Time Series Analysis

Road Map

- Why is prediction supervised learning, how it differs from classification.
- Beer dataset time series
- Electricity prediction example





A **prediction** or forecast is a statement about the way things will happen in the future, often but not always based on experience or knowledge.

Why is Prediction Supervised Learning



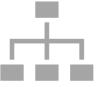
We use labeled training data to learn and make prediction.



Supervised learning means we have an already marked dataset giving us what the learning process should give you.

Forms of data analysis to predict future data trends

There are two forms of data analysis that can be used for extracting models describing important classes or to predict future data trends. These two forms are as follows







Regression

Also, called prediction in earlier literature

Classification vs Regression

Classification	Regression/Prediction
It predicts categorical class labels	It predicts continuous valued functions
Example: A bank loan officer wants to analyze the data in order to know which customer (loan applicant) are risky or which are safe.	Example: Suppose the marketing manager needs to predict how much a given customer will spend during a sale at his company.
A model or classifier is constructed to predict the categorical labels. These labels are risky or safe for loan application data	In this example we are bothered to predict a numeric value.

Reference: https://www.tutorialspoint.com/



A **time series** is simply a series of data points taken at specified **times** usually at equal intervals.

It is used to **predict** the future values based on the **previous** observed values.

Importance of Time Series Analysis



Business Forecasting



Understand past behavior



Plan future



Evaluate current accomplishment



Time series decomposition is a mathematical procedure which transforms a time series into multiple different time series.

The original time series is often split into 3 component series:

- Seasonal
- Trend
- Random/noise/remainder



Seasonal

 Patterns that repeat with a fixed period of time.

• **Example:** A website might receive more visits during weekends so this would produce data with a seasonality of 7 days.

Trend

- The underlying trend of the metrics.
- **Example:** A website increasing in popularity should show a general trend that goes up.

Random/ Noise/ Remainder

• This is the residuals of the original time series after the seasonal and trend series are removed.

Let's take one example

Data: beer.csv

Monthly beer consumption in Australia from 1956 to 1995

	А	В	С
1	beer		
2	93	2	
3	96		
4	95	2	
5	77	1	
6	70	9	
7	64	8	
8	70	1	
9	77	3	
10	79	5	
11	100	6	
12	100	7	
13	107	1	
14	95	9	
15	82	8	
16	83	3	
17	80		
18	80	4	
19	67	5	
20	75	7	
21	71	1	
22	89	3	
23	101	1	
24	105	2	
25	114	1	
26	96	3	
27	84	4	
28	91	2	
29	81	9	
30	80	5	
31	70	4	
32	74	8	
33	75	9	

```
beer<-read.csv("~/Downloads/beer.csv",header=T,dec=",",sep=";");</pre>
    beer
    beer<-ts(beer[,1],start=1956,freq=12);
    beer
    plot(beer)
11
    plot(stl(log(beer),s.window="periodic"))
13
    lbeer<-log(beer);</pre>
15
16
    plot(lbeer)
```

read.csv() is used to read csv file.

header: This CSV file has header so it is set to true.

dec: the character used in the file for decimal points.

sep: the field separator character. Values on each line of the file are separated by this character.

		А	В	С	
	1	beer			← Header
Ī	2	93	2		
	3	96			
	4	95	2	◀	 Decimal point
	5	77	1		
	6	70	9		
	7	64	8		
	8	70	1		
	9	77	3		
	10	79	5		
	11	100	6		
	12	100	7		
	13	107	1		

```
1
    beer<-read.csv("~/Downloads/beer.csv",header=T,dec=",",sep=";");</pre>
    beer
    beer<-ts(beer[,1],start=1956,freq=12);
 8
    beer
10
    plot(beer)
11
    plot(stl(log(beer),s.window="periodic"))
13
14
    lbeer<-log(beer);</pre>
15
16
    plot(lbeer)
```

```
> beer
     beer
     93.2
     96.0
    95.2
    77.1
4
     70.9
    64.8
     70.1
    77.3
9
     79.5
10
    100.6
11
    100.7
12 107.1
```

```
1
    beer<-read.csv("~/Downloads/beer.csv",header=T,dec=",",sep=";");</pre>
    beer
    beer<-ts(beer[,1],start=1956,freq=12);
    beer
    plot(beer)
11
    plot(stl(log(beer),s.window="periodic"))
13
    lbeer<-log(beer);</pre>
15
16
    plot(lbeer)
```

The function ts is used to create time-series objects.

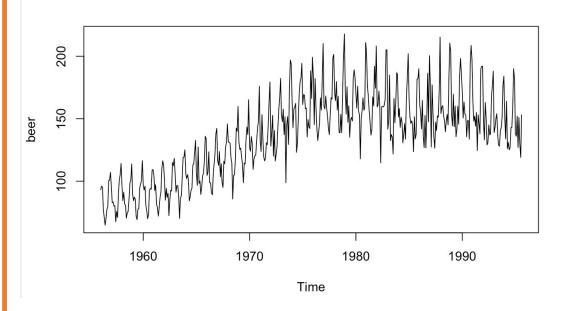
freq = 12 when the data are sampled monthly and the natural time period is a year.

freq = 7 when the data are sampled daily, and the natural time period is a week.

```
1
    beer<-read.csv("~/Downloads/beer.csv",header=T,dec=",",sep=";");
 3
    beer
    beer<-ts(beer[,1],start=1956,freq=12);
    beer
    plot(beer)
11
    plot(stl(log(beer),s.window="periodic"))
13
14
    lbeer<-log(beer);</pre>
15
    plot(lbeer)
```

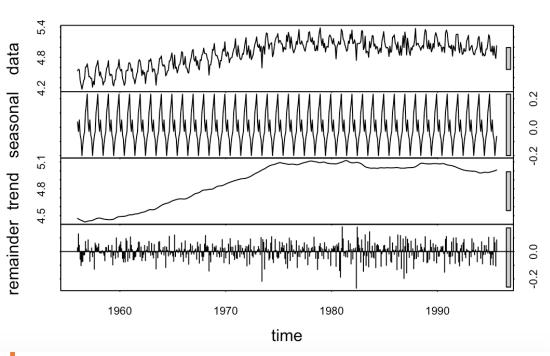
```
> beer
                                        Jul
                      77.1 70.9 64.8 70.1 77.3 79.5 100.6 100.7 107.1
           82.8 83.3 80.0 80.4 67.5 75.7 71.1 89.3 101.1 105.2 114.1
                           80.5
                                 70.4 74.8 75.9 86.3 98.7 100.9 113.8
           84.4 87.2 85.6 72.0 69.2 77.5 78.1 94.3 97.7 100.2 116.4
1960 97.1 93.0 96.0 80.5 76.1 69.9 73.6 92.6 94.2 93.5 108.5 109.4
1961 105.1 92.5 97.1 81.4 79.1 72.1 78.7 87.1 91.4 109.9 116.3 113.0
1962 100.0 84.8 94.3 87.1 90.3 72.4 84.9 92.7 92.2 114.9 112.5 118.3
1963 106.0 91.2 96.6 96.3 88.2 70.2 86.5 88.2 102.8 119.1 119.2 125.1
1964 106.1 102.1 105.2 101.0 84.3 87.5 92.7 94.4 113.0 113.9 122.9 132.7
1965 106.9 96.6 127.3 98.2 100.2 89.4 95.3 104.2 106.4 116.2 135.9 134.0
1966 104.6 107.1 123.5 98.8 98.6 90.6 89.1 105.2 114.0 122.1 138.0 142.2
1967 116.4 112.6 123.8 103.6 113.9 98.6 95.0 116.0 113.9 127.5 131.4 145.9
1968 131.5 131.0 130.5 118.9 114.3 85.7 104.6 105.1 117.3 142.5 140.0 159.8
1969 131.2 125.4 126.5 119.4 113.5 98.7 114.5 113.8 133.1 143.4 137.3 165.2
1970 126.9 124.0 135.7 130.0 109.4 117.8 120.3 121.0 132.3 142.9 147.4 175.9
1971 132.6 123.7 153.3 134.0 119.6 116.2 118.6 130.7 129.3 144.4 163.2 179.4
1972 128.1 138.4 152.7 120.0 140.5 116.2 121.4 127.8 143.6 157.6 166.2 182.3
1973 153.1 147.6 157.7 137.2 151.5 98.7 145.8 151.7 129.4 174.1 197.0 193.9
1974 164.1 142.8 157.9 159.2 162.2 123.1 130.0 150.1 169.4 179.7 182.1 194.3
1975 161.4 169.4 168.8 158.1 158.5 135.3 149.3 143.4 142.2 188.4 166.2 199.2
```

```
1
    beer<-read.csv("~/Downloads/beer.csv",header=T,dec=",",sep=";");</pre>
 3
    beer
    beer<-ts(beer[,1],start=1956,freq=12);
    beer
    plot(beer)
    plot(stl(log(beer),s.window="periodic"))
13
14
    lbeer<-log(beer);</pre>
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16
    plot(lbeer)
```



```
1
    beer<-read.csv("~/Downloads/beer.csv",header=T,dec=",",sep=";");</pre>
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10
    plot(stl(log(beer),s.window="periodic"))
13
14
    lbeer<-log(beer);</pre>
15
16
    plot(lbeer)
```

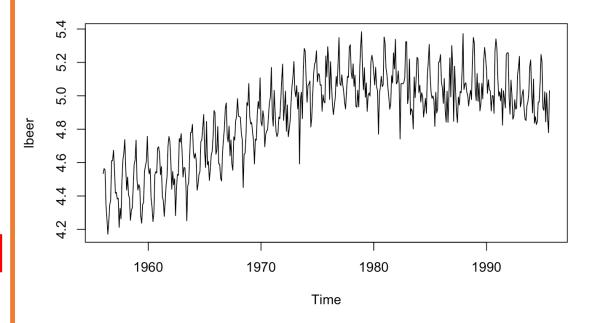
Seasonal decomposition using stl() Output



```
1
    beer<-read.csv("~/Downloads/beer.csv",header=T,dec=",",sep=";");</pre>
    beer
    beer<-ts(beer[,1],start=1956,freq=12);
    beer
    plot(beer)
11
    plot(stl(log(beer),s.window="periodic"))
    lbeer<-log(beer);</pre>
    plot(lbeer)
```

We are doing little bit transformation and explore more. So we are using logarithm.

```
1
    beer<-read.csv("~/Downloads/beer.csv",header=T,dec=",",sep=";");</pre>
 3
    beer
    beer<-ts(beer[,1],start=1956,freq=12);
 8
    beer
 9
10
    plot(beer)
11
    plot(stl(log(beer),s.window="periodic"))
13
    lbeer<-log(beer);</pre>
16
   plot(lbeer)
```



```
t<-seq(1956,1995.2,length=length(beer))
19
20
    t
21
    t2<-t^2
23
    sin.t<-sin(2*pi*t)
24
    cos.t < -cos(2*pi*t)
25
26
    sinCosSquareLM=lm(lbeer~t+t2+sin.t+cos.t)
27
28
    mean(abs(lbeer-sinCosSquareLM$fit)/lbeer)*100
```

seq function generate regular sequences

seq(Start Number, End number, Length)

Here Sequence is starting from **1956**Last number in the sequence will be **1995.2**

Length of sequence will be length of beer dataset which is **476**

So there will be 476 numbers in t variable

```
[17] 1956.000 1956.083 1956.165 1956.248 1956.330 1956.413 1956.495
 [8] 1956.578 1956.660 1956.743 1956.825 1956.908 1956.990 1957.073
 [15] 1957.155 1957.238 1957.320 1957.403 1957.485 1957.568 1957.651
 [22] 1957.733 1957.816 1957.898 1957.981 1958.063 1958.146 1958.228
 [29] 1958.311 1958.393 1958.476 1958.558 1958.641 1958.723 1958.806
 [36] 1958.888 1958.971 1959.053 1959.136 1959.219 1959.301 1959.384
 [43] 1959.466 1959.549 1959.631 1959.714 1959.796 1959.879 1959.961
 [50] 1960.044 1960.126 1960.209 1960.291 1960.374 1960.456 1960.539
 [57] 1960.621 1960.704 1960.787 1960.869 1960.952 1961.034 1961.117
 [64] 1961.199 1961.282 1961.364 1961.447 1961.529 1961.612 1961.694
 [71] 1961.777 1961.859 1961.942 1962.024 1962.107 1962.189 1962.272
 [78] 1962.355 1962.437 1962.520 1962.602 1962.685 1962.767 1962.850
 [85] 1962.932 1963.015 1963.097 1963.180 1963.262 1963.345 1963.427
 [92] 1963.510 1963.592 1963.675 1963.757 1963.840 1963.923 1964.005
 [99] 1964.088 1964.170 1964.253 1964.335 1964.418 1964.500 1964.583
[106] 1964.665 1964.748 1964.830 1964.913 1964.995 1965.078 1965.160
[113] 1965.243 1965.325 1965.408 1965.491 1965.573 1965.656 1965.738
[120] 1965.821 1965.903 1965.986 1966.068 1966.151 1966.233 1966.316
[127] 1966.398 1966.481 1966.563 1966.646 1966.728 1966.811 1966.893
[134] 1966.976 1967.059 1967.141 1967.224 1967.306 1967.389 1967.471
[141] 1967.554 1967.636 1967.719 1967.801 1967.884 1967.966 1968.049
[148] 1968.131 1968.214 1968.296 1968.379 1968.461 1968.544 1968.627
```

```
t<-seq(1956,1995.2,length=length(beer))
18
19
20
    t
21
    t2<-t^2
22
23
    sin.t<-sin(2*pi*t)</pre>
24
    cos.t<-cos(2*pi*t)
25
    sinCosSquareLM=lm(lbeer~t+t2+sin.t+cos.t)
26
27
28
    mean(abs(lbeer-sinCosSquareLM$fit)/lbeer)*100
```

Generate other variables which we will use while creating Model

```
t<-seq(1956,1995.2,length=length(beer))
18
19
20
    t
21
    t2<-t^2
23
    sin.t<-sin(2*pi*t)
24
    cos.t<-cos(2*pi*t)
25
    sinCosSquareLM=lm(lbeer~t+t2+sin.t+cos.t)
26
27
28
    mean(abs(lbeer-sinCosSquareLM$fit)/lbeer)*100
```

Here we are creating model.

Im() is used to fit linear models. It can be used to carry out regression.

```
t<-seq(1956,1995.2,length=length(beer))
18
19
20
    t
21
    t2<-t^2
23
    sin.t<-sin(2*pi*t)
24
    cos.t < -cos(2*pi*t)
25
26
    sinCosSquareLM=lm(lbeer~t+t2+sin.t+cos.t)
27
    mean(abs(lbeer-sinCosSquareLM$fit)/lbeer)*100
28
```

1.972046% Accuracy

Output

> mean(abs(lbeer-sinCosSquareLM\$fit)/lbeer)*100
[1] 1.972046

Not always possible to use such imagination

```
t<-seq(1956,1995.2,length=length(beer))
18
19
20
    t
21
    t2<-t^2
23
    sin.t<-sin(2*pi*t)
24
    cos.t < -cos(2*pi*t)
25
26
    sinCosSquareLM=lm(lbeer~t+t2+sin.t+cos.t)
27
    mean(abs(lbeer-sinCosSquareLM$fit)/lbeer)*100
28
```

1.972046% Accuracy

Output

> mean(abs(lbeer-sinCosSquareLM\$fit)/lbeer)*100
[1] 1.972046

Not always possible to use such imagination

Holt-Winters

- Exponential smoothing in its basic form (the term "exponential" comes from the fact that the weights decay exponentially) should only be used for time series with no systematic trend and/or seasonal components.
- It has been generalized to the "Holt–Winters"–
 procedure in order to deal with time series
 containg trend and seasonal variation.

A natural estimate for predicting the next value of a given time series x_t at the period $t = \tau$ is to take weighted sums of past observations:

$$\hat{x}_{(t=\tau)}(1) = \lambda_0 \cdot x_\tau + \lambda_1 \cdot x_{\tau-1} + \dots$$

It seems reasonable to weight recent observations more than observations from the past. Hence, one possibility is to use geometric weights

$$\lambda_i = \alpha (1 - \alpha)^i \qquad ; \quad 0 < \alpha < 1$$

such that
$$\hat{x}_{(t=\tau)}(1) = \alpha \cdot x_{\tau} + \alpha(1-\alpha) \cdot x_{\tau-1} + \alpha(1-\alpha)^2 \cdot x_{\tau-2} + \dots$$

HoltWinters in R

• R contains the function HoltWinters(x,alpha,beta,gamma), which lets you perform the Holt–Winters procedure on a time series x.

• In case one does not specify smoothing parameters, these are determined "automatically" (i.e. by minimizing the mean squared prediction error from one—step forecasts).

Let's do it in R with the same dataset

```
beer<-read.csv("~/Downloads/beer.csv",header=T,dec=",",sep=";");

beer<-ts(beer[,1],start=1956,freq=12);

hw<-HoltWinters(beer)

predict(hw,n.ahead=12)

plot(beer,xlim=c(1956,1996))

lines(predict(hw,n.ahead=12),col=2)

mean(abs(hw$fit[,1]-beer)/beer)*100</pre>
```

```
beer<-read.csv("~/Downloads/beer.csv",header=T,dec=",",sep=";");</pre>
32
33
    beer<-ts(beer[,1],start=1956,freq=12);
34
36
    hw<-HoltWinters(beer)</pre>
37
    predict(hw,n.ahead=12)
38
39
    plot(beer,xlim=c(1956,1996))
41
42
    lines(predict(hw,n.ahead=12),col=2)
43
    mean(abs(hw$fit[,1]-beer)/beer)*100
```

This performs the Holt–Winters procedure on the beer – dataset.

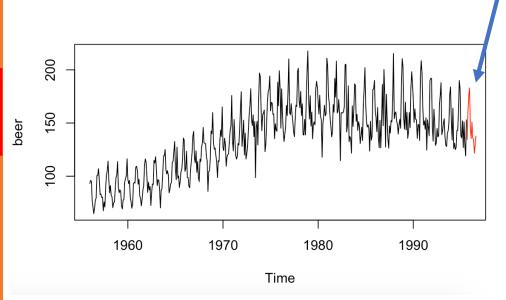
```
32
    beer<-read.csv("~/Downloads/beer.csv",header=T,dec=",",sep=";");
33
34
    beer<-ts(beer[,1],start=1956,freq=12);
35
36
    hw<-HoltWinters(beer)</pre>
27
38
    predict(hw,n.ahead=12)
22
    plot(beer,xlim=c(1956,1996))
41
42
    lines(predict(hw,n.ahead=12),col=2)
43
    mean(abs(hw$fit[,1]-beer)/beer)*100
```

This gives us the predicted values for the next 12 periods (i.e. Sep. 1995 to Aug. 1996).

```
> predict(hw,n.ahead=12)
          Jan
                   Feb
                                                        Jun
                                                                  Jul
                                                                                    Sep
                                                                                             0ct
                                                                                                                Dec
                            Mar
                                      Apr
                                               May
                                                                           Aua
                                                                                                       Nov
1995
                                                                               134.5864 162.1453 176.0870 182.9774
1996 145.0224 135.3375 150.8931 135.7861 134.8204 121.6526 129.1765 137.8240
```

```
beer<-read.csv("~/Downloads/beer.csv",header=T,dec=",",sep=";");</pre>
32
33
34
    beer<-ts(beer[,1],start=1956,freq=12);
35
36
    hw<-HoltWinters(beer)</pre>
37
38
    predict(hw,n.ahead=12)
    plot(beer,xlim=c(1956,1996))
41
42
    lines(predict(hw,n.ahead=12),col=2)
43
    mean(abs(hw$fit[,1]-beer)/beer)*100
```

These commands can be used to create a graph with the predictions for the next 1 year1 (i.e. 12 months):



```
beer<-read.csv("~/Downloads/beer.csv",header=T,dec=",",sep=";");</pre>
32
33
34
    beer<-ts(beer[,1],start=1956,freq=12);
35
36
    hw<-HoltWinters(beer)</pre>
37
38
    predict(hw,n.ahead=12)
39
    plot(beer,xlim=c(1956,1996))
41
42
    lines(predict(hw,n.ahead=12),col=2)
43
    mean(abs(hw$fit[,1]-beer)/beer)*100
```

Accuracy is 5.444085%

```
> mean(abs(hw$fit[,1]-beer)/beer)*100
[1] 5.444085
```

ARIMA Model

 ARIMA stands for Auto Regressive Integrated Moving Average.

• It is specified by three order parameters: **p**, **d**, **q**

ARIMA(p,d,q)

ARIMA models are classified by three factors:

p = number of autoregressive terms (AR)

$$x_t = c_1 x_{t-1} + c_2 x_{t-2} + \dots + c_p x_{t-p}$$

Auto Regressive (AR only) model is one where x_t depends only on its own lags.

d = how many non-seasonal differences are needed

$$x_t = c_1 x_{t-1} + c_2 (x_{t-2} - x_{t-1}) + c_3 (x_{t-3} - x_{t-2}) + \dots + c_d (x_{t-d} - x_{t-d})$$

Moving Average (MA only) model is one where x_t depends only on the lagged forecast errors.

As can be seen, the second equation with d can be rewritten as the first equation with p.

q = number of lagged forecast errors in the prediction equation (MA)

Let's do it in R with the same dataset

```
beer<-read.csv("~/Downloads/beer.csv",header=T,dec=",",sep=";");

beer<-ts(beer[,1],start=1956,freq=12);

ar<-arima(beer,order=c(4,0,0))

ar.predict <- predict(ar,n.ahead=12)

ar.predict</pre>
```

R Script

```
beer<-read.csv("~/Downloads/beer.csv",header=T,dec=",",sep=";");
beer<-ts(beer[,1],start=1956,freq=12);

ar<-arima(beer,order=c(4,0,0))

ar.predict <- predict(ar,n.ahead=12)

ar.predict</pre>
```

This performs the ARIMA procedure on the beer – dataset.

Here
$$p = 4$$

 $d = 0$
 $q = 0$

R Script

```
beer<-read.csv("~/Downloads/beer.csv",header=T,dec=",",sep=";");
beer<-ts(beer[,1],start=1956,freq=12);

ar<-arima(beer,order=c(4,0,0))

ar.predict <- predict(ar,n.ahead=12)

ar.predict</pre>
```

This gives us the predicted values for the next 12 periods (i.e. Sep. 1995 to Aug. 1996).



Let's try with Electricity Dataset

- Create our own autoregression
 - same hour of the last week
 - same hour yesterday
 - last four hours
- Use these six hours to predict the next hour

Let's try with Electricity Dataset

Data: electricityPrediction.txt

_	V1 [‡]	V2 [‡]	V3 [‡]	V4 [‡]	V5 [‡]	V6 [‡]	V7 [‡]
1	71.77033	320.57416	401.91388	344.49761	440.19139	440.19139	425.83732
2	62.20096	320.57416	344.49761	440.19139	440.19139	425.83732	397.12919
3	71.77033	358.85167	440.19139	440.19139	425.83732	397.12919	344.49761
4	66.98565	296.65072	440.19139	425.83732	397.12919	344.49761	344.49761
5	66.98565	330.14354	425.83732	397.12919	344.49761	344.49761	311.00478
6	66.98565	287.08134	397.12919	344.49761	344.49761	311.00478	339.71292
7	66.98565	258.37321	344.49761	344.49761	311.00478	339.71292	306.22010
8	66.98565	210.52632	344.49761	311.00478	339.71292	306.22010	315.78947
9	71.77033	196.17225	311.00478	339.71292	306.22010	315.78947	334.92823
10	66.98565	177.03349	339.71292	306.22010	315.78947	334.92823	320.57416
11	71.77033	200.95694	306.22010	315.78947	334.92823	320.57416	315.78947
12	71.77033	162.67943	315.78947	334.92823	320.57416	315.78947	325.35885

Use these six hours to predict the next hour

```
58
    xy<-read.csv("~/Downloads/electricityPrediction.txt",header=F);</pre>
59
60
    ху
61
62
    x=xy[,1:6]
63
64
    y=xy[,7]
65
66
    rg=lm(V7\sim.,xy)
67
68
    rg$coeff
69
    mean(100*abs(y-rg\$fit)/y)
```

Taking first 6 columns as x and last column as y

Use these six hours to predict the next hour

Using all columns except V7 for modeling

Use these six hours to predict the next hour

```
xy<-read.csv("~/Downloads/electricityPrediction.txt",header=F);</pre>
59
60
    ху
61
62
    x=xy[,1:6]
63
64
    y=xy[,7]
65
66
    rg=lm(V7\sim.,xy)
67
68
    rg$coeff
69
    mean(100*abs(y-rg\$fit)/y)
```

Output

Extracting Model coefficients

```
> rg$coeff
(Intercept) V1 V2 V3 V4 V5 V6
-0.3804857237 0.2528230532 0.1679550277 0.0345118162 0.0852869403 -0.0006030161 0.4614112202
```

Use these six hours to predict the next hour

```
xy<-read.csv("~/Downloads/electricityPrediction.txt",header=F);</pre>
59
60
    ху
61
62
    x=xy[,1:6]
63
64
    y=xy[,7]
65
66
    rg=lm(V7\sim.,xy)
67
68
    rg$coeff
69
    mean(100*abs(y-rg\$fit)/y)
```

Accuracy

```
> mean(100*abs(y-rg$fit)/y)
[1] 11.87863
```

```
install.packages("randomForest")
77
    library(randomForest)
78
79
    rf=randomForest(x,y,nodesize=10000)
80
81
82
    rfp=predict(rf,x)
83
    mean(100*abs(y-rfp)/y)
84
85
    rf=randomForest(x,y,nodesize=1000)
86
87
88
    rfp=predict(rf,x)
89
90
    mean(100*abs(y-rfp)/y)
```

Try with Random Forest and nodesize=10000

```
install.packages("randomForest")
77
    library(randomForest)
78
79
80
    rf=randomForest(x,y,nodesize=10000)
81
82
    rfp=predict(rf,x)
83
    mean(100*abs(y-rfp)/y)
84
85
    rf=randomForest(x,y,nodesize=1000)
86
87
    rfp=predict(rf,x)
88
89
90
    mean(100*abs(y-rfp)/y)
```

Accuracy: 12.26945

```
install.packages("randomForest")
77
    library(randomForest)
78
79
80
    rf=randomForest(x,y,nodesize=10000)
81
82
    rfp=predict(rf,x)
83
    mean(100*abs(y-rfp)/y)
84
85
    rf=randomForest(x,y,nodesize=1000)
86
87
88
    rfp=predict(rf,x)
89
    mean(100*abs(y-rfp)/y)
90
```

Change Node Size to 1000

```
install.packages("randomForest")
77
    library(randomForest)
78
79
80
    rf=randomForest(x,y,nodesize=10000)
81
82
    rfp=predict(rf,x)
83
84
    mean(100*abs(y-rfp)/y)
85
    rf=randomForest(x,y,nodesize=1000)
86
87
    rfp=predict(rf,x)
88
89
    mean(100*abs(y-rfp)/y)
90
```

Accuracy: 10.76181

Let us try with train and test set

```
> total=nrow(xy)
                                                        80% for training
> train=0.8*total ·
                                                        20% for testing
> test = 0.2*total
> xyTrain=xy[sample(1:total,train),]
> xyTest=xy[sample(1:total,test),]
> xTrain=xyTrain[,1:6]
> xTest=xyTest[,1:6]
> yTrain=xyTrain[,7]
> yTest=xyTest[,7]
> rg=lm(V7~.,xyTrain)
> mean(100*abs(yTrain-rg$fit)/yTrain)
[1] 11.86982
> ytp=predict(rg,xTest)
> mean(100*abs(yTest-ytp)/yTest)
[1] 11.75274
```

Similarly you can also perform using Random Forest

```
rf=randomForest(xTrain,yTrain,nodesize=10000)
209
210
     rfp=predict(rf,xTrain)
     mean(100*abs(yTrain-rfp)/yTrain)
211
     # [1] 12.60685
212
     rfpt=predict(rf,xTest)
213
214
     mean(100*abs(yTest-rfpt)/yTest)
215 # [1] 12.81233
216
     rf=randomForest(xTrain,yTrain,nodesize=1000)
     mean(100*abs(yTrain-rfp)/yTrain)
217
     # [1] 10.82798
218
219
     rfpt=predict(rf,xTest)
     mean(100*abs(yTest-rfpt)/yTest)
220
221 # [1] 10.99167
```

Thank You