Solutions to Reinforcement Learning by Sutton Chapter 11

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Exercise 11.1

It's generally similar with (11.6), with same treatment of the ends of episodes:

$$\mathbf{w}_{t+n} \doteq \mathbf{w}_{t+n-1} + \alpha \rho_{t:t+n-1} [G_{t:t+n} - \hat{v}(S_t, \mathbf{w}_{t+n-1})] \nabla \hat{v}(S_t, \mathbf{w}_{t+n-1})$$

$$G_{t:t+n} \doteq \sum_{k=1}^{n} \gamma^{k-1} R_{t+k} + \gamma^n \hat{v}(S_{t+n}, \mathbf{w}_{t+n-1}) \quad \text{(episodic)}$$

$$G_{t:t+n} \doteq \sum_{k=1}^{n} [R_{t+k} - \bar{R}_{t+k-1}] + \hat{v}(S_{t+n}, \mathbf{w}_{t+n-1}) \quad \text{(continuous)}$$

Exercise 11.2

It's still similar with SARSA but with the addition of a linear slider of σ .

$$\begin{aligned} \mathbf{w}_{t+n} &\doteq \mathbf{w}_{t+n-1} + \alpha \rho_{t:t+n-1} [G_{t:t+n} - \hat{q}(S_t, \mathbf{w}_{t+n-1})] \nabla \hat{q}(S_t, \mathbf{w}_{t+n-1}) \\ G_{t:h} &\doteq R_{t+1} + \gamma \Big(\sigma_{t+1} \rho_{t+1} + (1 - \sigma_{t+1}) \pi (A_{t+1} | S_{t+1}) \Big) \Big(G_{t+1:h} - Q_{h-1}(S_{t+1}, A_{t+1}) \Big) \\ &+ \gamma \bar{V}_{h-1}(S_{t+1}) \quad \text{(episodic)} \\ G_{t:h} &\doteq R_{t+1} - \bar{R}_t + \Big(\sigma_{t+1} \rho_{t+1} + (1 - \sigma_{t+1}) \pi (A_{t+1} | S_{t+1}) \Big) \Big(G_{t+1:h} - Q_{h-1}(S_{t+1}, A_{t+1}) \Big) \\ &+ \bar{V}_{h-1}(S_{t+1}) \quad \text{(continuous)} \end{aligned}$$

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Exercise 11.3

A quick solution. It's a quick and shallow solution. For better quality, one could do much better.

Exercise 11.4

Following the hint, we have:

$$\overline{\text{RE}}(w) = \mathbb{E}\left[\left(G_t - \hat{v}(S_t, w)\right)^2\right] \\
= \sum_s \mu(s) \left(G_t - \hat{v}(s, w)\right)^2 \\
= \sum_s \mu(s) \left(\left[G_t - v^*(s)\right] + \left[v^*(s) - \hat{v}(s, w)\right]\right)^2 \\
= \sum_s \mu(s) \left(\left[G_t - v^*(s)\right]^2 + \left[v^*(s) - \hat{v}(s, w)\right]^2 \\
+ 2\left[G_t - v^*(s)\right] \left[v^*(s) - \hat{v}(s, w)\right]\right)$$

since in expectation true value v* will equal to G, last term is zero

$$= \sum_{s} \mu(s) \Big([G_t - v^*(s)]^2 + [v^*(s) - \hat{v}(s, w)]^2 \Big)$$

= $\overline{VE}(w) + \mathbb{E} \Big[(G_t - v_{\pi}(S_t))^2 \Big].$