

$$\Delta^{(2)} = \sum_R \Delta_R^{(2)}$$

$$\Delta_k^{(2)} = \overbrace{-2(y^{(k)} - a_k^{(3)}) * a_k^{(3)} * (1 - a_k^{(3)})}^{k \sigma^{(3)}} \cdot a_k^{(2)} = \underbrace{\sigma^{(3)}}_{(S^{(3)} \times 1)} \cdot \underbrace{a^{(2)}}_{(1 \times S^{(2)})}$$

$$\Delta^{(2)} \text{ [redacted]} = -2(Y - A^{(3)}) * A^{(3)} * (1 - A^{(3)}) \cdot [A^{(2)}]^T \quad \boxed{\begin{matrix} S^{(3)} \times S^{(2)} \\ \text{SIZE} \end{matrix}}$$

$$A^{(2)} = \begin{bmatrix} a_1^{(2)} & a_2^{(2)} & \dots & a_k^{(2)} & \dots & a_M^{(2)} \\ 1 & 1 & & 1 & & 1 \end{bmatrix}$$

$$\Delta^{(2)} \text{ [redacted]} = \underbrace{\begin{bmatrix} \sigma_1^{(3)} & \sigma_2^{(3)} & \dots & \sigma_k^{(3)} & \dots & \sigma_M^{(3)} \\ 1 & 1 & & 1 & & 1 \end{bmatrix}}_{S^{(3)} \times M} \cdot \underbrace{\begin{bmatrix} -a_1^{(2)} \\ \vdots \\ -a_M^{(2)} \end{bmatrix}}_{M \times S^{(2)}} \quad \underbrace{\hspace{10em}}_{S^{(3)} \times S^{(2)}}$$

$$= \begin{bmatrix} \left( \sum_R \sigma_R^{(3)} a_{R1}^{(2)} \right) & \dots & \left( \sum_R \sigma_R^{(3)} a_{RS^2}^{(2)} \right) \\ \vdots & & \vdots \\ \left( \sum_R \sigma_R^{(3)} a_{RS^3}^{(2)} \right) & \dots & \left( \sum_R \sigma_R^{(3)} a_{RS^2}^{(2)} \right) \end{bmatrix}$$

So it works !!