Change point detection in Python with ruptures

Digital French-German Summer School with Industry 2020

Charles Truong¹

¹Centre Borelli Université Paris-Saclay ENS Paris-Saclay, CNRS

Wednesday 24th June







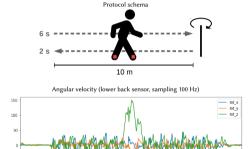




- ▶ Change point detection is a common task when dealing with non-stationary time series.
- Application example: automatic diagnosis of neurologically impaired patients [Truong et al., 2019a].

Healthy and pathological subjects underwent a fixed protocol:

- standing still,
- walking 10m,
- turning around,
- walking back,
- standing still.



1000

1500

2000

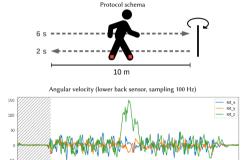
Can also be applied to finance, industrial monitoring, public health monitoring, etc. [Truong et al., 2020].

son

- ▶ Change point detection is a common task when dealing with non-stationary time series.
- Application example: automatic diagnosis of neurologically impaired patients [Truong et al., 2019a].

Healthy and pathological subjects underwent a fixed protocol:

- standing still,
- walking 10m,
- turning around,
- walking back,
- standing still.



1000

1500

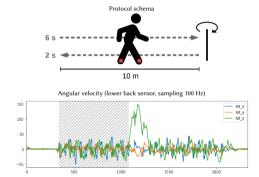
2000

Can also be applied to finance, industrial monitoring, public health monitoring, etc. [Truong et al., 2020].

- ▶ Change point detection is a common task when dealing with non-stationary time series.
- Application example: automatic diagnosis of neurologically impaired patients [Truong et al., 2019a].

Healthy and pathological subjects underwent a fixed protocol:

- standing still,
- walking 10m,
- turning around,
- walking back,
- standing still.

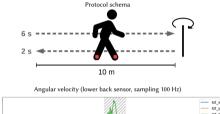


Can also be applied to finance, industrial monitoring, public health monitoring, etc. [Truong et al., 2020].

- ▶ Change point detection is a common task when dealing with non-stationary time series.
- Application example: automatic diagnosis of neurologically impaired patients [Truong et al., 2019a].

Healthy and pathological subjects underwent a fixed protocol:

- standing still,
- walking 10m,
- turning around,
- walking back,
- standing still.



1000

1500

2000



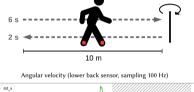
150

son

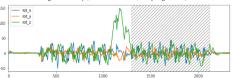
- ▶ Change point detection is a common task when dealing with non-stationary time series.
- Application example: automatic diagnosis of neurologically impaired patients [Truong et al., 2019a].

Healthy and pathological subjects underwent a fixed protocol:

- standing still,
- walking 10m,
- turning around,
- walking back,
- standing still.



Protocol schema

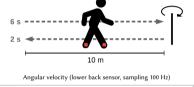


Can also be applied to finance, industrial monitoring, public health monitoring, etc. [Truong et al., 2020].

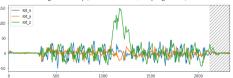
- ▶ Change point detection is a common task when dealing with non-stationary time series.
- Application example: automatic diagnosis of neurologically impaired patients [Truong et al., 2019a].

Healthy and pathological subjects underwent a fixed protocol:

- standing still,
- walking 10m,
- turning around,
- walking back,
- standing still.



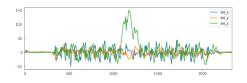
Protocol schema

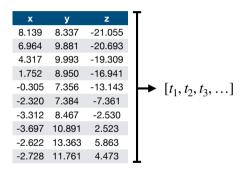


Can also be applied to finance, industrial monitoring, public health monitoring, etc. [Truong et al., 2020].

What is change point detection?

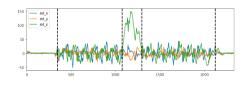
- ▶ Change point detection consists in finding the temporal boundaries between homogeneous time periods.
- ► Informally: "multivariate signal —> list of change point indexes"

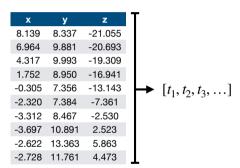




What is change point detection?

- ▶ Change point detection consists in finding the temporal boundaries between homogeneous time periods.
- ▶ Informally: "multivariate signal → list of change point indexes"





ruptures: a Python library



Github page (github.com/deepcharles/ruptures)



Selective review of offline change point detection methods

```
Charles Truong <sup>3</sup>, Laurent Oudre A<sup>5</sup>89, Nicolas Vayatis <sup>3</sup>

Show more 

https://doi.org/10.1016/j.sigpro.2019.107299 Get rights and content
```

Associated publication [Truong et al., 2020]



Documentation



How to install

Links and information on the Github page.

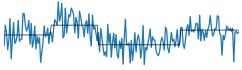
Table of contents

- Introduction
- 2. What is change point detection?
- 3. General principle of ruptures
- ruptures in action
 A simple example
 Gait analysis
- Supervised change point detection General principle Deep detection
- 6. Conclusior

General principle

ruptures: a Python library

How to choose a segmentation?



$$\mathcal{T}{=\{t_1,t_2,t_3\}}$$

$$V(T) = c(y_{0..t_1}) + c(y_{t_1..t_2}) + c(y_{t_2..t_3}) + c(y_{t_3..T})$$

Problem 1.

Fixed number K of change points:

$$\widehat{\mathcal{T}} := \underset{\mathcal{T}}{\operatorname{arg \, min}} \ V(\mathcal{T}) \quad \text{s.t.} \ |\mathcal{T}| = K.$$

The "best segmentation" is the minimizer, denoted \widehat{T} , of a criterion V(T):

$$V(\mathcal{T}) := \sum_{k=0}^K c(y_{t_k \dots t_{k+1}}).$$

Cost example: $c(y) = \sum_t (y_t - \bar{y})^2$.

Problem 2.

Unknown number of change points:

$$\widehat{\mathcal{T}} := \operatorname*{arg\;min}_{\mathcal{T}} V(\mathcal{T}) + \operatorname{pen}(\mathcal{T})$$

where pen(\mathcal{T}) measures the complexity of a segmentation \mathcal{T} .

General principle

ruptures: a Python library

Detection methods are the combination of three elements [Truong et al., 2020].

Cost function

Search method

Constraint

Criterion $V(\mathcal{T})$ to minimize: $V(\mathcal{T}) := \sum_{k=0}^{K} \frac{c(y_{t_k..t_{k+1}})}{c(y_{t_k..t_{k+1}})}$.

Problem 1.

Fixed number *K* of change points:

$$\widehat{\mathcal{T}} := \begin{array}{c|c} \operatorname{arg\ min} & V(\mathcal{T}) \end{array}$$
 s.t. $|\mathcal{T}| = K$

Problem 2.

Unknown number of change points:

$$\widehat{\mathcal{T}} := \left[egin{argain}{c} \operatorname{arg\ min} \\ \mathcal{T} \end{array}
ight] V(\mathcal{T}) \ + \left[\operatorname{pen}(\mathcal{T}) \right]$$

where pen(\mathcal{T}) measures the complexity of a segmentation \mathcal{T} .

General principle

ruptures: a Python library

A modular architecture.

```
First import and data loading.
[3191:
           import ruptures as rpt
          signal = get signal(...) # user defined
         1 # cost function
                                                                             Choosing the cost function
[3291:
         2 c = rpt.costs.CostL2()
                                                                             Here, c(y) = \sum_t (y_t - \bar{y})^2.
                                                                             Choosing the search method
         1 # search method
[330]:
         2 algo = rpt.Binseg(jump=5, min size=10, custom cost=c)
                                                                             Here, binary segmentation.
                                                                             Fitting the algorithm.
[331]: 1 # fit algo
         2 algo.fit(signal)
                                                                             Choosing the constraint
[332]: 1 # predict change points
         2 # fixed number of changes
                                                                             Then detecting the change points ("predict").
         3 bkps = algo.predict(n bkps=10)
         4 # or penalized detection
         5 bkps = algo.predict(pen=50)
                                                                             Measuring the detection accuracy.
         1 from ruptures.metrics import hausdorff
[3331:
           error = hausdorff(true bkps, bkps)
```

Table of contents

- 1. Introduction
- 2. What is change point detection?
- 3. General principle of ruptures
- 4. ruptures in action A simple example Gait analysis
- Supervised change point detection General principle Deep detection
- 6. Conclusior

A simple example

ruptures in action

Import and generate signal [91]: import ruptures as rpt signal, bkps = rpt.pw_normal(n_samples=500) 300 200

Choose a method and detect change points

```
[130]: 1  # cost for multivariate Gaussian
2  cost = rpt.costs.CostNormal()
3  # search method: binary segmentation
4 algo = rpt.Binseg(custom_cost=cost)
5  # fit
6 algo.fit(signal)
7  # predict
8  prediction = algo.predict(3)
9  # print results
10  print(f"True change points:\t\t(bkps)")
11  print(f"Treedicted change points:\t(orediction)")
```

True change points: [123, 246, 369, 500]
Predicted change points: [120, 245, 370, 500]

Measure accurary

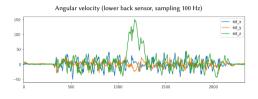
[143]: 1 from ruptures.metrics import hausdorff print(hausdorff(bkps, prediction))

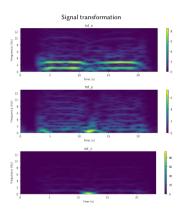
3.0

Gait analysis

ruptures in action

- ▶ To simplify the detection task, the signal is transformed (here, short-term Fourier transform).
- ► Then mean-shifts are detected.

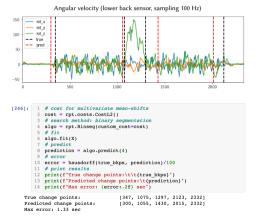




Gait analysis

ruptures in action

- ▶ To simplify the detection task, the signal is transformed (here, short-term Fourier transform).
- Then mean-shifts are detected.



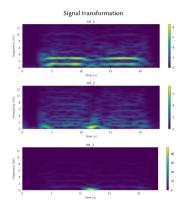


Table of contents

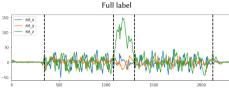
- 1. Introduction
- 2. What is change point detection?
- 3. General principle of ruptures
- 4. ruptures in action A simple example Gait analysis
- 5. Supervised change point detection General principle Deep detection
- 6. Conclusior

Supervised change point detection

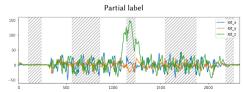
General principle

▶ How to integrate expert knowledge to calibrate the change point detection? [Truong et al., 2019b]

The expert provides the target segmentation: either full or partial label.



The exact change point locations are provided.



Only homogeneous periods (hatched areas) are provided (weakly supervised).

Labels are transformed into constraints. Intuitively, the problem is:

Learn a transformation Ψ such that $d(\Psi(x_t), \Psi(x_s)) \leq u$ if x_t and x_s similar $d(\Psi(x_t), \Psi(x_s)) \geq l$ if x_t and x_s dissimilar

$$(u > 0 \text{ and } l > 0)$$

Two samples are *similar* if they belong to the same regime.

Two samples are *dissimilar* if they belong to consecutive regimes.

Supervised change point detection

This setting can be used to learn a deep representation.

Here, two layers of temporal separable convolutions and maxpooling (with tensorflow).

Learning phase

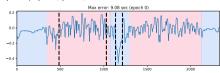
Model: "segmential 33"

Layer (type)	Output	Shape		Param #
separable_conv1d_77 (Separab	(None,	None,	5)	140
max_pooling1d_73 (MaxPooling	(None,	None,	5)	0
separable_convld_78 (Separab	(None,	None,	1)	166
max_pooling1d_74 (MaxPooling	(None,	None,	1)	0
Total params: 306				
Trainable params: 306				
Non-trainable params: 0				

Prediction phase

True change points: [347, 1075, 1297, 2123, 2332]
Predicted change points: [355, 1075, 1295, 2090, 2332]
Max error: 0.33 sec

Epoch by epoch (epoch 0)



True segmentation: alternating colors.

Supervised change point detection

This setting can be used to learn a deep representation.

Here, two layers of temporal separable convolutions and max-pooling (with tensorflow).

Learning phase

Model: "segmential 33"

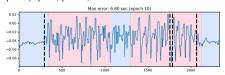
Layer (type)	Output	Shape		Param #
separable_convld_77 (Separab	(None,	None,	5)	140
max_pooling1d_73 (MaxPooling	(None,	None,	5)	0
separable_convld_78 (Separab	(None,	None,	1)	166
max_poolingld_74 (MaxPooling	(None,	None,	1)	0
Total params: 306 Trainable params: 306 Non-trainable params: 0				

Prediction phase

```
[267]: 1 true_bkps = y[0].numpy().tolist()
2 transformed = model(X[0][0].numpy()
3 prediction = pyte.lineney(jump=5).fit(transformed).predict(4)
5 print = results
6 print("True change pointsit*\tyttrue_bkps)")
7 print("True change pointsit\tyttrue_bkps)")
8 print("True change pointsit\tyttrue_bkps)")
7 print("True change pointsit\tytrue_bkps)")
8 print("Max error: {error: 2f} sec")
True change pointsi
[347, 1075, 1297, 2123, 2332]
```

True change points: [347, 1075, 1297, 2123, 2332]
Predicted change points: [355, 1075, 1295, 2090, 2332]
Max error: 0.33 sec

Epoch by epoch (epoch 10)



True segmentation: alternating colors.

Supervised change point detection

This setting can be used to learn a deep representation.

Here, two layers of temporal separable convolutions and max-pooling (with tensorflow).

Learning phase

Model: "sequential 33"

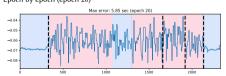
Layer (type)	Output	Shape		Param #
separable_convld_77 (Separab	(None,	None,	5)	140
max_pooling1d_73 (MaxPooling	(None,	None,	5)	0
separable_convld_78 (Separab	(None,	None,	1)	166
max_pooling1d_74 (MaxPooling	(None,	None,	1)	0
Total params: 306				
Trainable params: 306				

Prediction phase

```
[267]: 1 true_bbps = y[0].numpy().tolist()
2 transformed = model(x)[0].numpy()
3 prediction = rpt.Binney()ump*0).fit(transformed).predict(4)
4 error = hausdorff(true_bbps, prediction)/100
5 * print results
6 print(f*True change points:\tt\true_bbps)*)
7 print(f*Predicted change points:\tt\prediction)*)
8 print(f*Max error: (error: 2f) sec*)
True change points:
[247, 1075, 1297, 2123, 2332]
Predicted change points: [347, 1075, 1297, 2123, 2332]
```

Max error: 0.33 sec

Epoch by epoch (epoch 20)



True segmentation: alternating colors.

Supervised change point detection

This setting can be used to learn a deep representation.

Here, two layers of temporal separable convolutions and maxpooling (with tensorflow).

Learning phase

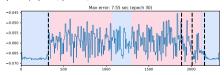
Model: "sequential 33"

Layer (type)	Output	Shape		Param #
separable_convld_77 (Separab	(None,	None,	5)	140
max_pooling1d_73 (MaxPooling	(None,	None,	5)	0
separable_convld_78 (Separab	(None,	None,	1)	166
max_pooling1d_74 (MaxPooling	(None,	None,	1)	0
Total params: 306 Trainable params: 306 Non-trainable params: 0				

Prediction phase

True change points: [347, 1075, 1297, 2123, 2332]
Predicted change points: [355, 1075, 1295, 2090, 2332]
Max error: 0.33 sec

Epoch by epoch (epoch 30)



True segmentation: alternating colors.

Supervised change point detection

This setting can be used to learn a deep representation.

Here, two layers of temporal separable convolutions and maxpooling (with tensorflow).

Learning phase

```
[262]: 1 x, y = get_Xy(8)
2 model = get_model()
3 model.compile(loss=loss_func,
optimizer=keras.optimizers.Adam(le-2))
5 history = model.fit(x, y, epochs=101, verbose=0,
callbacks=CustomCallback())
7 model.summary()
```

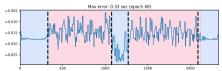
Model: "segmential 33"

				Param #
eparable_conv1d_77 (Separab	(None,	None,	5)	140
ax_pooling1d_73 (MaxPooling	(None,	None,	5)	0
eparable_convld_78 (Separab	(None,	None,	1)	166
ax_pooling1d_74 (MaxPooling	(None,	None,	1)	0

Prediction phase

Predicted change points: Max error: 0.33 sec [347, 1075, 1297, 2123, 2332] [355, 1075, 1295, 2090, 2332]

Epoch by epoch (epoch 40)



True segmentation: alternating colors.

Supervised change point detection

This setting can be used to learn a deep representation.

Here, two layers of temporal separable convolutions and maxpooling (with tensorflow).

Learning phase

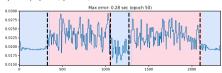
Model: "sequential 33"

Layer (type)	Output	Shape		Param #
separable_convld_77 (Separab	(None,	None,	5)	140
max_pooling1d_73 (MaxPooling	(None,	None,	5)	0
separable_convld_78 (Separab	(None,	None,	1)	166
max_pooling1d_74 (MaxPooling	(None,	None,	1)	0
Total params: 306 Trainable params: 306 Non-trainable params: 0				

Prediction phase

True change points: [347, 1075, 1297, 2123, 2332]
Predicted change points: [355, 1075, 1295, 2090, 2332]
Max error: 0.33 sec

Epoch by epoch (epoch 50)



True segmentation: alternating colors.

Supervised change point detection

This setting can be used to learn a deep representation.

Here, two layers of temporal separable convolutions and maxpooling (with tensorflow).

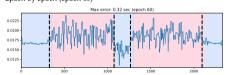
Learning phase

Model: "segmential 33"

Layer (type)	Output	Shape		Param #
separable_convld_77 (Separab	(None,	None,	5)	140
max_pooling1d_73 (MaxPooling	(None,	None,	5)	0
separable_convld_78 (Separab	(None,	None,	1)	166
max_pooling1d_74 (MaxPooling	(None,	None,	1)	0
Total params: 306 Trainable params: 306 Non-trainable params: 0				

Prediction phase

Max error: 0.33 sec Epoch by epoch (epoch 60)



True segmentation: alternating colors.

Supervised change point detection

This setting can be used to learn a deep representation.

Here, two layers of temporal separable convolutions and max-pooling (with tensorflow).

Learning phase

```
[262]: 1 x, y = get_xy(8)
2 model = get_model()
3 model.compile(loss=loss_func,
optimizer=keras.optimizers.Adam(1e-2))
5 history = model.fit(x, y, epoch==101, verbose=0,
callbacks=CustomCallback())
7 model.summary()
```

Model: "segmential 22"

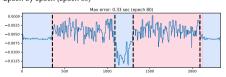
Layer (type)	Output	Shape		Param #
separable_convld_77 (Separab	(None,	None,	5)	140
max_pooling1d_73 (MaxPooling	(None,	None,	5)	0
separable_convld_78 (Separab	(None,	None,	1)	166
max_poolingld_74 (MaxPooling	(None,	None,	1)	0
Total params: 306 Trainable params: 306 Non-trainable params: 0				

Prediction phase

[355, 1075, 1295, 2090, 2332]

Predicted change points: Max error: 0.33 sec

Epoch by epoch (epoch 80)



True segmentation: alternating colors.

Supervised change point detection

This setting can be used to learn a deep representation.

Here, two layers of temporal separable convolutions and maxpooling (with tensorflow).

Learning phase

```
[262]: 1 x, y = get_Xy(8)
2 model = get_model()
3 model.compile(loss=loss_func,
optimizer=keras.optimizers.Adam(1e-2))
5 history = model.fit(x, y, epocha=101, verbose=0,
callbacks=CustomCallback())
7 model.summary()
```

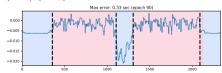
Model: "sequential 33"

Layer (type)	Output	Shape		Param #
separable_convld_77 (Separab	(None,	None,	5)	140
max_pooling1d_73 (MaxPooling	(None,	None,	5)	0
separable_convld_78 (Separab	(None,	None,	1)	166
max_pooling1d_74 (MaxPooling	(None,	None,	1)	0
Total params: 306 Trainable params: 306 Non-trainable params: 0				

Prediction phase

True change points: [347, 1075, 1297, 2123, 2332]
Predicted change points: [355, 1075, 1295, 2090, 2332]
Max error: 0.33 sec

Epoch by epoch (epoch 90)



True segmentation: alternating colors.

Supervised change point detection

This setting can be used to learn a deep representation.

Here, two layers of temporal separable convolutions and maxpooling (with tensorflow).

Learning phase

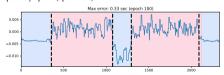
Model: "sequential 33"

Layer (type)	Output	Shape		Param #
separable_conv1d_77 (Separab	(None,	None,	5)	140
max_pooling1d_73 (MaxPooling	(None,	None,	5)	0
separable_convld_78 (Separab	(None,	None,	1)	166
max_poolingld_74 (MaxPooling	(None,	None,	1)	0
Total params: 306 Trainable params: 306 Non-trainable params: 0				

Prediction phase

True change points: [347, 1075, 1297, 2123, 2332]
Predicted change points: [355, 1075, 1295, 2090, 2332]
Max error: 0.33 sec

Epoch by epoch (epoch 100)



True segmentation: alternating colors.

Conclusion

- ► Code for those experiments will be available on my GitHub github.com/deepcharles.
- Data set is already published [Truong et al., 2019a].
- New methods are frequently implemented in ruptures.
- Extensions to graph/network data soon.

References



Truong, C., Barrois-Müller, R., Moreau, T., Provost, C., Vienne-Jumeau, A., Moreau, A., Vidal, P.-P., Vayatis, N., Buffat, S., Yelnik, A., Ricard, D., and Oudre, L. (2019a).

A data set for the study of human locomotion with inertial measurements units.

Image Processing On Line, 9.



Truong, C., Oudre, L., and Vayatis, N. (2019b).

Supervised kernel change point detection with partial annotations.

In Proceedings of the IEEE International Conference on Acoustics, Speech and Signal Processing (ICASSP), pages 1–5, Brighton, UK.



Truong, C., Oudre, L., and Vayatis, N. (2020).

Selective review of offline change point detection methods.

Signal Processing, 167.