

# Fast exponentiation mod n

- Algorithm calculates  $a^e \bmod n$  so, that largest number stored in variables  $\bullet (n-1)^2$ . Algorithm is fast, and overflow is avoided.

Algorithm: Four BigInteger variables are needed:

A = base, E = exponent

n = modulus , C = additional variable

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1. Set C = 1
2. While E > 1 DO
    If E is odd,
        then {E = E-1 ; C = A*C mod n ;}
        else { E = E/2 ; A = A^2 mod n ; }
3. A = A*C mod n
Return A
```

# Example $7^{11} \bmod 13$

Variables:

$$\begin{aligned}7^{11} \bmod 13 &= \\7^{10} * 7 \bmod 13 &= \\49^5 * 7 \bmod 13 &= \\10^5 * 7 \bmod 13 &= \\10^4 * 5 \bmod 13 &= \\100^2 * 5 \bmod 13 &= \\9^2 * 5 \bmod 13 &= \\81 * 5 \bmod 13 &= \\3 * 5 \bmod 13 &= \\2\end{aligned}$$

A	E	C	N
7	11	1	13
7	10	7	13
49=10	5	7	13
10	4	7*10= 5	13
100 =9	2	5	13
81=3	1	5	13
3*5 =2	1	1	13

result