

template class T>

Node<T>* Linked List<T>:: Merge Sort(Node<T>* head)

merge Sorting (&head);

return head;

}

$$T(n) = c_1 (n \log_2 n) + c_2 c_1$$

$$T(n) = O(n \log_2 n)$$

costs	# reces	$O(?)$
c_1	$O(n \log_2 n)$	
c_2	1	

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costs		# times	$O(?)$
C_1			$O(n \log_2 n)$
C_2		1	


```

template <class T>
void LinkedList<T>::mergeSorting(Node<T>*& head) {
    Node<T>* cur = *head;
    Node<T>* first;
    Node<T>* second;
    if (!cur or !cur->getNext()) return;
    findMiddle(cur, &first, &second); //  $\rightarrow O(n)$ 
    mergeSorting(&first);
    mergeSorting(&second);
    *head = mergeBoth(first, second);
}

```

Cost θ	# veces θ $O(?)$
C_1	1
C_2	1
C_3	1
C_4	1
C_5	1
C_6	$T(n/2)$
C_7	$T(n/2)$
C_8	1

$$T(n) = \begin{cases} 1, & n=1 \\ 2T(n/2) + n, & n>1 \end{cases}$$

$$= 2T(n/2) + n$$

$$= 2[2T(n/4) + n/2] + n$$

$$= 2^2 T(n/2^2) + 2n$$

$$= 2^3 T(n/2^3) + 3n$$

$$= 2^k T(n/2^k) + kn$$

$$\frac{n}{2^k} = 1 \Rightarrow n = 2^k \Rightarrow k = \log_2 n$$

$$2^{\log_2 n} T\left(\frac{n}{2^{\log_2 n}}\right) + \log_2 n \cdot n$$

$$n T\left(\frac{n}{n}\right) + n \log_2 n$$

$$T(n) = 1 + n \log_2 n$$

$$T(n) = O(n \log_2 n)$$


```

template <class T>
void LinkedList<T>::findMiddle(Node<T>* cur, Node<T>* first, Node<T>* second)
{
    Node<T>* fast;
    Node<T>* slow;
    slow = cur;
    fast = cur cur->getNext();
    while (fast != nullptr) → fast getNext + 2 until end
    {
        fast = fast->getNext();
        if (fast != nullptr)
        {
            slow = slow->getNext();
            fast = fast->getNext();
        }
    }
    *first = cur;
    *second = slow->getNext();
    slow->setNext(nullptr);
}

```

Best case = worst case $O(n)$

costo	# veces $O(?)$
c_1	1
c_2	1
c_3	1
c_4	1
c_5	n
c_6	n
c_7	n
c_8	n
c_9	n
c_{10}	1
c_{11}	1
c_{12}	1

$\} O(n)$

$$T(n) = c_1(1) + c_2(1) + c_3(1) + c_4(1) + c_5(n) + c_6(n) + c_7(n) + c_8(n) + c_9(n) + c_{10}(1) + c_{11}(1) + c_{12}(1)$$

$$= c_1 + c_2 + c_3 + c_4 + c_5n + c_6n + c_7n + c_8n + c_9n + c_{10} + c_{11} + c_{12}$$

$$T(n) = n(c_5 + c_6 + c_7 + c_8 + c_9) + 1(c_1 + c_2 + c_3 + c_4 + c_{10} + c_{11} + c_{12})$$

$$T(n) = O(n)$$

template <class T> Node<T> * LinkedList::mergeBoth (Node<T> * first, Node<T> * second)	costs	#recs of $\mathcal{O}(?)$
{	c_1	\mathcal{O}
Node<T> * answer = nullptr;	c_2	\mathcal{O}
if (C ! first)		\mathcal{O}
{	c_3	\mathcal{O}
return second;		
}		
else if (C ! second)	c_4	\mathcal{O}
{	c_5	\mathcal{O}
return first;		
}		
if (first->getIpVal() <= second->getIpVal())	c_6	\mathcal{O}
{	c_7	\mathcal{O}
answer = first;	c_8	$T(n+1)$
answer->setNext(mergeBoth (first->getNext(), second->getNext()));		
}		
else		
{	c_9	\mathcal{O}
answer = second;	c_{10}	$T(n+1)$
answer->setNext(mergeBoth (first->getNext(), second->getNext()));		
}		
return answer;	c_{11}	\mathcal{O}
}		

$$T(n) = c_1(1) + c_2(\mathcal{O}) + c_3(\mathcal{O}) + c_4(\mathcal{O}) + c_5(\mathcal{O}) + c_6(\mathcal{O}) + c_7(\mathcal{O}) + c_8(T(n)) + c_9(\mathcal{O}) + c_{10}(T(n)) + c_{11}(\mathcal{O})$$

$$T(n) = \begin{cases} 1, & n=1 \\ 2T(n/2), & n>1 \end{cases}$$

$$2T(n/2), n>1$$

$$2^k T(n/k)$$

$$T(n) = 2T(n/2)$$

$$2^k T(n/k)$$

$$= 2[2T(n/2)]$$

$$n+k=1$$

$$8^2 T(n/8)$$

$$1+k=1$$

$$= 2^3 T(n/8)$$

$$k=0$$

$$= 2^k T(n/8)$$

$$T(n) = \mathcal{O}(n)$$