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# Dynamic deformation and failure of ultrafine-grained titanium



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#### ABSTRACT

Dynamic deformation and shear localization of ultrafine-grained ( $\sim$ 120 nm) pure titanium are examined. The strain hardening can be considered as having two regimes: below and above a strain  $\sim$ 0.04; at this point there is a drastic decrease in the slope. The strain-rate sensitivity of ultrafine-grained titanium is found to be approximately the same as its coarse grained counterpart. Based on experimentally determined parameters, the Zerilli-Armstrong equation is modified to describe the mechanical response of the ultrafine-grained titanium over the strain rate range  $10^{-5}$  to  $10^3$  s<sup>-1</sup>. Adiabatic shear banding is examined in a forced shear configuration where large strain is imposed in a narrow region. The microstructure inside the adiabatic shear band consists of a mixture of elongated grains and equiaxed nanograins ( $\sim$ 40 nm) that are significantly smaller than the initial grains ( $\sim$ 120 nm). The formation of equiaxed nanograins is modeled through a mechanism of rotational dynamic recrystallization. This further reduction in grain size from the one generated by ECAP is interpreted in terms of the Zener-Hollomon parameter for quasistatic and dynamic deformation. The adiabatic shear band eventually fractures by a combination of brittle and ductile failure.

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#### 1. Introduction

Ultrafine-grained (UFG) and nanocrystalline metals have been the subject of widespread research over the past couple of decades with significant acceleration in recent years [1]. As the name suggests, nanocrystalline materials are single or multi-phase polycrystals with nano-scale (1–100 nm) grain size. At the upper limit of this regime, the term "ultrafine grain size (UFG)" is often used (grain sizes of 100–1000 nm) [2]. Most studies on the failure behavior of UFG and nanocrystalline materials have mainly focused on the phenomena occurring under static or quasi-static loading, whereas research on dynamic properties under high strain rates is rare. Shear bands are often sites of initiation and growth for subsequent dynamic fracture [3,4].

There have been a number of investigations on the dynamic behavior of  $\alpha$ -titanium with different grain sizes. Meyers et al. [5] investigated dynamic response and shear-band formation of CP grade 2 titanium with a grain size ~72  $\mu$ m in high strain-rate plastic

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deformation. Micrograins smaller than the initial grain size were observed within the shear band and attributed to the dynamic recovery/recrystallization. Ko et al. [6] and Liu et al. [7] studied mechanical behavior of UFG pure titanium (~300 nm) and showed that it exhibited a significant improvement in yield strength with an absence of strain hardening behavior compared with coarse grained titanium. However, dynamic behavior of UFG titanium with grain size significantly below 300 nm, especially shear localization, still remains largely unexamined.

### 2. Experimental procedure

The as-received UFG pure titanium samples investigated were 200 mm long and 6 mm diameter rods processed by ECAP-C technique, according to a general procedure presented elsewhere [8,9]. The average grain size of the as-received UFG titanium was ~120 nm. The microstructure of cross-section of as-received titanium rod was observed by Lopes et al. [10] using transmission electron microscope (TEM) as shown in Fig. 1. Dynamic compression tests were performed using a split Hopkinson pressure bar (SHPB). Dynamic response and shear deformation were measured using cylindrical and hat-shaped specimens. The cylinders had a

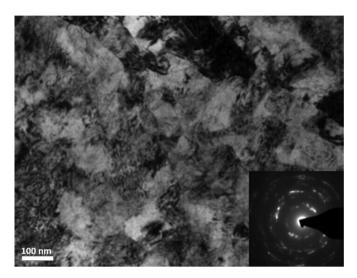


Fig. 1. TEM image of the as-received titanium rod [10].

length and diameter of 4 mm. Hat-shaped specimens were used to generate high shear strain in the "forced" localized region [11]. Fig. 2(a) illustrates their geometry and dimensions. The details and principles of this procedure are discussed by Meyers et al. [11] and have been used for the formation of adiabatic shear bands in coarse grained titanium [12].

The deformed hat-shaped samples were cut parallel to the shear band for microstructural examination. A diamond saw at a speed of 600 rpm and a feed speed of approximately 0.01 mm/s was used. The etching solution for UFG titanium was 2.5 ml HF, 3 ml HNO<sub>3</sub>, 5 ml HCl and 91 ml H<sub>2</sub>O. The shear band was examined in a Phillips XL30 scanning electron microscopy (SEM). A focused ion beam (FIB) instrument was used to accurately prepare TEM samples in the shear band regions. The FIB specimen orientation is shown in Fig. 2(b). Figs. 2(c) and (d) further show the FIB sections in samples B and C, which are perpendicular to shear band and along shear band, respectively. The specimens were characterized by TEM using a FEI Tecnai G<sup>2</sup> Polara transmission electron microscope operating at 200 kV.

#### 3. Results and discussion

#### 3.1. Mechanical properties of UFG titanium

# 3.1.1. Strain hardening and strain-rate sensitivity

Fig. 3(a) shows the room-temperature compression stress-

strain curves at different strain rates. After an initial stage of rapid strain hardening, the strain-hardening rate beyond a strain of 0.04 is significantly reduced. This is characteristic of nanocrystalline and UFG materials, which often show low strainhardening rate. Fig. 3(b) further shows that the strain-hardening rate of UFG titanium under dynamic loading follows the same trend. In contrast, the flow stress of coarse-grained polycrystalline titanium under dynamic loading continues to increase [5]. The density of dislocations in a nanocrystalline metal saturates due to dislocation annihilation at grain boundaries. UFG Ti thus loses its defect accumulation ability and hence the capacity for strain hardening. However, dislocations are still the carriers of plastic deformation until the grain size is in the range of 10-15 nm. Flat compression curves have been observed for UFG pure titanium made by ECAP [13]. Elias et al. [14] also reported a low strainhardening rate for UFG titanium having a grain size ~200 nm after a strain of 0.05.

The strain-rate dependence of the yield stress for two grain sizes (72  $\mu$ m and 120 nm) is shown in Fig. 3(c). The strain-rate sensitivity, defined as  $m=\partial\log\sigma/\partial\log\varepsilon$ , is 0.027 between  $10^{-4}$  s<sup>-1</sup> and  $10^3$  s<sup>-1</sup> for both UFG titanium and coarse-grained titanium [5,15]. At the higher strain-rate, there is an increase in m. The activation volume parameter concept provides insight into the deformation mechanisms [16]. It is expressed as:

$$v^* = \frac{kT}{m\sigma_v} \tag{1}$$

where T is the temperature,  $\sigma_y$  is the yield stress, and k is Boltzmann constant. It can be seen from Eqn. (1) that the activation volume  $v^*$  is inversely proportional to both the strain-rate sensitivity and yield stress. The yield stress of UFG titanium is approximately twice that of coarse-grained CP titanium. The activation volume of UFG pure titanium is  $\sim 6b^3$ , where b=0.289 nm is the Burgers vector in hexagonal titanium. This represents a significant reduction in the activation volume, compared with  $80b^3$  for coarse-grained CP titanium [10], suggesting a change in the rate controlling mechanism. The influence of the cutting of forest dislocations decreases for UFG materials. This results in a decrease of the activation volume related to its low strain-hardening response.

#### 3.1.2. Constitutive response

Zerilli and Armstrong [17,18] developed physically-based constitutive equations based on the general mechanical responses for fcc, bcc and hcp metals. The Zerilli-Armstrong equation is based on the framework of thermally-activated dislocation motion, where both the work hardening and strain-rate sensitivity are influenced by the temperature. This equation was applied by Meyers et al. [19]

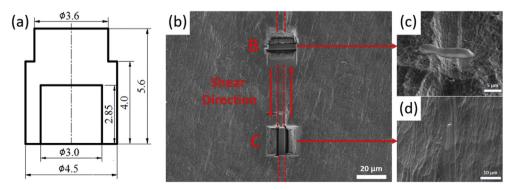
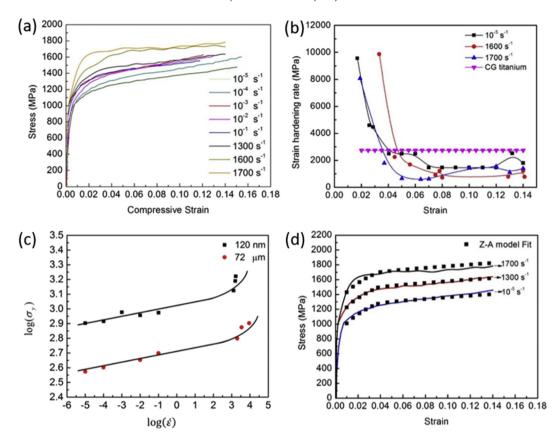


Fig. 2. (a) Schematic configuration of the hat-shaped specimen (Dimensions in mm). (b) SEM images of FIB positions. (c) Sample B position perpendicular to the shear band. (d) Sample C position along the shear band. (The edges of the shear band marked by red lines). (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)



**Fig. 3.** (a) Stress-strain relationships of UFG titanium cylindrical samples at different strain rates [10]. (b) Strain-hardening rate as a function of strain [5]. (c) Strain-rate sensitivity of coarse grained titanium [5] and UFG titanium [10]. (d) Stress-stress relationship and Zerilli-Armstrong constitutive equation fit to experimental results at strain rates 10<sup>-5</sup> s<sup>-1</sup>, 1300 s<sup>-1</sup> and 1700 s<sup>-1</sup>.

to describe the mechanical response of hexagonal materials and is modified below to account for two regimes:

$$\sigma = \begin{cases} \sigma_{G} + k_{s}d^{-1/2} + C_{1}\left(\frac{\dot{\epsilon_{0}}}{\dot{\epsilon}}\right)^{-C_{3}T} + \frac{C_{2}}{e^{-C_{4}T}}\varepsilon^{n_{1}}, \varepsilon \in (0, \varepsilon_{0}) \\ \sigma_{G} + k_{s}d^{-1/2} + C_{1}\left(\frac{\dot{\epsilon_{0}}}{\dot{\epsilon}}\right)^{-C_{3}T} + \frac{C_{2}}{e^{-C_{4}T}}\varepsilon^{n_{1}}_{0} + \frac{C_{5}}{e^{-C_{4}T}}(\varepsilon - \varepsilon_{0})^{n_{2}} \end{cases}$$
(2)

where  $\sigma_G$  represents the athermal part of the stress required for plastic deformation. The second term in the right-hand side represents the Hall–Petch relationship (also considered athermal). The third and fourth terms represent the increase of the yield stress related to an increase of strain rate  $\varepsilon$  and plastic strain  $\varepsilon$  (thermal part). As discussed, in the first stage of plastic deformation, for a strain less than 0.04, dislocations are still the carriers of plastic deformation for the UFG titanium. For the nearly zero post-yield work-hardening range ( $\varepsilon \geq 0.04$ ), the experimentally determined parameters, the  $C_5$  and  $n_2$ , are changed to describe low strain hardening ability. This provides the fifth term. For UFG titanium,  $\sigma_G = 0$  MPa,  $k_S = 6$  MPa mm<sup>-1/2</sup> [2],  $C_1 = 420$  MPa,  $C_2 = 2200$  MPa,  $C_3 = 8.05 \times 10^{-3}$  K<sup>-1</sup>,  $C_4 = 6.8 \times 10^{-4}$  K<sup>-1</sup>,  $C_5 = 655$  MPa,  $\varepsilon_0 = 1700$  s<sup>-1</sup>,  $n_1 = 0.33$  and  $n_2 = 0.8$ . The validity of the constitutive equations is further assessed by comparing the experimental and predicted results in Fig. 3(d).

# 3.2. Adiabatic shear band formation and failure

# 3.2.1. Mechanical response and temperature rise in adiabatic shear band

The thermal softening associated with the plasticity-induced temperature rise may lead to shear localization [20]. The hat-shaped samples H-1, (with maximum displacement of 1 mm) and H-2 (with maximum displacement of 1.15 mm) were loaded at different stresses. The formation of adiabatic shear band in sample H-1 is discussed first; the flow stress versus strain in the ASB is shown in Fig. 4(a). In the first stage (A-B), the shear stress increases with shear strain due to strain hardening and strain-rate hardening. When the stress reaches the maximum value of 650 MPa, it begins to fluctuate due to the competition between strain hardening, strain-rate hardening and thermal softening; this is the second stage (B-C). In the third stage (C-D), when thermal softening is larger than strain hardening and strain-rate hardening, the stress decreases sharply and an ASB is generated in the specimen.

Assuming adiabatic heating, it is possible to estimate the temperature rise within the shear band. Taking into account that a fraction  $\beta$  of the work done is converted into heat, the following equation for the conservation of energy holds [20]:

$$\rho \cdot C_p \cdot dT = \beta \cdot \sigma \cdot d\varepsilon \tag{3}$$

where  $\rho$  is the density of the material,  $C_P$  is the specific heat capacity, T is the temperature,  $\sigma$  is the true stress and  $\varepsilon$  is the strain. The temperature rise is:

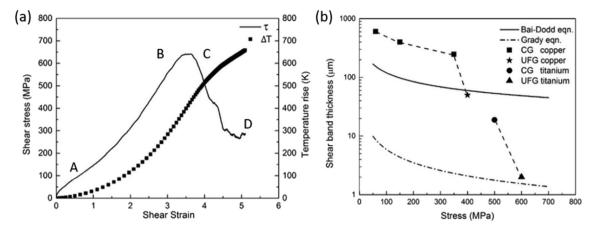


Fig. 4. (a) Shear stress versus shear strain in hat-shaped sample with maximum displacement of 1 mm deformation and corresponding temperature rise. Shear stress-shear strain has three stages: (A—B) flow stress increases with strain due to strain hardening and strain-rate hardening, (B—C) strain hardening, strain-rate hardening and thermal softening compete, (C—D) thermal softening dominates hardening and the shear band is formed. (b) Shear band thickness of copper and titanium with different grain sizes obtained from experiments [5,24] as compared with predicted equations by Bai and Dodd [21] and Grady [22,23].

$$\Delta T = \frac{\beta}{\rho \cdot C_p} \int_{\epsilon_n}^{\epsilon_e} \sigma d\epsilon \tag{4}$$

The initial conditions are  $\varepsilon_s = 0$  and T = 293 K;  $\beta = 0.9$ ,  $C_p = 523$  J/(kg K), and  $\rho = 4500$  kg/m<sup>3</sup>. The temperature increase as a function of the shear strain in the shear band for UFG titanium is shown in Fig. 4(a). The recrystallization temperature T = 900K  $\approx 0.46$   $T_m$  can be reached at a shear strain  $\sim$ 4.5 (This is obtained by converting the normal strain into shear strain).

#### 3.2.2. Width and susceptibility of formation of shear band

A theoretical shear-band thickness equation was obtained by Bai and Dodd [21]:

$$\delta = 2 \left( \frac{\lambda T}{\tau \dot{\gamma}} \right)^{1/2} \tag{5}$$

where  $\lambda = 20 \text{ W(m K)}^{-1}$ , T = 900 K, and  $\dot{\gamma} = 5 \times 10^4 \text{ s}^{-1}$ .  $\lambda$ , T,  $\dot{\gamma}$  and  $\tau$  are the thermal conductivity, temperature, shear strain rate and shear stress inside the shear band, respectively. Grady [22,23] proposed an alternative equation:

$$\delta = \left(\frac{16\rho^3 C_p^2 \chi^3}{\tau^3 \alpha^2 \dot{\gamma}}\right)^{1/4} \tag{6}$$

where  $\alpha$  is the thermal softening parameter, and  $\chi$  is thermal diffusivity coefficient. For UFG titanium,  $\rho=4500~{\rm kg/m^3}$ ,  $\chi=\lambda/(\rho\cdot C_p)=8.5\times 10^{-6}~{\rm m^2/s}$ ,  $C_p=523~{\rm J/(kg\cdot K)}$ ,  $\dot{\gamma}=5\times 10^4~{\rm s^{-1}}$  and  $\alpha=-(1/\sigma_y)\cdot\partial\sigma/\partial T=0.002~{\rm [10]}$ . Fig. 4(b) shows predictions from the above equations and the experimentally measured shear band thickness of UFG and coarse-grained titanium; the shear-band thickness measured from Fig. 2(b) is only ~2 µm. Mishra et al. [24] reported that there was a large drop of shear-band thickness for UFG copper compared with its coarse grained counterpart. The reason for this difference is considered to be the increased propensity to thermal softening in ECAP samples. Although both the Bai-Dodd and Grady equations predict a decrease in band thickness with increasing flow stress, the precipitous drop for the UFG titanium must be attributed to an additional mechanism for the loss of mechanical stability. Guo et al. [25] reported that the thermal conductivity of nanocrystalline titanium with a grain size less than

100 nm is 5.2 (m K) $^{-1}$ , which is only about one fourth that of the coarse-grained titanium 20 (m K) $^{-1}$ . The thermal softening parameter of UFG titanium is twice that of coarse-grained titanium [5,10]. From Equations (5) and (6), the decrease of thermal conductivity parameter  $\lambda$  and increased thermal softening parameter  $\alpha$  explain the decrease in shear-band thickness compared with coarse grained titanium.

A quantitative description of the susceptibility to adiabatic shear banding (ASB),  $\chi_{SB}$ , by Wright [26,27], has the following form:

$$\frac{\chi_{SB}}{a/m} = \min\left\{1, \frac{1}{n/m + \sqrt{n/m}}\right\} \tag{7}$$

where a is a nondimensional thermal softening parameter defined by  $a = (-\partial \sigma/\partial T)/\rho C_p$ , n is the strain hardening exponent and m is the strain-rate sensitivity. For a perfectly plastic material (no strain hardening), the susceptibility reduces to:

$$\chi_{SB} = \frac{a}{m} = \frac{\alpha \sigma_y}{\rho C_p m} \tag{8}$$

where  $\alpha=0.002~{\rm K}^{-1}$  is the thermal softening parameter evaluated under isothermal conditions and  $\sigma_y$  is the yield strength [5]. The susceptibility to ASB of the UFG titanium can thus be estimated to be  $\sim 30$  using the following parameters:  $\sigma_y=0.97~{\rm GPa}$ , m=0.027 [10]. For the coarse grained titanium,  $\sigma_y=0.4~{\rm GPa}$ ,  $\alpha=0.001{\rm K}^{-1}$ , and m=0.027 [5] result in a susceptibility to ASB of  $\sim 6$ , five times lower than that for the UFG Ti. A similar increase in susceptibility to shear localization of UFG Fe was also reported by Wei et al. [28].

#### 3.2.3. Examination of the microstructure

TEM was carried out on the samples B and C to study microstructural features of the shear bands. Fig. 5(a) provides an overall view of sample B (the shear band lies between the blue lines). The microstructures within and outside the shear band are quite distinct. The continuous sharp diffraction ring pattern indicates that the microstructure is randomly oriented, with no strong texture. Lins et al. [29] showed that the shear band in an interstitial-free steel displays a strong heterogeneous character from the center of the shear band to its edges. Fig. 5(b) shows both the nominally equiaxed UFG matrix and abnormally grown coarse grains with low dislocation density (see arrow). The abnormal grain growth is due to the temperature rise near and in the shear band and the thermal

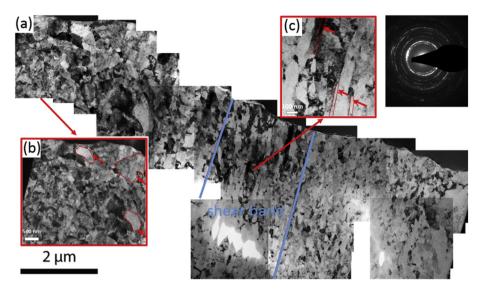


Fig. 5. TEM images of the microstructure (a) of the sample B (perpendicular to shear band), (b) near the shear band, (c) inside the shear band. (Shear direction nominally perpendicular to the foil; misorientation is possible).

instability of the UFG titanium. The elongated grains, which were less severely deformed, were formed along the edge of the shear band. Fig. 5(c) shows a mixture of elongated and equiaxed grains inside the shear band. The grain boundaries are clearly delineated. The thickness of the elongated grains varies, which may be due to the inhomogeneous shear stress distribution inside the shear band. Some very narrow elongated grains (see arrow) are formed, which may further break down to form nanograins upon further deformation. This evolution process was described in several studies [5,11]. Fig. 6(a) shows the microstructure of sample C. It shows the randomly distributed nanostructured grains. The dark-field image of Fig. 6(b) shows that the nanograins tend to flow in one direction (shown by arrows) under shear deformation inside the shear band. Fig. 6(c) highlights a high magnification image of a nanograin with grain size ~40 nm, corresponding to the breakdown of the narrow elongated grains as detailed in Fig. 5(c).

In Fig. 5, the FIB cutting direction is perpendicular to the shear band; therefore, the sample is only partially in the shear band (shown between two blue lines). The matrix of UFG titanium can also be seen. Both elongated UFG grains and recrystallized

nanosized grains can be observed. Fig. 6, on the other hand, only shows the microstructure right in the middle of the shear band, since the FIB cutting direction is parallel to the shear band. Only fully recrystallized nanograins are seen. The temperature rise in the middle of the shear band is higher than that at its edges, providing more thermal energy to form recrystallized equiaxed nanograins. Different applied shear strains and inhomogeneous temperature distribution occur during the formation of the shear band, as demonstrated by finite element simulation of formation and failure of the shear band [30]. This leads to different shear direction and different microstructures in different regions as shown in Figs. 5 and 6. As indicated by the TEM diffraction ring patterns in Figs. 5 and 6, the recrystallized grains are nearly randomly distributed, and do not show strong texture inside the shear band.

3.2.4. Modeling of microstructural evolution inside the shear band Meyers et al. [31], and Hines and Vecchio [32] demonstrated that migrational recrystallization could not account for the grains generated inside the shear band and proposed complementary rotational recrystallization mechanisms. Whereas Meyers et al.

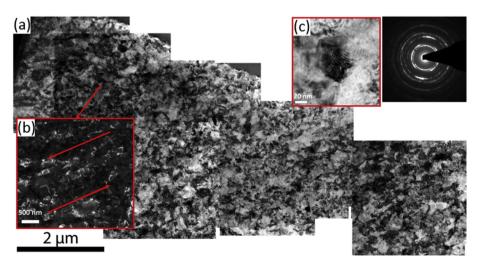


Fig. 6. TEM images of (a) the microstructure of the sample C (inside shear band), (b) the dark-field microstructure, (c) the equiaxed grains. (Shear direction indicated in dark-field micrograph (b)).

[31,33] used a dislocation energetics approach, Hines and Vecchio [32] and Hines et al. [34] implemented a continuum mechanics analysis. The sequence of events shown in Fig. 7 leading to the formation of equiaxed nanograins is expected to occur. The formation of elongated grains is due to the dislocation motion instead of dynamic recrystallization. In essence, the equiaxed grains shown in Fig. 7(a) are deformed into elongated grains as shown in Fig. 7(b). Fig. 7(c) shows that dislocations are accumulated in subgrain boundaries inside the elongated grains. The elongated grains then break up to finer subgrains. Once the elongated subgrains are achieved, further break-up by dislocation generated at the grain boundaries is due to geometrically-necessary dislocations required to accommodate further plastic deformation. The relaxation of elongated subgrains into an equiaxed crystalline structure can occur by minor rotations of the grain boundaries in Fig. 7(d).

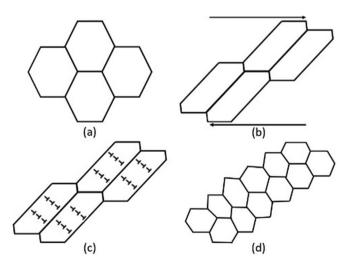
According to the rotational dynamic recrystallization mechanism, the formation of a new grain requires local grain-boundary segments to tilt about  $30^{\circ}$  during the last stage of the deformation process (from Fig. 7(c) to d) [33]. The time needed for these processes is given by:

$$t = \frac{LkTf(\theta)}{4\delta\eta D_{b0} \exp(-Q_b/RT)}$$
 (9)

where t is time, L is the average subgrain diameter,  $\delta$  is grain-boundary thickness,  $\eta$  is the grain boundary energy,  $D_{b0}$  is a constant related to grain boundary diffusion,  $Q_b$  denotes the activation energy for grain boundary diffusion,  $\theta$  is the subgrain misorientation, and  $f(\theta)$  can be described as follows:

$$f(\theta) = \frac{3\tan(\theta) - 2\cos(\theta)}{3 - 6\sin(\theta)} + \frac{2}{3} - \frac{4\sqrt{3}}{9}\ln\frac{2 + \sqrt{3}}{2 - \sqrt{3}} + \frac{4\sqrt{3}}{9}\ln\frac{\tan(\theta) - 2 - \sqrt{3}}{\tan(\theta) - 2 + \sqrt{3}}$$
(10)

For UFG titanium,  $\delta = 1.5 \times 10^{-9}$  m,  $\eta = 0.675$  J/m²,  $D_{b0} = 1.4 \times 10^{-3}$  m²/s,  $Q_b = 151$  kJ/mol,  $k = 1.38 \times 10^{-23}$  J/K, R = 8.314 J/(K·mol),and T = 900 K [35–37]. The kinetic curve for the rotational dynamic recrystallization mechanism in a shear band can be obtained by incorporating the parameters into Eqns. (9) and



**Fig. 7.** Schematic illustration of microstructural evolution inside the shear band: (a) randomly distributed equiaxed grains; (b) formation of elongated grains through plastic deformation (shear direction indicated by arrows); (c) dislocation accumulation forming subgrain boundaries; (d) breakup of elongated grains, reorientation of grain boundaries and formation of equiaxed nanosized grains.

(10), as shown in Fig. 8(a) and (b). A decrease in the activation energy for grain-boundary diffusion [10] and increase of grainboundary thickness [35] accelerate the formation of equiaxed grains by the grain-boundary diffusion process. In Fig. 8(a), the nanograin size, L, is varied from 40 nm to 100 nm at  $T = 900 \text{ K} \approx 0.46 T_m$ . Fig. 8(b) indicates that the increase of temperature helps the grain-boundary diffusion process. The rate of rotation decreases with increasing angle and asymptotically approaches 30° as  $t \to \infty$ . The calculations predict significant rotations of the boundary within the deformation time. Thus, rotational recrystallization can also take place during plastic deformation  $(2 \times 10^{-4} \text{ s})$ . This does not exclude the possibility of further coalescence of nanograins inside the shear band. Since the deformation mechanisms in nanocrystalline titanium are different from the ones in coarse-grained titanium, the discussion below provides deeper insight into the formation of nanograins inside the shear hand

3.2.4.1. Grain boundary mobility. The driving force for the migration of a grain boundary can be simply estimated by equating the force acting on a curved segment of the boundary, dS, due to the grain-boundary energy  $\eta = 0.675$  J/m<sup>2</sup> [37]. Assuming a two-dimensional geometry, for simplicity, the total force acting on the grain boundary in the y-direction (seen in Fig. 8(c)) is:

$$F = 2\eta \sin \frac{d\theta}{2} \approx \eta d\theta \tag{11}$$

Therefore.

$$force/area = \frac{\eta d\theta}{Rd\theta} = \frac{\eta}{R}$$
 (12)

The velocity of the grain boundary is proportional to the force acting on the segment *dS*:

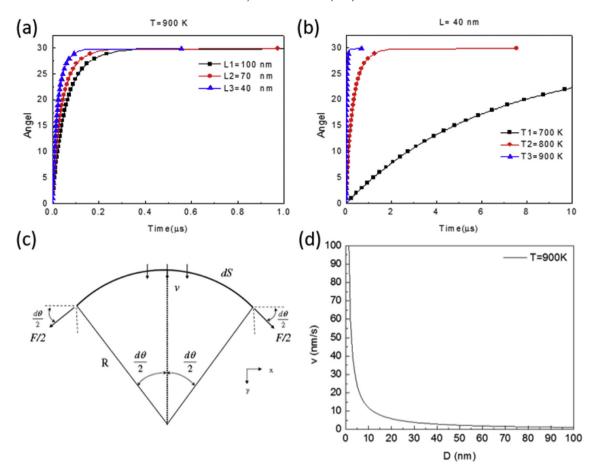
$$\nu \propto \frac{\eta}{R} = M \frac{\eta}{R} \tag{13}$$

where *M*, the grain boundary mobility, has an Arrhenius-type temperature dependence [38]:

$$M = M_0 \exp\left(\frac{-Q_m}{RT}\right) \tag{14}$$

For titanium [39],  $M_0 = 4.3 \times 10^{-6}$  m<sup>4</sup>/J/s and  $Q_m = 179$  kJ/mol. Grain-boundary velocity is plotted against the grain size at 900 K in Fig. 8(d). For a grain size of 40 nm (v = 6 nm/s), a grain boundary movement of 6 nm at 900 K can be expected in 1 s. This cannot be sufficient to reorganize the deformed grain configuration. For a shear band, the cooling takes place in time scales of fractions of milliseconds. For 0.2 ms and a grain size of 40 nm, a displacement of  $1.2 \times 10^{-3}$  nm is obtained. Thus, the calculation shows that no significant grain growth by grain-boundary migration takes place after a nanocrystalline size of 40 nm is reached. However, growth of equiaxed nanograins might occur by grain rotation during shear deformation inside the band.

3.2.4.2. Zener-Hollomon parameter and grain refinement. Mishra et al. [24] reported that the similarity of structure evolution in SPD and shear-band formation is related to the hypothesis that both processes are regulated by a similar mechanism with two significant differences: the time is shorter and temperature is higher in shear-band formation. The Zener-Hollomon (ZH) parameter is defined as [40]:



**Fig. 8.** Angle of rotation of grain boundary during the deformation process as a function of time for (a) different grain sizes (40, 70, and 100 nm) at T = 900 K and (b) different temperatures (700, 800, and 900 K) for grain size L = 40 nm. (c) Schematic showing force acting on the grain boundary with radius of curvature R. (d) Grain-boundary velocity as a function of radius R typical of shear band deformation process at 900 K.

$$Z = \dot{\varepsilon} \exp\left(\frac{Q_d}{RT}\right) \tag{15}$$

where R is the gas constant and  $Q_d$  is the related activation energy for deformation. At a constant Z, the resultant grain size in SPD and dynamic deformation is the same; this is clear from the opposing effects of  $\dot{\varepsilon}$  and T in Eqn. (15). Li et al. [41] reported that finer copper grains were formed in deformation at a temperature of 77 K at high strain rates, on the order of  $10^2$  s<sup>-1</sup>, than under quasi-static conditions. This increased the ZH parameter of the process and consequently decreased the resulting grain size. Extending the proposal of Mishra et al. [24], they reported that the recrystallized grain size was inversely related to the ZH parameter.

In fact, a different grain refinement mechanism inside the shear band for nanocrystalline titanium may operate at the high Zener-Hollomon parameter deformation conditions. For nanocrystalline titanium, as grain size decreases, an increasing amount of grain-boundary sliding can occur. Using MD simulation, Schiøtz et al. [42] reported that grain-boundary sliding dominates the plastic deformation instead of dislocation motion, due to the larger volume fraction of grain boundaries when the grain size is under 10 nm. Thus, with further increase of the ZH parameter, the grain size inside the shear band may reach a steady-state value of several nanometers, where most plastic deformation is due to grain-boundary sliding instead of dislocation motion.

#### 3.2.5. Fracture of adiabatic shear band

The formation of an ASB precedes the failure mechanisms by void and crack formation. Xue et al. [43] observed both elongated and equiaxed voids that preceded failure of the shear band. Both morphologies are observed inside the shear bands, depending on how the separation of the two parts occurs. If only tension is applied, the two parts separate by forming voids in the shear band; these voids grow until their diameters reach the band thickness. The elongated dimples are a characteristic of shear failure, due to elongated and coalesced voids. The formation of elongated voids when the failure has a strong shear component is explained by Meyers and Chawla [44].

Fig. 9(a) shows a microvoid in sample H-1 between the shear band and its surrounding; this indicates that microvoids can be nucleated at the edge of the shear band. Fig. 9(b) shows the ductile ligaments (see arrow) along the shear band in sample H-1. The ductile ligaments indicate the coalescence of microvoids. The shear failure surface of the sample H-2 (which underwent a higher strain than H-1) was observed by SEM shown in Fig. 9(c). The fracture surface contains both ductile features such as dimples, and brittle features such as cleavage patterns, indicating that brittle and ductile fracture modes might take place simultaneously. A microstructure consisting of elongated dimples, shows similar characteristics to other HCP materials such as Re, Hf and Ti-6Al-4V alloy [45]. The coalescence of voids, leading to cracks, was observed along the shear band in rhenium in high-strain-rate deformation [46]. Similar elongated shear dimples were observed in the fracture

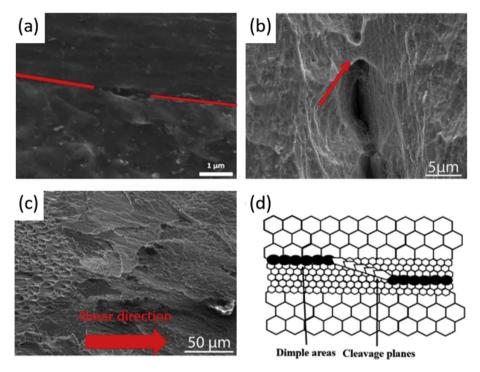


Fig. 9. SEM images of the sample H-1 with maximum-displacement 1 mm (a) the dimple along the shear band, (b) alignment between dimples and fracture surface, and of the sample H-2 with maximum-displacement 1.15 mm (c) ductile areas and cleavage plane. (d) Schematic illustration of ASB failure of UFG titanium.

surface of polycrystalline hafnium [47].

A schematic illustration of ASB fracture is shown in Fig. 9(d). Microvoids can be nucleated inside shear band or at its edges, followed by their coalescence and the formation of microcracks; this leads to the formation of a mixture of ductile and brittle failure. The formation of cracks between sheets of dimples along the shear band can lead to more rapid fracture of the ASB and a more brittle fracture.

#### 4. Conclusions

The present investigation addressed the dynamic deformation, adiabatic shear-band formation, and failure mechanism of ultrafine-grained (grain size ~120 nm) titanium. The conclusions are as follows:

- (1) The flow stress of UFG titanium at different strain rates is described by a modified Zerilli-Armstrong constitutive equation. After an initial stage of rapid stress rise, the strain hardening beyond a strain of 0.04 is considerably lower. The strain-rate sensitivity of UFG titanium is similar to the one in coarse-grained CP titanium.
- (2) The width of the shear band formed by forced shear stress in UFG titanium is about 2  $\mu$ m, which is significantly lower than that of coarse-grained (72  $\mu$ m) CP titanium. Lower strain hardening, lower thermal conductivity and higher thermal softening make UFG titanium more sensitive to shear localization and lead to the decrease in the width of the shear band.
- (3) Randomly oriented nanograins were observed inside the shear band. The equiaxed nanograins, which are under 100 nm, are generated inside the shear band by a mechanism of rotational dynamic recrystallization.
- (4) The basic equations of rotational dynamic recrystallization are applied to the nanograins and it is demonstrated that the

- grain boundaries can undergo 30° rotation during deformation, thus enabling a steady-state process, in which the equiaxed structure is retained.
- (5) The adiabatic shear band eventually fractures by a combination of brittle and ductile failure. The microvoids can be nucleated both inside the shear bands and at their edges, followed by their coalescence and crack formation linking them. The formation of cracks along the shear band can lead to more rapid failure of the ASB and a more brittle fracture.

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