## SipHash: a fast short-input PRF

Jean-Philippe Aumasson, Daniel J. Bernstein

### SipHash: a fast short-input MAC

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#### **UMAC**

(Black, Halevi, Krawczyk, Krovetz, Rogaway; 2000)

	43 bytes	256 bytes	1500 bytes	256 kbytes
UMAC32	16.3	3.8	2.1	1.9
UMAC-STD	52.9	12.3	3.8	1.9
UMAC16	14.0	2.7	1.2	1.0
UMAC-MMX	35.9	4.5	1.7	1.0

http://fastcrypto.org/umac/update.pdf

#### 1 cycle/byte on a Pentium III!

 $UMAC(m) = H(k1, m) \oplus AES(k2, n)$ 

#### UMAC's universal hash

# Polynomial-evaluation using 64-bit multipliers with Horner's rule

$$\left(\sum_{i=1}^{\ell/2} \left( (m_{2i-1} + k_{2i-1}) \bmod 2^w \right) \cdot \left( (m_{2i} + k_{2i}) \bmod 2^w \right) \right) \bmod 2^{2w}$$

#### UMAC fast C implementation

2000+ LoC (without AES)

Not portable

```
int uhash(uhash ctx t ahc, char *msg, long len, char *res)
        /* assumes that msg is in a writable buffer of length divisible by */
1799
        /* L1 PAD BOUNDARY. Bytes beyond msg[len] may be zeroed.
1801
1802
           UINT8 nh result[STREAMS*sizeof(UINT64)];
           UINT32 nh len;
            int extra zeroes_needed;
1804
1805
1806
           /* If the message to be hashed is no longer than L1 HASH LEN, we skip
             * the polyhash.
1808
           if (len <= L1 KEY LEN) {</pre>
                                               /* If zero length messages will not */
                if (len == 0)
                    nh len = L1 PAD BOUNDARY; /* be seen, comment out this case
1811
1812
1813
                    nh_len = ((len + (L1_PAD_BOUNDARY - 1)) & ~(L1_PAD_BOUNDARY - 1));
                extra zeroes needed = nh len - len;
1814
                zero pad((UINT8 *)msg + len, extra_zeroes_needed);
1815
                nh(&ahc->hash, (UINT8 *)msg, nh len, len, nh result);
1816
                ip short(ahc,nh result, res);
1817
           } else {
1819
                /* Otherwise, we hash each L1 KEY LEN chunk with NH, passing the NH
                 * output to poly hash().
1820
                 */
1822
                do {
                    nh(&ahc->hash, (UINT8 *)msg, L1 KEY LEN, L1 KEY LEN, nh result);
                    poly hash(ahc,(UINT32 *)nh result);
1824
1825
                    len -= L1 KEY LEN;
                    msg += L1 KEY LEN;
                } while (len >= L1 KEY LEN);
```

```
1) This version does not work properly on messages larger than 16MB
  2) If you set the switch to use SSE2, then all data must be 16-byte
     aligned
  3) When calling the function umac(), it is assumed that msg is in
  a writable buffer of length divisible by 32 bytes. The message itself
 * does not have to fill the entire buffer, but bytes beyond msg may be
  zeroed.
```

http://fastcrypto.org/umac/2004/src/umac.c

# UMAC uses a PRG to expand the key to 33280 bits

Using a PRG, map Key to  $K = K_1 K_2 \cdots K_{1024}$ , with each  $K_i$  a 32-bit word, and to A, where |A| = 512.

# RFC4418 replaces UMAC's PRG with an AES-based KDF...

#### 3.2.1. KDF Algorithm

```
Input:
  K, string of length KEYLEN bytes.
  index, a non-negative integer less than 2^64.
  numbytes, a non-negative integer less than 2^64.
Output:
 Y, string of length numbytes bytes.
Compute Y using the following algorithm.
  //
  // Calculate number of block cipher iterations
  //
  n = ceil(numbytes / BLOCKLEN)
 Y = <empty string>
  // Build Y using block cipher in a counter mode
  for i = 1 to n do
    T = uint2str(index, BLOCKLEN-8) || uint2str(i, 8)
    T = ENCIPHER(K, T)
    Y = Y \mid \mid T
  end for
 Y = Y[1...numbvtes]
  Return Y
```

# ... and uses AES and this KDF in a "Pad-Derivation Function"

#### 3.3.1. PDF Algorithm

```
Input:
  K, string of length KEYLEN bytes.
 Nonce, string of length 1 to BLOCKLEN bytes.
 taglen, the integer 4, 8, 12 or 16.
Output:
 Y, string of length taglen bytes.
Compute Y using the following algorithm.
   //
   // Extract and zero low bit(s) of Nonce if needed
   if (taglen = 4 or taglen = 8)
     index = str2uint(Nonce) mod (BLOCKLEN/taglen)
     Nonce = Nonce xor uint2str(index, bytelength(Nonce))
   end if
   //
   // Make Nonce BLOCKLEN bytes by appending zeroes if needed
   //
   Nonce = Nonce | | zeroes(BLOCKLEN - bytelength(Nonce))
   //
   // Generate subkey, encipher and extract indexed substring
   K' = KDF(K, 0, KEYLEN)
   T = ENCIPHER(K', Nonce)
   if (taglen = 4 \text{ or } taglen = 8)
     Y = T[1 + (index*taglen) ... taglen + (index*taglen)]
   else
     Y = T[1...taglen]
   end if
   Return Y
```

# Not so simple

# SipHash

Simple ARX round function
Simple JH-like message injection

No key expansion

No external primitive

No state between messages

# SipHash initialization

256-bit state v0 v1 v2 v3

128-bit key k0 k1

$$v0 = k0 \oplus 736f6d6570736575$$

$$v2 = k0 \oplus 6c7967656e657261$$

$$v3 = k1 \oplus 7465646279746573$$

# SipHash initialization

256-bit state v0 v1 v2 v3

128-bit key k0 k1

$$v0 = k0 \oplus$$
 "somepseu"

$$v1 = k1 \oplus "dorandom"$$

$$v2 = k0 \oplus "lygenera"$$

$$v3 = k1 \oplus \text{"tedbytes"}$$

Message parsed as 64-bit words m0, m1, ...

c iterations of SipRound

Message parsed as 64-bit words m0, m1, ...

c iterations of SipRound

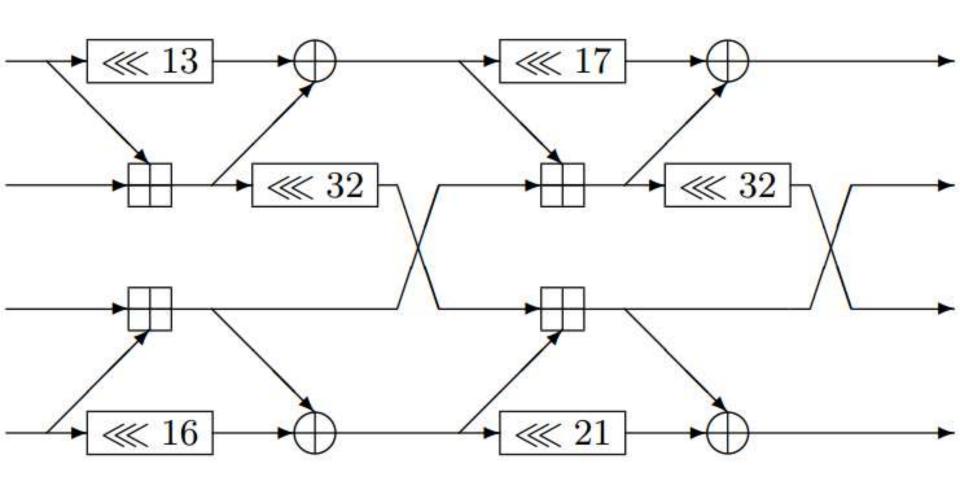
Message parsed as 64-bit words m0, m1, ...

c iterations of SipRound

Message parsed as 64-bit words m0, m1, ...

Etc.

# SipRound

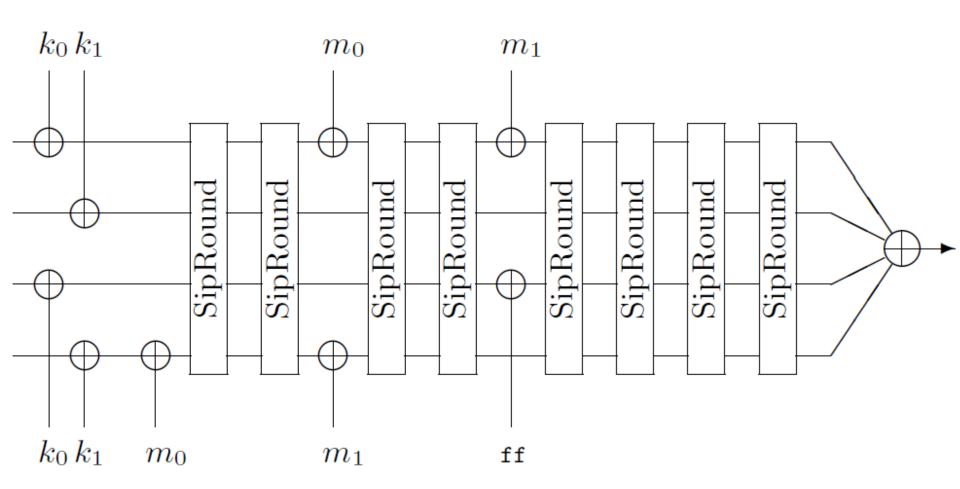


# SipHash finalization

d iterations of SipRound

Return v0  $\bigoplus$  v1  $\bigoplus$  v2  $\bigoplus$  v3

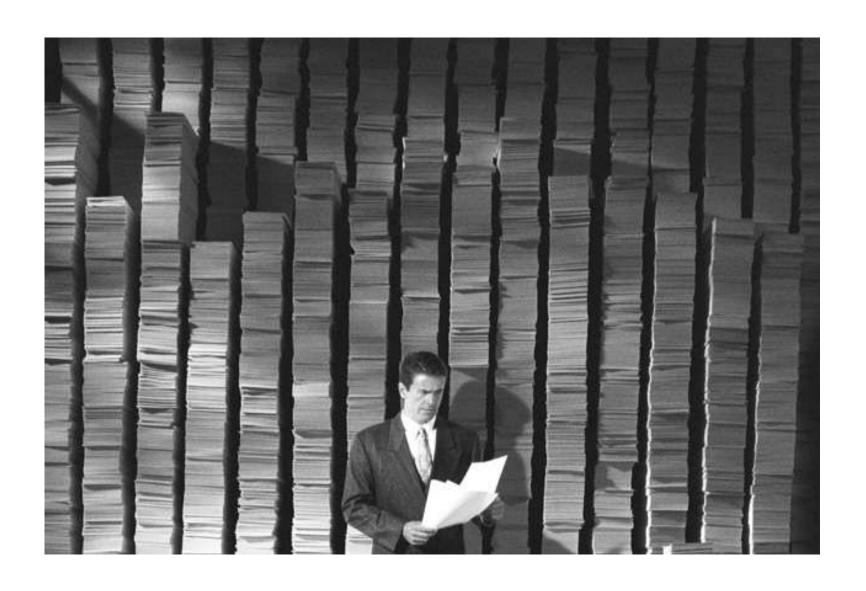
#### SipHash-2-4 hashing 15 bytes



- Family SipHash-c-d
- Fast proposal: SipHash-2-4
- Conservative proposal: SipHash-4-8

- Weaker versions for cryptanalysis:
- SipHash-1-0, SipHash-2-0, etc.
- SipHash-1-1, SipHash-2-1, etc.
- Etc.

# (Many) short inputs?



⊗⊜   File Fdit View Go	o Capture Analyze Stati	istics Telephony Tools	Internals I	Help	
			3 F J		
			V 1 2		
Filter: tcp.dstport ec	q 80 or tcp.dstport eq 443	▼ Expres	ssion Clea	ar Apply	
No. Time	Source	Destination		Length Info	
25/5 140.0/1983			TOP	00 [TCP Keep-Active] 53317 > NTCP [ACK] Seq=1 ACK=1 WIN=1104 Len=0 TSVat=70072448 TSect=18005050	
2519 149.923984			TCP	66 53518 > http [ACK] Seq=2 Ack=2 Win=255 Len=0 TSval=76674761 TSecr=1806619891	
2542 151.325449		100 to 10	НТТР	831 Continuation or non-HTTP traffic	
200 HO OF THE PROPERTY OF THE PARTY OF THE P		10.0.00.00	HTTP	1333 Continuation or non-HTTP traffic	
2549 151.504048		10 h 10 m	TCP	54 45886 > http [ACK] Seq=8269 Ack=40432 Win=65535 Len=0	
2551 151.504058		10.0.00.00	TCP	54 45886 > http [ACK] Seq=8269 Ack=41120 Win=65535 Len=0	
2553 151.509701		10 h 10 m	TCP	54 45886 > http [ACK] Seq=8269 Ack=42480 Win=65535 Len=0	
2555 151.509713		10.0.00.00	TCP	54 45886 > http [ACK] Seq=8269 Ack=43168 Win=65535 Len=0	
2557 151.517987		(A) A (B) (B)	TCP	54 45886 > http [ACK] Seq=8269 Ack=44528 Win=65535 Len=0	
2559 151.517999 2561 151.524712		175 H. J. J. B. 48	TCP	54 45886 > http [ACK] Seq=8269 Ack=45216 Win=65535 Len=0	
		10.0.00		54 45886 > http [ACK] Seq=8269 Ack=46576 Win=65535 Len=0 54 45886 > http [ACK] Seq=8269 Ack=47264 Win=65535 Len=0	
2563 151.524725 2565 151.527101		10 to 10 to	TCP	The state of the s	
				54 45886 > http [ACK] Seq=8269 Ack=48624 Win=65535 Len=0	
2567 151.527112		10.0.00.00	TCP	54 45886 > http [ACK] Seq=8269 Ack=49312 Win=65535 Len=0	
2569 151.532604		10 h 10 m	TCP	54 45886 > http [ACK] Seq=8269 Ack=50672 Win=65535 Len=0	
2571 151.532612		10.00.00.00	TCP	54 45886 > http [ACK] Seq=8269 Ack=51360 Win=65535 Len=0	
2573 151.535491		0.000	TCP	54 45886 > http [ACK] Seq=8269 Ack=52720 Win=65535 Len=0	
		10.00.00.00	TCP	54 45886 > http [ACK] Seq=8269 Ack=53408 Win=65535 Len=0	
2577 151.537818		10 h m m	TCP	54 45886 > http [ACK] Seq=8269 Ack=54768 Win=65535 Len=0	
		15 3 10 10 10	TCP	54 45886 > http [ACK] Seq=8269 Ack=55456 Win=65535 Len=0	
2583 151.543724		0.000	TCP	54 45886 > http [ACK] Seq=8269 Ack=57504 Win=65535 Len=0	
2585 151.548877		10.31.00.00	ТСР	54 45886 > http [ACK] Seq=8269 Ack=58501 Win=65535 Len=0	
2645 155.535986			TCP	66 53517 > http [ACK] Seq=2 Ack=2 Win=1104 Len=0 TSval=76676164 TSecr=1806625501	
2682 158.265727		10.30.50.00	TCP	66 53517 > http [FIN, ACK] Seq=2 Ack=2 Win=1104 Len=0 TSval=76676846 TSecr=1806625501	
2684 158.265970			TCP	66 53518 > http [FIN, ACK] Seq=2 Ack=2 Win=255 Len=0 TSval=76676846 TSecr=1806619891	
3306 196.607981			TCP	54 [TCP Keep-Alive] 45886 > http [ACK] Seq=8268 Ack=58501 Win=65535 Len=0	
Type. IF (UXUOUU					
▶ Internet Protocol Version 4, Src: ▼ Transmission Control Protocol, Src Port: 53518 (53518), Dst Port: http (80), Seq: 2, Ack: 2, Len: 0					
H-		: 53518 (53518), DST P	ort: nttp	(80), Seq: 2, Ack: 2, Len: 0	
Source port: 535					
Destination port					
[Stream index: 0					
Sequence number:	· 2 (relative seguen	ce_number)		in the second se	

### Hash tables

```
h = {}
h [ 'foo'] = 'bar' # insert 'bar'
Print h['foo'] # lookup
```

#### Non-crypto functions to produce 'foo':

```
for (; nKeyLength > 0; nKeyLength -=1) {
hash = ((hash << 5) + hash) + *arKey++;
}</pre>
```

# Hash flooding attacks

**Multicollisions** forcing worst-case complexity of  $\Theta(n^2)$ , instead of  $\Theta(n)$ 

[when table implemented as linked lists]

# djbdns/cache.c, 1999

```
nextpos = prevpos ^ get4(pos);
prevpos = pos;
pos = nextpos;
if (++loop > 100) return 0; /* to protect against hash flooding */
}
return 0;
```

#### **USENIX 2003**

#### Denial of Service via Algorithmic Complexity Attacks

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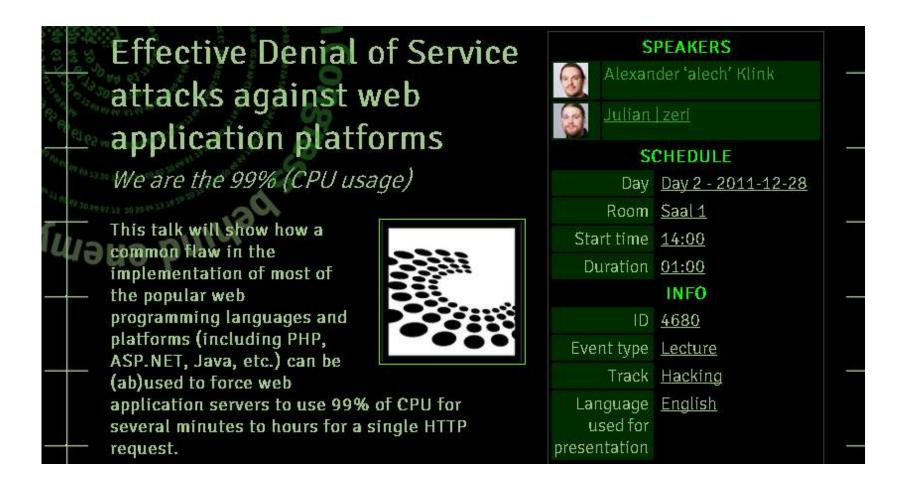
Department of Computer Science, Rice University

#### Abstract

We present a new class of low-bandwidth denial of service attacks that exploit algorithmic deficiencies sume O(n) time to insert n elements. However, if each element hashes to the same bucket, the hash table will also degenerate to a linked list, and it will take  $O(n^2)$  time to insert n elements.

#### Vulnerabilities in Perl, web proxy, IDS

#### CCC 2011



Affected: PHP, ASP.net, Python, etc.

```
n.runs-SA-2011.004
                                         28-Dec-2011
Vendors: PHP, http://www.php.net
          Oracle, http://www.oracle.com
          Microsoft, http://www.microsoft.com
          Python, http://www.python.org
          Ruby, http://www.ruby.org
          Google, http://www.google.com Affected Products: PHP 4 and 5
          Java
          Apache Tomcat
          Apache Geronimo
          Jetty
          Oracle Glassfish
          ASP.NET
          Python
          Plone
          CRuby 1.8, JRuby, Rubinius
          v8
Vulnerability:
               Denial of Service through hash table
```

security(at)nruns.com

n.runs AG

http://www.nruns.com/

multi-collisions

## How short?

OpenDNS cache: 27 bytes on average

Ruby on Rails web application: <20 bytes

# Why SipHash?

Minimizes hash flooding

→ impact limited to sqrt(communication)

Well-defined security goal (PRF)

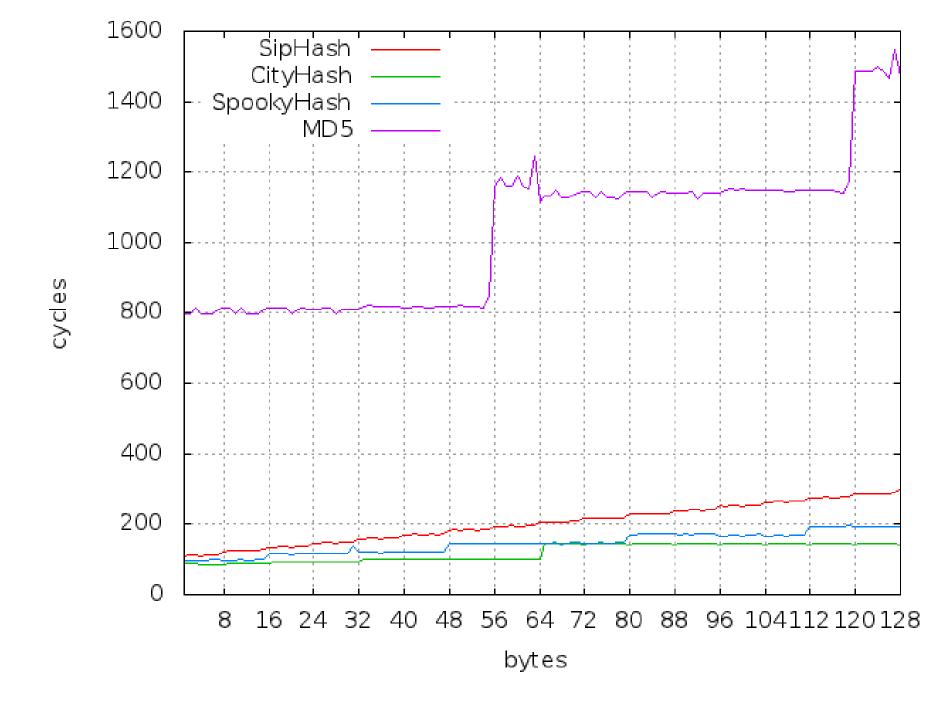
Competitive in speed with non-crypto hashes

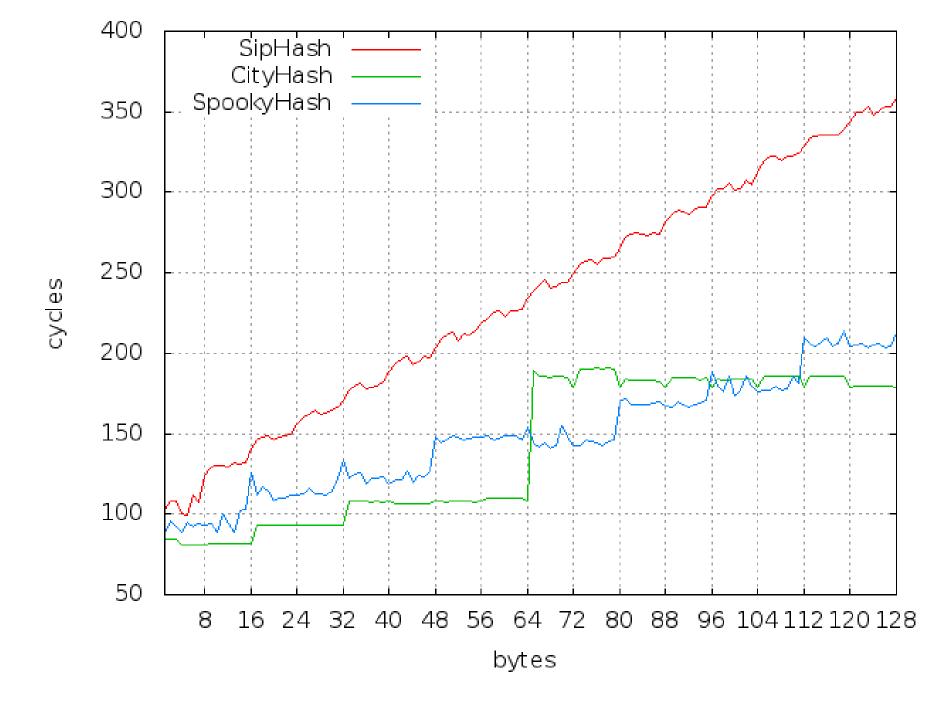
## How fast?

SipHash-2-4 on an AMD Athlon II Neo

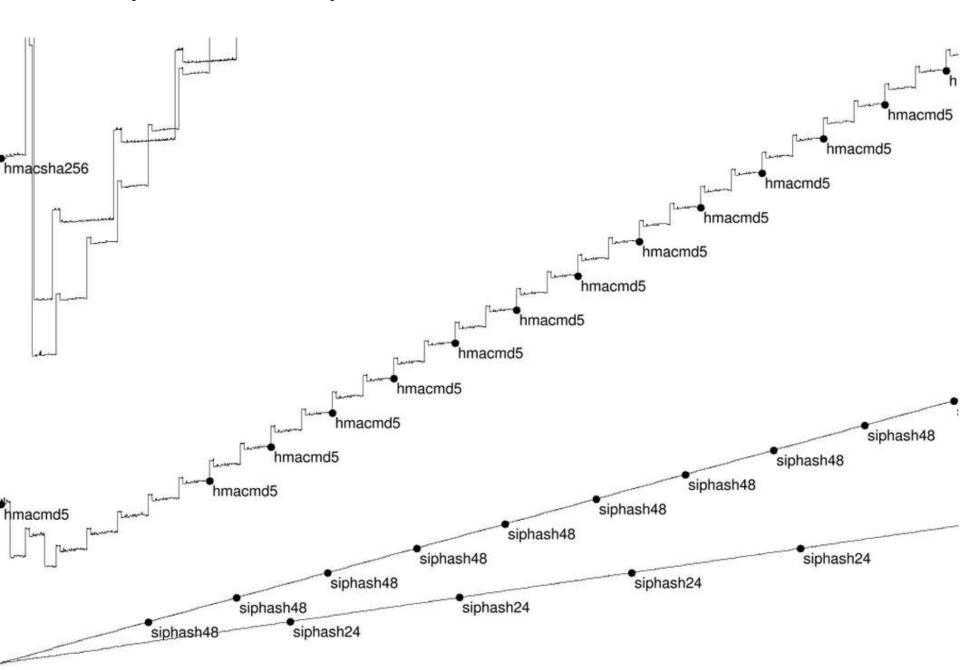
Byte length	8	16	32	64
Cycles	123	134	158	204
(per byte)	(15.38)	(8.38)	(4.25)	(3.19)

Long data: 1.44 cycles/byte

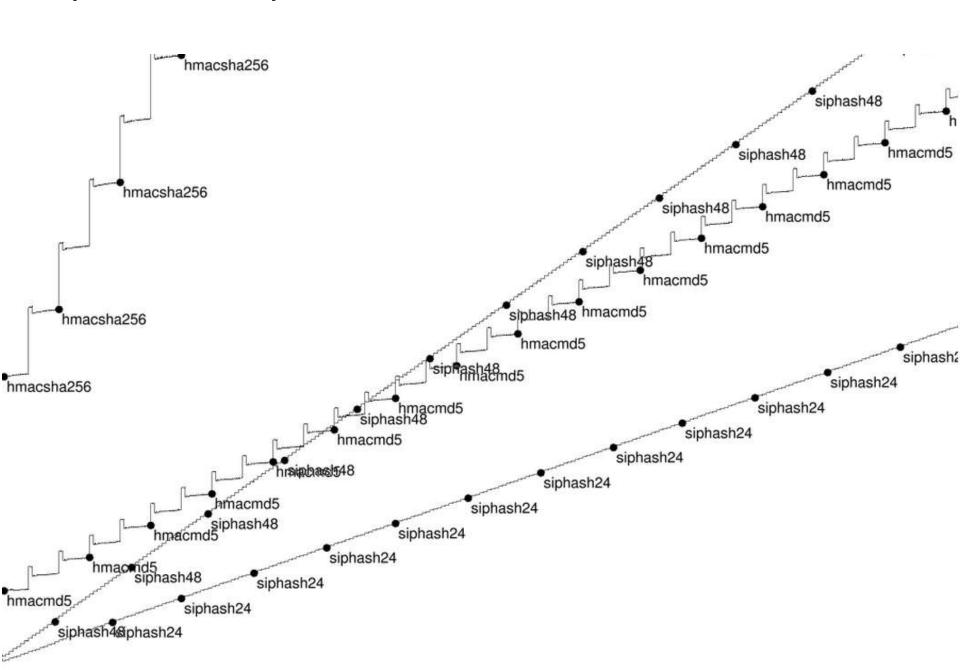




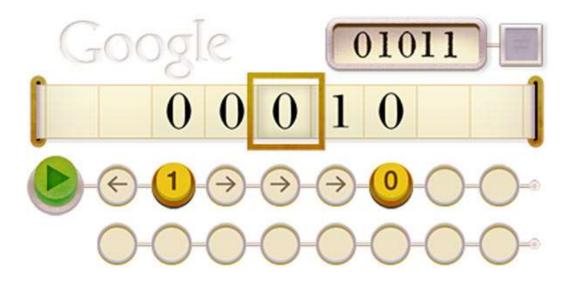
#### amd64; K10 45nm; 2010 AMD Phenom II X6 1090T



#### x86; K10 45nm; 2010 AMD Phenom II X6 1090T



# Cryptanalysis



## Generic attacks

- ≈ 2<sup>128</sup> key recovery
- ≈ 2<sup>192</sup> state recovery
- ≈ 2<sup>128</sup> internal-collision forgeries
- ≈ 2<sup>s</sup> forgery attack with success probability 2<sup>s-64</sup>

Round	Differences	Prob.
1		1 (1)
2	8	13 (14)
3	1.81 811a.1.1 8.1.181. 8.1.822 a18.1.8.11 8.12b413a292821. 82928282	42 (56)
4	228221211 e835621322.1.235 2221.8.122613 621.c21.4242.3 2.1124ca35e.13 6677845357bd22 4.1.cc212641. 82828.11.6	103 (159)
5	a21182244a24e613 2ec144fcb8.115dd c245d93226674453 e2.1848a34a6.3 f225f3ce8cd.c6d8 a44f51d8d.9e5616 2.445936ac53e25. a.4.d3.2.a551	152 (311)
6	52652.cc868.c689 27baa9d2d.e.fcd8 7ccdb44684.b.8ee 32246acc8cb4ce93 566.3a5175df891e 2.e5d3.249fb3ea6 4ee9de8a.8bfc67d 2425523ec62cf459	187 (498)

#### Characteristic verified with ARXtools

http://www.di.ens.fr/~leurent/arxtools.html

## Proof of insecurity

SipRound(0) = 0
That is, SipRound is not ideal
Therefore SipHash is insecure



## Proof of simplicity

June 20: paper published online

June 28: 18 third-party implementations

```
C (Floodyberry, Boßlet, Neves); C# (Haynes)
Cryptol (Lazar); Erlang, Javascript, PHP (Denis)
Go (Chestnykh); Haskell (Hanquez);
Java, Ruby (Boßlet); Lisp (Brown);
```

## More on SipHash:

http://131002.net/siphash

Thanks to all implementers!