 | 8 | 6 | 9 |   |  |
| 2 | 4 | 2 | 8 | 7 | 9 |   |   |  |

Numpy Matrix  
`image[rows, cols, channels]`



# Image Representation, Features

**Problem:** need to represent image as table data

|   |   |   |   |   |   |
|---|---|---|---|---|---|
| 1 | 4 | 2 | 5 | 6 | 9 |
| 1 | 4 | 2 | 5 | 5 | 9 |
| 1 | 4 | 2 | 8 | 8 | 7 |
| 3 | 4 | 3 | 9 | 9 | 8 |
| 1 | 0 | 2 | 7 | 7 | 9 |
| 1 | 4 | 3 | 9 | 8 | 6 |
| 2 | 4 | 2 | 8 | 7 | 9 |

# Image Representation, Features

**Problem:** need to represent image as table data

**Solution:** row concatenation

|       |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |     |
|-------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|-----|
| Row 1 | 1 | 4 | 2 | 5 | 6 | 9 | 1 | 4 | 2 | 5 | 5 | 9 | 1 | 4 | 2 | 8 | 8 | 7 | 3 | ... |
| Row 2 | 1 | 4 | 2 | 8 | 8 | 7 | 3 | 4 | 3 | 9 | 9 | 8 | 1 | 4 | 2 | 5 | 5 | 9 | 1 | ... |
| ...   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |     |
| Row N | 9 | 4 | 6 | 8 | 8 | 7 | 4 | 1 | 3 | 9 | 2 | 1 | 1 | 5 | 2 | 1 | 5 | 9 | 1 | ... |

## Dimension Reduction with Images

Images Representation

Randomized PCA

Kernel PCA



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# Features of Images

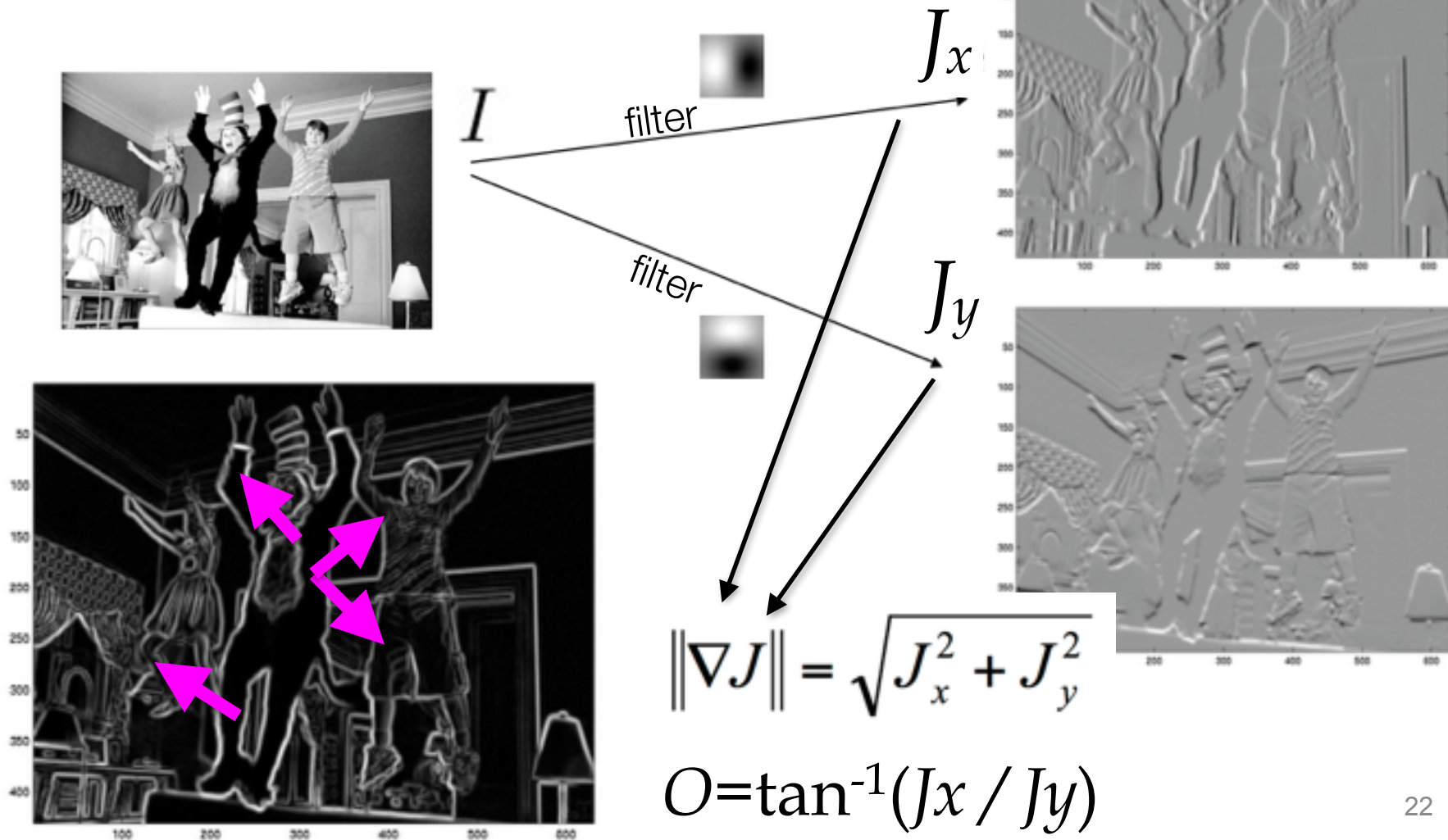
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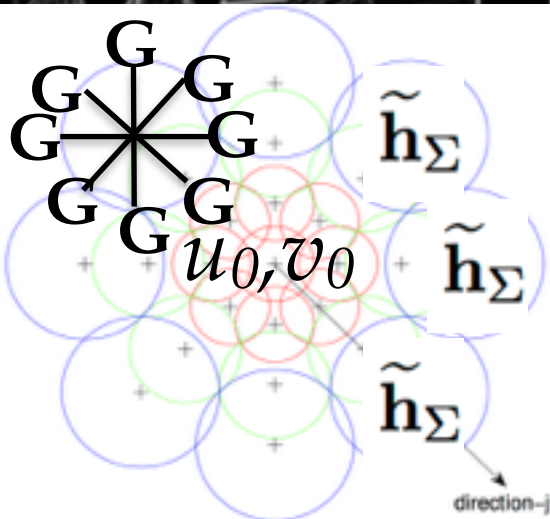


# Common operations

- the gradient (2D derivative)

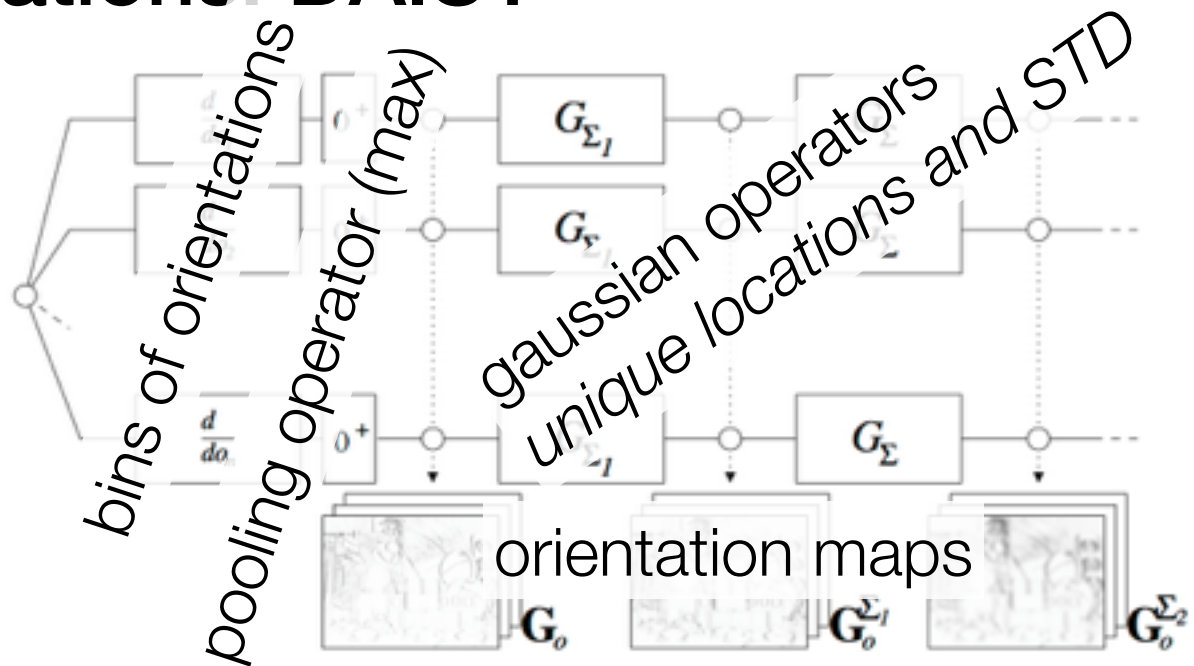


# Common operations: DAISY



$$\mathcal{D}(u_0, v_0) =$$

$$\left[ \begin{array}{l} \tilde{h}_{\Sigma_1}^\top(u_0, v_0), \\ \tilde{h}_{\Sigma_1}^\top(l_1(u_0, v_0, R_1)), \dots, \tilde{h}_{\Sigma_1}^\top(l_T(u_0, v_0, R_1)), \\ \tilde{h}_{\Sigma_2}^\top(l_1(u_0, v_0, R_2)), \dots, \tilde{h}_{\Sigma_2}^\top(l_T(u_0, v_0, R_2)), \end{array} \right]$$



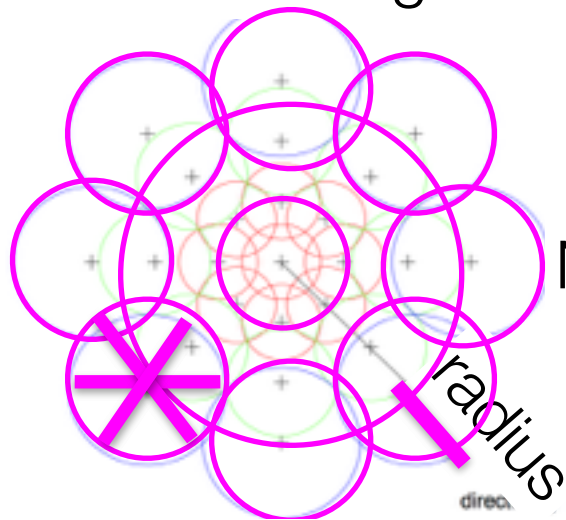
take normalized histogram at point  $u, v$

$$\tilde{h}_\Sigma(u, v) = \left\| \left[ \mathbf{G}_1^\Sigma(u, v), \dots, \mathbf{G}_H^\Sigma(u, v) \right]^\top \right\|$$

Tola et al. "Daisy: An efficient dense descriptor applied to wide-baseline stereo." Pattern Analysis and Machine Intelligence, IEEE Transactions

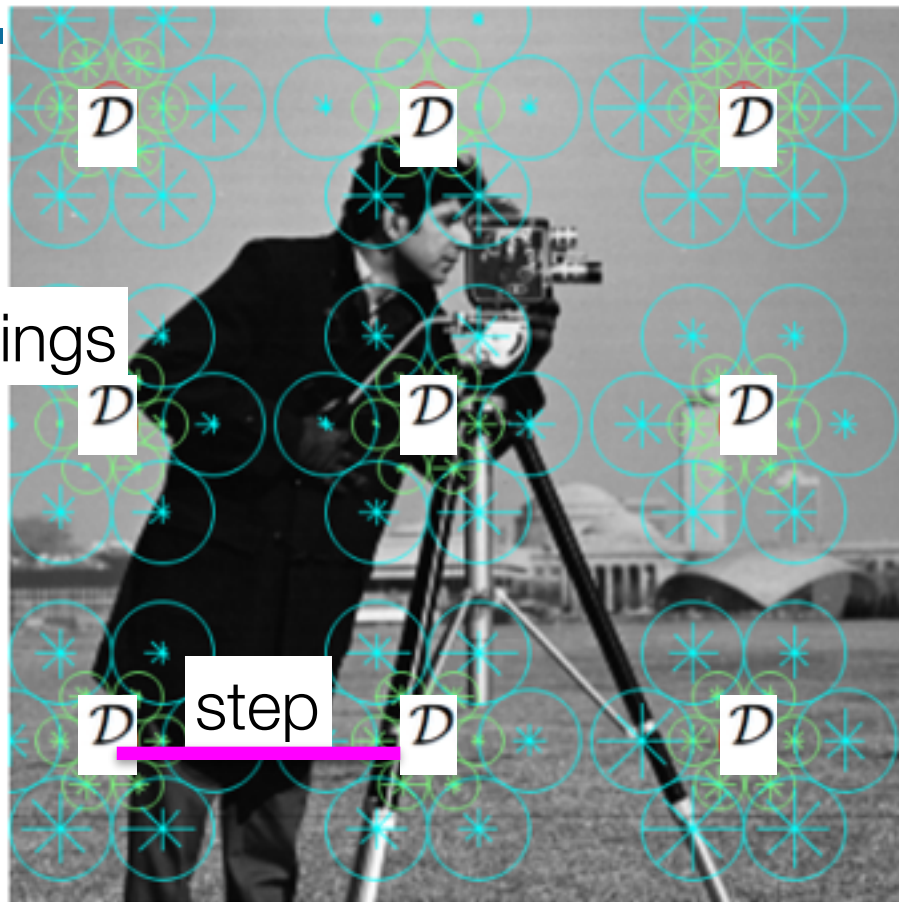
# Common operations: DAISY

Num histograms



Num rings

num orientations (bins)



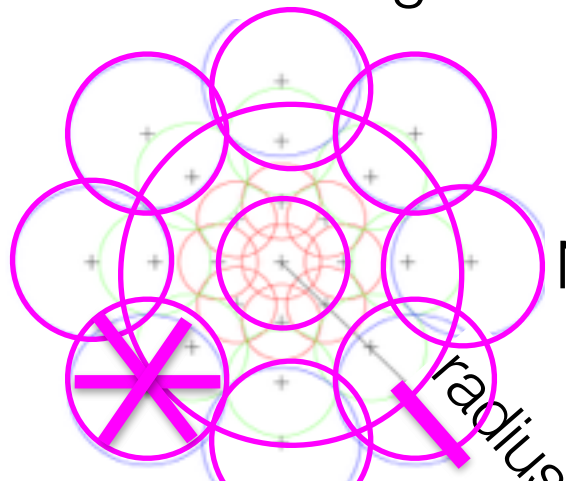
## Params:

step, radius, num rings,  
num histograms per ring,  
orientations per histogram



# Common operations: DAISY

Num histograms

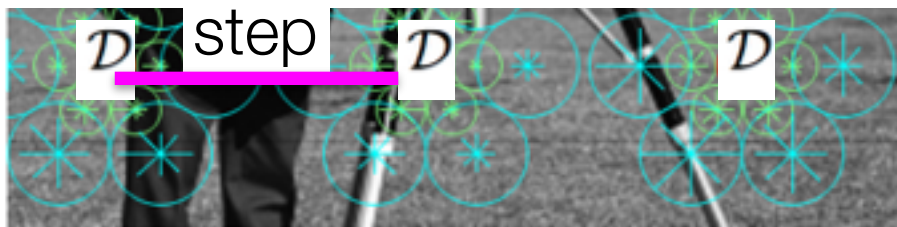


Num rings

radius



num Bag of Features Image Representation

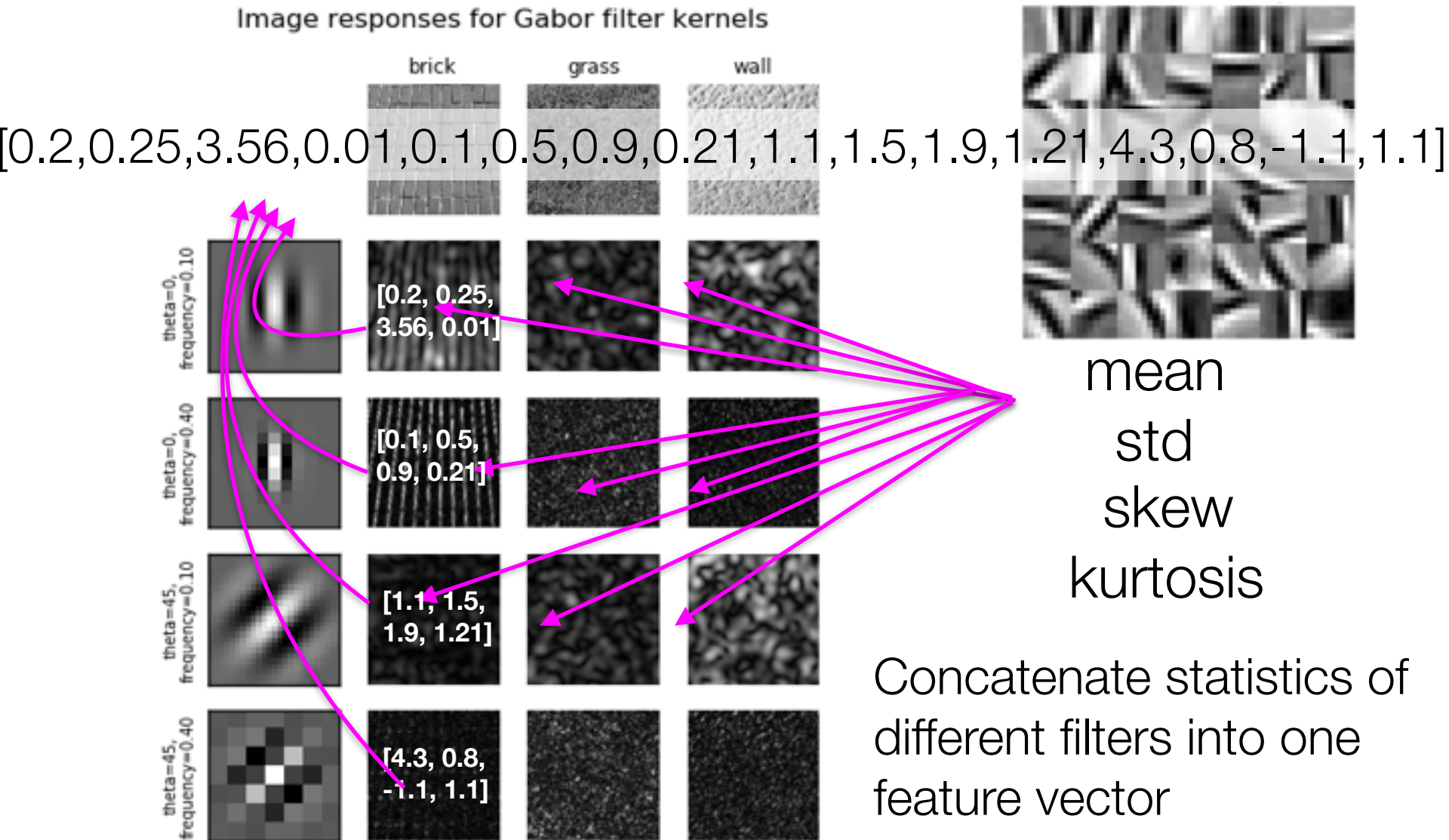


## Params:

step, radius, num rings,  
num histograms per ring,  
orientations per histogram

# Common operations: Gabor filter Banks (if time)

- common used for texture classification



## More Image Processing

Gradients

DAISY

Gabor Filter Banks

## Other Tutorials:



# For Next Lecture

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- There is no lecture next week!!
- Project work week:
  - Work on Lab One and Turn it in on Time.
- I am actually out of town (Germany)
- But email me your issues and I will try to get back when I can...