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# 3D Concept Grounding on Neural Fields

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## Abstract

In this paper, we address the challenging problem of 3D concept grounding (*i.e.* segmenting and learning visual concepts) by looking at RGBD images and reasoning about paired questions and answers. Existing visual reasoning approaches typically utilize supervised methods to extract 2D segmentation masks on which concepts are grounded. In contrast, humans are capable of grounding concepts on the underlying 3D representation of images. However, traditionally inferred 3D representations (*e.g.*, point clouds, voxelgrids and meshes) cannot capture continuous 3D features flexibly, thus making it challenging to ground concepts to 3D regions based on the language description of the object being referred to. To address both issues, we propose to leverage the continuous, differentiable nature of neural fields to segment and learn concepts. Specifically, each 3D coordinate in a scene is represented as a high dimensional descriptor. Concept grounding can then be performed by computing the similarity between the descriptor vector of a 3D coordinate and the vector embedding of a language concept, which enables segmentations and concept learning to be jointly learned on neural fields in a differentiable fashion. As a result, both 3D semantic and instance segmentations can emerge directly from question answering supervision using a set of defined neural operators on top of neural fields (*e.g.*, filtering and counting). Experimental results show that our proposed framework outperforms unsupervised / language-mediated segmentation models on semantic and instance segmentation tasks, as well as outperforms existing models on the challenging 3D aware visual reasoning tasks. Furthermore, our framework can generalize well to unseen shape categories and real scans<sup>\*</sup>.

## 1 Introduction

Consider an image of a table pictured in Figure 1. We wish to construct a method that is able to accurately ground the concepts and reason about the image such as the number of legs the pictured table has. Existing works typically address this problem by utilizing a supervised segmentation model for legs, and then applying a count operator on extracted segmentation masks [19]. However, as illustrated in Figure 1, in many visual reasoning tasks, the correct answer depends on a very small portion of a given image, such as a highly occluded back leg, which many existing 2D segmentation systems may neglect. Humans are able to accurately ground the concepts from images and answer such questions by reasoning on the underlying 3D representation of the image [32]. In this underlying 3D representation, the individual legs of a table are roughly similar in size and shape, without

\*Project page: <http://3d-cg.csail.mit.edu>

Shape & Question	Segmentation	Answer	Shape & Question	Segmentation	Answer
		Answer: 3 X			Answer: 3 X
Question: How many legs does this table have?	Segment Legs		Question: How many wheels does this cart have?	Segment Wheels	

Figure 1: **Issues with 2D Concept Grounding and Visual Reasoning.** Existing methods typically answer questions by relying on 2D segmentation masks obtained from supervised models. However, heavy occlusion leads to incorrect segmentations and answers.

underlying issues of occlusion of different legs, making reasoning significantly easier and more flexible. In addition, such an intermediate 3D representation further abstracts confounding factors towards reasoning, such as the underlying viewing direction from which we see the input shape. To resemble more human-like reasoning capability, in this paper, we propose a novel concept grounding framework by utilizing an intermediate 3D representation.

A natural question arises – what makes a good intermediate 3D representation for concept grounding? Such an intermediate representation should be discovered in a self-supervised manner and efficient to infer, as well as maintain correspondences between 3D coordinates and feature maps in a fully differentiable and flexible way, so that segmentation and concept learning can directly emerge from this inferred 3D representation with natural supervision of question answering. While traditional 3D representations (*e.g.*, point clouds, voxelgrids and meshes) are efficient to infer, they can not provide continuous 3D feature correspondences flexibly, thus making it challenging to ground concepts to 3D coordinates based on the language descriptions of objects being referred to. To address both issues, in this work, we propose to leverage the continuous, differentiable nature of neural fields as the intermediate 3D representation, which could be easily used for segmentation and concept learning through question answering.

To parameterize a neural field for reasoning, we utilize recently proposed Neural Descriptor Fields (NDFs) [30] which assign each 3D point in a scene a high dimensional descriptor. Such descriptors are learned in a self-supervised manner, and implicitly capture the hierarchical nature of a scene, by leveraging implicit feature hierarchy learned by a neural network. Portions of a scene relevant to a particular concept could be then differentiably extracted through a vector similarity computation between each descriptor and a corresponding vector embedding of the concept, enabling concept segmentations on NDFs to be differentiably learned. In contrast, existing reasoning approaches utilize supervised segmentation models to pre-defined concepts, which prevents reasoning on concepts unseen by the segmentation model [19], and further prevents models from adapting segmentations based on language descriptions.

On top of NDFs, we define a set of neural operators for visual reasoning. First, we construct a filter operator, and predict the existence of a particular concept in an image. We also have a query operator which queries about an attribute of the image. In addition, we define a neural counting operator, which quantifies the number of instances of a particular concept. We find that by integrating our neural operators with NDF, our framework is able to effectively and robustly answer a set of visual reasoning questions. Simultaneously, we observe the emergence of natural 3D segmentations of concepts, at the semantic and instance level, directly from the underlying supervision of downstream reasoning.

Our contributions can be summed up as follows: 1) we propose 3D-CG, which utilizes the differentiable nature of neural descriptor fields (NDF) to ground concepts and perform segmentations; 2) we define a set of neural operators, including a neural counting operator on top of the NDF; 3) with 3D-CG, semantic and instance segmentations can naturally emerge from question answering supervision; 4) our 3D-CG outperforms baseline models in both segmentation and reasoning tasks; 5) it can also generalize well to unseen shape categories and real scans.

## 2 Related works

**Visual Reasoning.** There have been different tasks focusing on learning visual concepts from natural language, such as visually-grounded question answering [8, 9] and text-image retrieval [33].

Visual reasoning stands out as a challenging task as it requires human-like understanding of the visual scene. Numerous visual reasoning models have been proposed in recent years. Specifically, MAC [13] combined multi-modal attention for compositional reasoning. LCGN [12] built contextualized representations for objects to support relational reasoning. These methods model the reasoning process implicitly with neural networks. Neural-symbolic methods [37, 19, 1] explicitly perform symbolic reasoning on the objects representations and language representations. Specifically, they use perception models to extract 2D masks for 3D shapes as a first step, and then execute operators and ground concepts on these pre-segmented masks, but are limited to a set of pre-defined concepts. In this paper, we present an approach towards grounding 3D concepts in a fully differentiable manner, with which 3D segmentations can emerge naturally with question answering supervision.

**Neural Fields.** Our approach utilizes neural fields also known as neural implicit representations, to parameterize an underlying 3D geometry of a shape for reasoning. Such fields have been shown to accurately represent 3D geometry [23, 3, 26–28], dynamic scenes [24, 7], and appearance [31, 21, 25, 36, 29], acoustics [17] and more general multi-modal signals [6]. In this work, we utilize descriptors defined on such fields [30] to differentiably reason in 3D.

**Language-driven Segmentation.** Recent works have been focused on leveraging language for segmentation. Specifically, BiLD [10] distills the knowledge from a pre-trained zero-shot image classification model into a two-stage detector. MDETR [14] is an end-to-end modulated detector that detects objects in an image conditioned on a raw text query, like a caption or a question. LSeg [15] uses a text encoder to compute embeddings of descriptive input labels together with a transformer-based image encoder that computes dense per-pixel embeddings of the input image. GroupViT [35] learns to group image regions into progressively larger arbitrary-shaped segments with a text encode. These methods typically use an encoder to encode the text and do not have the ability to modify the segmentations based on the question answering loss. LORL [34] uses the object-centric concepts derived from language to facilitate the learning of object-centric representations. However, they can only improve the segmentation results but cannot generate segmentations from scratch with language supervision.

### 3 3D Concept Grouping

In Figure 2, we show an overall framework of our 3D Concept Grounding (3D-CG), which seamlessly bridges the gap between 3D perception and reasoning by using Neural Descriptor Field (NDF). Specifically, we first use NDF to assign a high dimensional descriptor vector for each 3D coordinate, and run a semantic parsing module to translate the question into neural operators to be executed on the neural field. The concepts, also the parameters of the operators, possess concept embeddings as well. Upon executing the operators and grounding concepts in the neural field, we perform dot product attention between the descriptor vector of each coordinate and the concept embedding vector to calculate the score (or mask probability) of a certain concept being grounded on a coordinate. We also propose a count operator which assigns point coordinates into different slots for counting the number of instances of a part category. Both the NDF and the neural operator have a fully differentiable design. Therefore, the entire framework can be end-to-end trained, and the gradient from the question answering loss can be utilized to optimize both the NDF perception module and the visual reasoning module and jointly learn all the embeddings and network parameters.

#### 3.1 Model Details

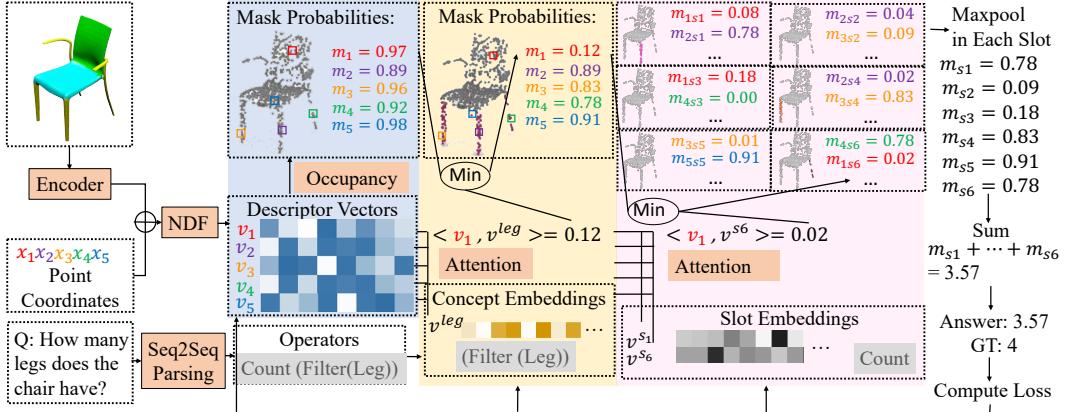
##### 3.1.1 Neural Descriptor Fields

In this paper, we utilize a neural field to map a 3D coordinate  $\mathbf{x}$  using a descriptor function  $f(\mathbf{x})$  and extract the feature descriptor of that 3D coordinate:

$$f(\mathbf{x}) : \mathbb{R}^3 \rightarrow \mathbb{R}^n, \quad \mathbf{x} \mapsto f(\mathbf{x}) = \mathbf{v} \quad (1)$$

where  $\mathbf{v}$  is the descriptor representation which encodes information about shape properties (*e.g.*, geometry, appearance, *etc.*).

In our setting, we condition the neural field on the partial point cloud  $\mathcal{P}$  derived from RGB-D images. We use a PointNet-based encoder  $\mathcal{E}$  to encode  $\mathcal{P}$ . The descriptor function then becomes  $f(\mathbf{x}, \mathcal{E}(\mathcal{P})) = \mathbf{v}$ . This continuous and differentiable representation maps each 3D coordinate  $\mathbf{x}$  to a descriptor vector  $\mathbf{v}$ . Since the concepts to be grounded in most reasoning tasks focus on geometry



**Figure 2: Our 3D Concept Grounding (3D-CG) framework.** Given an input image and a question, 3D-CG first utilizes a Neural Descriptor Field (NDF) to extract a descriptor vector for each 3D point coordinate (here we take 5 coordinates with 5 different colors as examples), and a semantic parsing network to parse the question into operators. The mask probabilities of the coordinates are initialized with occupancy values. Concepts are also mapped to embedding vectors. Attention is calculated between the descriptors and concept embeddings to yield new mask probabilities and filter the set of coordinates being referred as the concept. We also define a count operator which segments a part category into different slots. The sum of the maxpooled mask probabilities of all slots can be used for counting, and the loss can be back propagated to optimize NDF as well as the embeddings. Semantic and instance segmentations naturally emerge with 3D-CG.

and appearance, we leverage two self-supervised pre-training tasks to parameterize  $f$  and learn the features concerning these properties.

**Shape Reconstruction.** Inspired by recent works on using occupancy networks [20] to reconstruct shapes and learn shape representations, we also use an MLP decoder  $\mathcal{D}_1$  which maps each descriptor vector  $\mathbf{v}$  to an occupancy value:  $\mathcal{D}_1 : \mathbf{v} \mapsto \mathbf{o} \in [0, 1]$ , where the occupancy value indicates whether the 3D coordinate is at the surface of a shape.

**Color Reconstruction.** We use another MLP  $\mathcal{D}_2$  to decode an RGB color of each coordinate:  $\mathcal{D}_2 : \mathbf{v} \mapsto \mathbf{c} \in \mathbb{R}^3$ , where the color value indicates the color of the 3D coordinate on the shape.

After learning decoders  $D_i$  through these self-supervised pre-training tasks, to construct the Neural Descriptor Field (NDF)  $f(\mathbf{x})$ , we concatenate all the intermediate activations of  $D_i$  when decoding a 3D point  $\mathbf{x}$  [30]. The resultant descriptor vector  $\mathbf{v}$  can then be used for concept grounding. Since  $\mathbf{v}$  consists of intermediate activations of  $D_i$ , they implicitly capture the hierarchical nature of a scene, with earlier activations corresponding to lower level features and later activations corresponding to higher level features.

### 3.1.2 Concept Quantization

Visual reasoning requires determining the attributes (*e.g.*, color, category) of a shape or shape part, where each attribute contains a set of visual concepts (*e.g.*, blue, leg). As shown in Figure 2, visual concepts such as legs, are represented as vectors in the embedding space of part categories. These concept vectors are also learned by our framework. To ground concepts in the neural fields, we calculate the dot products  $\langle \cdot, \cdot \rangle$  between the concept vectors and the descriptor vectors from the neural field. For example, to calculate the score of a 3D coordinate belonging to the category leg, we take its descriptor vector  $\mathbf{v}$  and compute  $p = \langle \mathbf{v}, v^{leg} \rangle$ , where  $v^{leg}$  is the concept embedding of leg.

### 3.1.3 Semantic Parsing

To transform natural language questions into a set of primitive operators that can be executed on the neural field, a semantic parsing module is incorporated into our framework. This module utilizes a LSTM-based Seq2Seq to translate questions into a set of fundamental operators for reasoning. These operators takes concepts and attributes as their parameters (*e.g.*, Filter(leg), Query(color)).

### 3.1.4 Neural operators on Neural Descriptor Fields

The operators extracted from natural language questions can then be executed on the neural field. Due to the differentiable nature of the neural field, the whole execution process is also fully-differentiable. We represent the intermediate results in a probabilistic manner: for the  $i$ -th sampled coordinate  $\mathbf{x}_i$ , it is represented by a descriptor vector  $\mathbf{v}_i$  and has an attention mask  $\mathbf{m}_i \in [0, 1]$ .  $\mathbf{m}_i$  denotes the probability that a coordinate belongs to a certain set, and is initialized using the occupancy value output by  $\mathcal{D}_1$ :  $\mathbf{m}_i = \mathbf{o}_i$ .

There are three kinds of operators output by the semantic parsing module, we will illustrate how each operator executes on the descriptor vectors to yield the outputs.

**Filter Operator.** The filter operator “selects out” a set of coordinates belonging to the concept  $c$  by outputting new mask probabilities:

$$\text{Filter}(c) : \mathbf{m}_i^c = \min(\mathbf{m}_i, \langle \mathbf{v}_i, v^c \rangle) \quad (2)$$

**Query Operator.** The query operator asks about an attribute  $a$  on selected coordinates and outputs concept  $\hat{c}$  of the maximum probability:

$$\text{Query}(a) : \hat{c} = \arg \max \min(\mathbf{m}_i, \langle \mathbf{v}_i, v^c \rangle), c \in a \quad (3)$$

**Count Operator.** The count operator intends to segment the coordinates in the same part category into instances and count the number of instances. Inspired by previous unsupervised segmentation methods which output different parts in various slots [16, 2], we also allocate a set of slots for different instances of a category. The  $j$ -th slot  $s_j$  has its own embedding vector  $v^s_j$ . The score  $s_{ij}$  of the  $i$ -th coordinate belonging to the  $j$ -th slot is also computed by dot product  $s_{ij} = \langle \mathbf{v}_i, v^s_j \rangle$ . We further take softmax to normalize the probabilities across slots. Since we want to count the instances of a part that was previously selected out, we also take the minimum of previous mask probabilities and the mask probabilities of each slot. The result of counting (*i.e.*, the number of part instances  $n$ ) is obtained by summing up the maximum probability in each slot.

$$\text{Count}(c) : \mathbf{m}_{ij} = \min(\mathbf{m}_i^c, \frac{s_{ij}}{\sum s_{ij}}) \quad (4)$$

$$n = \sum_j \max_i \mathbf{m}_{ij} \quad (5)$$

### 3.1.5 Segmentation

Note that based on the above operators, not only visual reasoning can be performed, but we can also do semantic segmentation and instance segmentation.

**Semantic Segmentation.** We can achieve semantic segmentations by executing `Query(category)` on each coordinate and output the category  $\hat{c}$  with the maximum probability for each point.

**Instance Segmentation.** We can perform instance segmentations by first doing semantic segmentation, and then for each output  $\hat{c}$  we further execute `count( $\hat{c}$ )`.

## 3.2 Training Paradigm

**Optimization Objective.** During training, we jointly optimize the NDF and the concept embeddings by minimizing the loss as:

$$\mathcal{L} = \alpha \cdot \mathcal{L}_{\text{NDF}} + \beta \cdot \mathcal{L}_{\text{reasoning}} \quad (6)$$

Specifically, the NDF loss consists of two parts: the binary cross entropy classification loss between the ground-truth occupancy and the predicted occupancy, and the MSE loss between the ground-truth rgb value and the predicted rgb value.

We also define three kinds of losses for three types of questions: 1) For questions that ask about whether a part exist, we use an MSE loss  $\|a - \max(\mathbf{m}_i)\|^2$  where  $a$  is the ground-truth answer and  $\max(\mathbf{m}_i)$  takes the maximum mask probability among all sampled 3D coordinates; 2) For questions that query about an attribute, we take the cross entropy classification loss between the predicted concept category  $\hat{c}$  and the ground-truth concept category; 3) For counting questions, we first use an MSE loss  $\|a - n\|^2$  between the answer and the number output by summing up the maxpool values

of all the slots, and further add a loss to ensure that the mask probabilities of the top  $K$  values in the top  $a$  slots (*i.e.*, the slots with the maximum maxpool values) should be close to 1, where  $K$  is a hyper-parameter. During training, we first train the NDF module only for  $N_1$  epochs and then jointly optimize the NDF module and the concept embeddings. The Seq2seq model for semantic parsing is trained independently with supervision.

**Curriculum Learning.** Motivated by previous curriculum strategies for visual reasoning [19], we employ a curriculum learning strategy for training. We split the questions according to the length of operators they are parsed into. Therefore, we start with questions with only one neural operator (*e.g.*, “is there a yellow part of the chair” can be parsed into `Filter(Color)`).

## 4 Experiments

### 4.1 Experimental Setup

#### 4.1.1 Dataset

Instead of object-based visual reasoning tasks where objects are spatially disentangled, which makes segmentations quite trivial, we seek to explore part-based visual reasoning tasks where segmentations and reasoning are both harder. To this end, we collect a new dataset, **PartNet-Reasoning**, which focuses on visual question answering on the PartNet [22] dataset. Specifically, we render approximately 3K RGB-D images from shapes of 4 categories: Chair, Table, Bag and Cart, with 8 questions on average for each shape. We have three question types: `exist_part` queries about whether a certain part exists by having the filter operator as the last operator; `query_part` uses query operator to query about an attribute (*e.g.*, part category or color) of a filtered part; `count_part` utilizes the count operator to count the number of instances of a filtered part. We are interested in whether the reasoning tasks can benefit the segmentations of the fine-grained parts, as well as whether the latent descriptor vectors by NDF can result in better visual reasoning.

#### 4.1.2 Evaluation Tasks

**Reasoning.** We report the visual question answering accuracy on the **PartNet-Reasoning** dataset w.r.t the three types of questions on all four categories.

**Segmentation.** We further evaluate both the performances of semantic segmentation and instance segmentation on our dataset. As stated in 3.1.5, semantic segmentation can be performed by querying the part category with the maximum mark probability of each coordinate, and filtering the coordinates according to category labels, and instance segmentation can be achieved by using the count operator on each part category. We report the mean per-label Intersection Over Union (IOU).

#### 4.1.3 Baselines

We compare our approach to a set of different baselines, with details provided in the supp. material.

**Unsupervised Segmentation Approaches.** We compare 3D-CG with two additional 3D unsupervised segmentation models, and further consider how we may integrate such approaches with concept grounding. First, we consider **CVXNet** [5], which decomposes a solid object into a collection of convex polytope using neural implicit fields. In this baseline, a number of primitives are selected and a convex part is generated in each primitive. Next, we consider **BAENet** [2] which decomposes a shape into a set of pre-assigned branches, each specifying a portion of a whole shape. In practice, we tuned with the original codes of BAENet on our dataset and found that nearly all coordinates would be assigned to a single branch. This is probably because the original model is trained on voxel models, while ours is on partial point cloud and contains more complex shapes, thus posing more challenges. Therefore, for BAENet we use an additional loss which enforces that at least some of the branches should have multiple point coordinates assigned to positive occupancy value. The primitives in CVXNet and the branches in BAENet are similar to slots in our paper.

**Reasoning Baselines.** We compare our approach to a set of different reasoning baselines. First we consider **PointNet+LSTM** and **NDF+LSTM**, which use the features by PointNet or our NDF module, concatenated with the features of the questions encoded by a LSTM model. The final answer distribution is predicted with an MLP. Next, we compare with **MAC**, a commonly-used attention-based model for visual reasoning. We add a depth channel to the input to the model. Finally

		PointNet+LSTM	MAC	NDF+LSTM	CVX+L	BAE+L	3D-CG
Chair	exist_part	52.3	65.2	55.7	71.9	72.4	<b>85.4</b>
	query_part	41.6	53.9	54.2	<b>72.3</b>	70.5	68.7
	count_part	63.4	78.1	71.6	48.8	68.0	<b>92.2</b>
Table	exist_part	55.1	66.4	61.3	68.5	71.0	<b>80.3</b>
	query_part	43.6	51.2	54.4	69.7	73.6	<b>75.1</b>
	count_part	35.5	55.3	50.1	30.7	45.7	<b>90.9</b>
Bag	exist_part	65.4	85.4	69.2	87.3	73.8	<b>89.2</b>
	query_part	53.1	74.8	64.0	<b>88.1</b>	70.6	85.2
	count_part	51.2	70.9	<b>72.3</b>	53.4	31.4	68.3
Cart	exist_part	49.7	75.3	61.7	79.1	<b>91.0</b>	90.1
	query_part	50.1	64.0	57.0	72.3	81.5	<b>86.3</b>
	count_part	41.6	<b>82.1</b>	67.3	46.6	47.3	74.8

Table 1: **Visual question answering accuracies.** `exist_part` queries about whether a certain part exists by having the filter operator as the last operator; `query_part` uses query operator to query about an attribute of a filtered part; `count_part` utilizes the count operator to count the number of instances of a filtered part. Point+LSTM, MAC and NDF+LSTM are methods based on neural networks. CVX+L and BAE+L are neural-symbolic methods which pre-segment the masks and ground concepts on the masks. 3D-CG outperforms baseline models by a large margin.

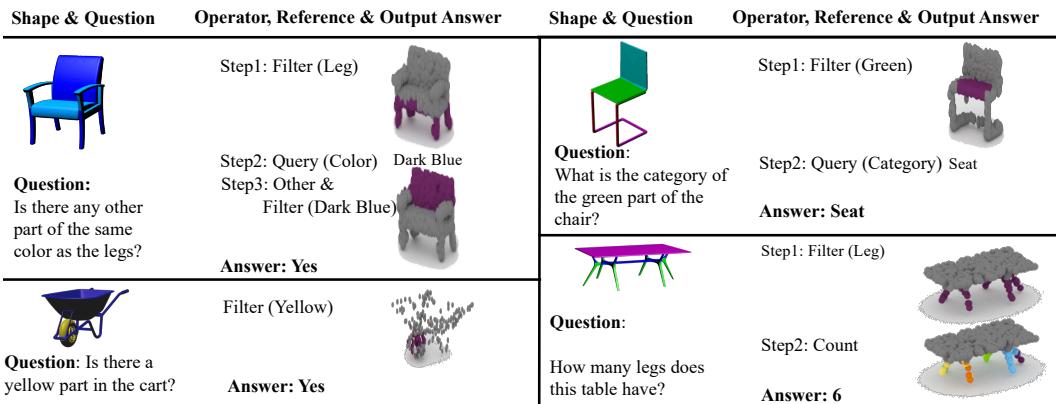


Figure 3: **Qualitative Illustration.** Examples of the reasoning process of our proposed 3D-CG. Given an input image of a shape and a question, we first parse the question into steps of operators. We visualize the set of points being referred to by the operator via highlighting the regions where mask probabilities  $> 0.5$ . As is shown, our 3D-CG can make reference to the right set of coordinates, thus correctly answering the questions.

we compare with **CVX+L** and **BAE+L** are neural-symbolic models that use the similar language-mediated segmentation framework from [34]. Specifically, they first initiate the segmentations in the slots, and each slot has a slot feature vector. The operators from the questions are executed symbolically on the slot features. Question answering loss can be also propagated back to finetune the slot segmentations and features.

**Segmentation Baselines.** For the segmentation tasks, we compare our approach with unsupervised segmentation approaches **CVX** and **BAE** described above. We further construct language-mediated variants **CVX-L** and **BAE-L**. For semantic segmentation by CVX and BAE, we use the manual grouping methods as in [5]. For semantic segmentation by language-mediated models, we use the filter operator to filter the slots belonging to the part categories.

## 4.2 Experimental Results

### 4.2.1 Reasoning & Concept Grounding

Table 1 shows the VQA accuracy among all models on our dataset. We can see that overall, our 3D-CG outperforms baseline models by a large margin. Language-mediated neural-symbolic methods (**CVX+L** & **BAE+L**) are better than neural methods in the `exist_part` and `query_part` question types, but in general they are far worse than our method. This is because the slot-based representations pre-select the parts and make it easier for the concepts to attend to specific regions.

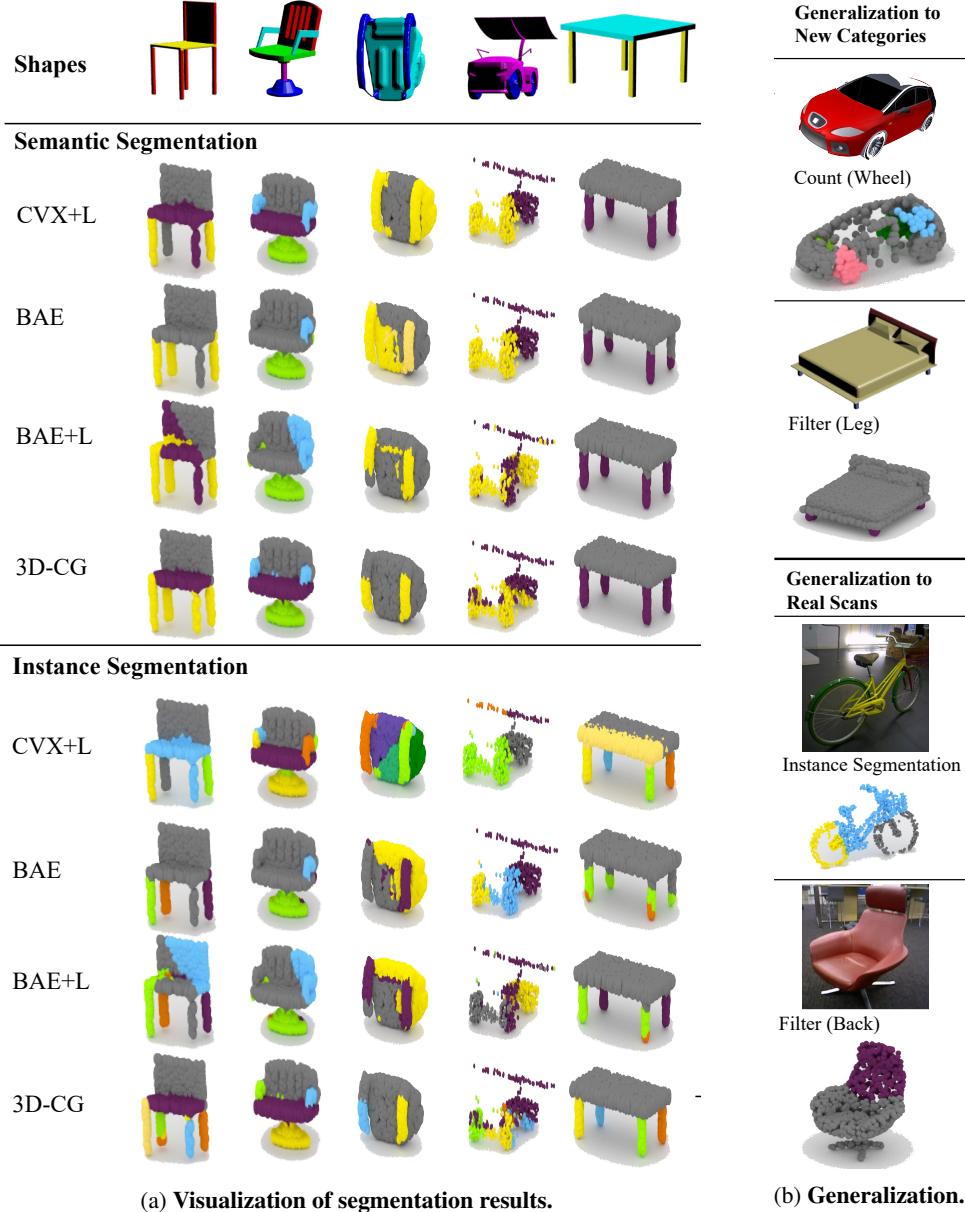


Figure 4: Visualization of segmentation as well as generalization. CVX and BAE are unsupervised segmentation methods. CVX+L and BAE+L are language-mediated methods which utilize question answering loss to finetune the segmentation module. 3D-CG has better performances in both semantic and instance segmentations, while other methods suffer from merging parts or segmenting a part into multiple parts. It can also generalize well to unseen categories and real scans.

However, wrong pre-segmentations are also hard to be corrected during the training of reasoning. The accuracies for the count\_part type further demonstrates this point, where language-mediated baselines have extremely low accuracies, and segmentations from Figure 4a also show that even with supervision from question answering loss, BAE and CVX cannot segment the instances of a part category (e.g., legs and wheels). Neural methods such as MAC and NDF+LSTM perform well in the count\_part type in some categories, probably due to some shortcuts of the PartNet dataset (e.g., most bags have two shoulder straps). In comparison to both neural and neural-symbolic methods, our method performs well in all three question types. This is because the regions attended by concepts are dynamically improved with the question answering loss, while the advantage of explicit disentanglement of concept learning and reasoning process is maintained.

	Chair	Table	Bag	Cart	Mean		Chair	Table	Bag	Cart	Mean
CVX	62.3	74.2	66.0	44.2	61.7	CVX	44.1	40.6	31.2	22.5	34.6
CVX+L	64.6	74.5	<b>70.2</b>	51.3	65.2	CVX+L	42.6	51.2	41.3	20.4	38.9
BAE	49.5	71.0	64.1	49.7	58.6	BAE	53.3	32.2	39.8	34.0	39.9
BAE+L	56.3	72.3	69.8	46.9	61.3	BAE+L	50.1	47.0	34.1	36.6	42.0
3D-CG	<b>76.6</b>	<b>79.3</b>	67.3	<b>54.2</b>	<b>69.4</b>	3D-CG	<b>68.5</b>	<b>71.2</b>	<b>47.2</b>	<b>40.5</b>	<b>56.9</b>

(a) Semantic Segmentation IOU

(b) Instance Segmentation IOU

Table 2: **Segmentation Results.** 3D-CG outperforms all unsupervised / language-mediated baseline models.

Figure 3 shows some qualitative examples of the reasoning process of our method. Specifically, the questions are parsed into a set of neural operators. For each step, the neural operator takes the output of the last step as its input. For the filter operator, we visualize the attended regions with mask probabilities greater than 0.5. From the figure, we can see that our method can attend to the correct region to answer the questions, as well as segment the instances correctly for counting problems. This attention-based reasoning pipeline is also closer than previous neural-symbolic methods to the way that humans perform reasoning. For example, when asked the question “What is the category of the green part of the chair?”, humans would directly pay attention to the green region regardless of the segmentations of the rest of the chair. However, previous neural symbolic methods [37, 19, 34] segment the chair into different parts first and then select the green part, which is very unnatural.

#### 4.2.2 Segmentation

Table 2 shows the semantic segmentation and instance segmentation results, and Figure 4a visualizes some qualitative examples. We can see that overall, our 3D-CG can better segment parts than unsupervised or language-mediated methods. Other methods experience some common problems such as failing to segment the instances within a part category (*e.g.*, one of the legs is always merged with the seat), or experience unclear boundaries and segment one part into multiple parts (*e.g.*, segmenting the chair back or the tabletop into two parts). In general, language-mediated methods are better than pure unsupervised methods, which indicates that the natural supervision of question answering does benefit the segmentation modules. However, a lot of the wrong segmentations cannot be corrected by reasoning, resulting in bad results for counting questions for these models. In contrast, our 3D-CG can learn segmentations well using question answering loss, mainly because the segmentations emerge naturally from scratch without any restrictions.

#### 4.2.3 Generalization

In Figure 4b, we show some qualitative examples of how our 3D-CG trained on seen categories can be generalized directly to unseen categories and real scans. We show results of semantic and instance segmentations, as well as visualize the parts that are referred to in the questions.

For generalizing to new categories, we use the model trained on carts to ground and count the instances of the concept “wheel” in cars. We can see that the instance segmentation results on the wheels are not perfect because one wheel is in wrong position. However, most of the wheels are detected and the model manages to output the right count. We also use the model trained on chairs to filter the legs of a bed. All the legs are successfully selected out by our 3D-CG.

We also use real 3D scans from the RedWood dataset [4] to estimate 3D-CG’s ability to generalize to real scenes. We use a single-view scan to reconstruct partial point cloud and remove the background such as the floor. We input the partial point cloud into our 3D-CG and output the segmentations on the ground-truth voxels. For generalizing to bicycles, we use the 3D-CG model trained on carts. We can see that 3D-CG can find all instances in the bicycle and detect both wheels. Furthermore, 3D-CG trained on chairs can also be generalized to chairs in real scans.

## 5 Discussion

**Conclusion.** In this paper, we propose 3D-CG, which leverages the continuous and differentiable nature of neural descriptor fields to segment and learn concepts in the 3D space. We define a set of neural operators on top of the neural field, with which not only can semantic and instance segmentations emerge naturally, but visual reasoning can also be well performed.

**Limitations and Future Work.** An limitation of our underlying framework with 3D-CG is that while we show transfer results on real scenes, our approach is only trained with synthetic scenes and questions. While we believe our proposed operations is general-purpose, an interesting direction of future work would be scale our framework to directly train on complex real-world scenes, and ground more concepts from natural language on these real scenes is worth delving into in the future.

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## Overview

In this appendix, we supplement our paper by providing more qualitative examples and details about our model to help readers better understand our paper.

This appendix is organized as follows.

- In Sec. A, we provide more qualitative examples about how 3D-CG performs reasoning steps.
- In Sec. B, we provide more details about our 3D-CG model, including the detailed architecture of NDF, the semantic parsing module and the curriculum learning strategies.
- In Sec. C, we provide more details about the baselines models.
- In Sec. D, we discuss the potential societal impacts of this paper.

## A More Qualitative Examples

### A.1 QA Examples

In Figure 5, we show more examples of the reasoning process of 3D-CG. We can see that overall, our model can make reference to the correct region to answer the questions, although sometimes the segmentation might be a little noisy (*e.g.*, for the bag a part of the shoulder strap is not highlighted, and the highlighted part of cart contains part of the wheel.). Also, for counting problems, we can see that our model can segment the legs and make the right prediction. However, for the chair with five legs, although our model can assign five colors to five legs, some of the legs are overlapped with each other by colors.

Shape & Question	Operator, Reference & Output Answer	Shape & Question	Operator, Reference & Output Answer
	Step 1: Filter (back) Step 2: Query (Color) Dark Blue Step 3: Other & Filter (Dark Blue) Answer: Arm		Filter (leg) Question: Does this table have any legs? Answer: No
	Step 1: Filter (leg) Step 2: Count Question: How many legs does this chair have? Answer: 4		Step 1: Filter (leg) Step 2: Count Question: How many legs does this chair have? Answer: 5
	Step 1: Filter (body) Query (color) Answer: Cyan		Step 1: Filter (pink) Step 2: Query (category) Handle Question: What is the category of the purple part of the bag? Answer: Handle
			Filter (shoulder strap) Question: Does this bag have any shoulder straps? Answer: Yes

Figure 5: More qualitative examples that illustrate the reasoning process of 3D-CG. Given an input image of a shape and a question, we first parse the question into steps of operators. We visualize the set of points being referred to by the operator via highlighting the regions where mask probabilities  $> 0.5$ . As is shown, our 3D-CG can make reference to the right set of coordinates, thus correctly answering the questions.

## B Details on 3D-CG

### B.1 NDF

We first train the reconstruction task solely for 50,000 iterations.

For encoder, we use a PointNet-based encoder network with ResNet blocks. We first map the 6-dim ( $x, y, z, r, g, b$ ) point cloud to 128-dim features, followed by several pooling and leaky relu layers. We then go through another fully-connected layer to get 256-dim features. We use 5 resnet fully connected blocks, each with input dim 256 and output dim 128. At each step the output is concatenated with the input to produce the input of the next step. A final fully-connected layer maps the feature back to 128.

For the decoder, we first concatenate the coordinates and the point cloud latent feature vector. The new input is passed through 5-layer resnet blocks. All the resnet blocks have a hidden size of 128. The features of the blocks are concatenated together and passed through a fully-connected layer to produce the occupancy value. For color reconstruction, the features further go through 3 linear layers with hidden size 128 and produce  $r, g, b$  value. The batch size is 4. The learning rate is 1e-4. All embeddings have the dim 2049.

### B.2 Semantic Parsing

Our semantic parser is an attention-based sequence to sequence (seq2seq) model with an encoder-decoder structure similar to that in [18]. The encoder is a bidirectional LSTM [11]. The decoder is a similar LSTM that generates a vector from the previous token of the output sequence. Both the encoder and decoder have two hidden layers with a 256-dim hidden vector. We set the dimensions of both the encoder and decoder word vectors to be 300.

### B.3 Curriculum learning

In Figure 6, we show detailed strategies of curriculum training for 3D-CG. During the whole training process, we gradually add more visual concepts and more complex question examples into the model, which is shown in Figure 6. In general, the whole training process is split into 3 stages. First, we learn color concepts. We want to learn individual concepts like `red` or `seat`. However, since most chairs contain certain parts like `back` and `seat`, we therefore learn the color concepts first by asking questions like “Is there a red part in the chair?” For the second lesson, after learning about color concepts like in the figure, we can then attend to the red region, and we can ground different part categories by asking questions like “What is the category of the red part?”. Finally, we can train more complex questions altogether. Each lesson is trained for approximately 50,000 iterations.

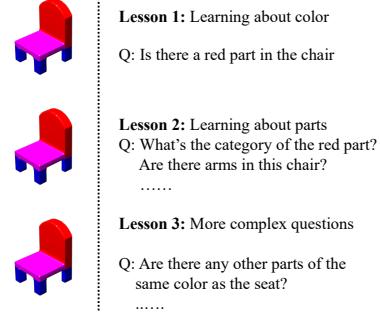


Figure 6: The curriculum learning strategy of 3D-CG.

## C Details on Baseline Models

### C.1 Details on Language-mediated models

We explain in detail how CVX-L and BAE-L work for segmentation and reasoning, as is shown for Figure 7. As the original CVX/BAE model, we use the same NDF as in 3D-CG, except that instead of decoding the descriptor vectors into  $N*1$  occupancy values, we first decode them into  $N*S$  occupancy values for different slots, and then maxpool to get the overall occupancy values for reconstruction. For reasoning, the descriptor vectors of each slot is mean pooled to get a part-centric representation. The question also goes through a semantic parsing module like 3D-CG, and attention is calculated between the concept embedding vector and the descriptor vector of each slot to identify whether the part in one slot can be accounted for a concept. The reasoning loss can also be back-propagated to the NDF module and the concept embeddings. We use the same curriculum learning strategy as 3D-CG and train for the same number of epochs.

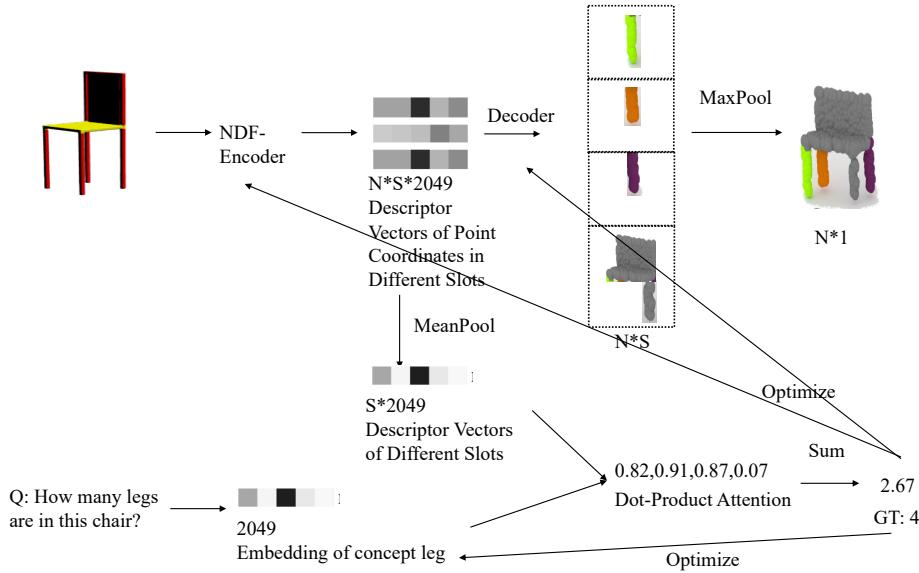


Figure 7: Detailed framework of CVX-L / BAE-L, where  $N$  denotes the number of sampled points, and  $S$  denotes the number of slots.

### C.2 Neural-network based baselines

For MAC, we use an ImageNet-pretrained ResNet-101 to extract  $14 \times 14 \times 1024$  feature maps for MAC. For PointNet+LSTM, we use a 2048 dimensional feature from the last layer. For NDF+LSTM, we mean-pool the descriptor vectors of all point coordinates to get 2049-dimensional vectors. All models are trained for 50 epochs.

## D Societal Impacts

Our work is of broad interest to the computer vision and machine learning communities. Our proposed no inherent ethical or societal issues on its own, but inherit those typical of learning methods, such as capturing the implicit biases of data. Our work aims to enable more interpretable reasoning, and may serve as an inspiration for works that aims to perform less black-box reasoning with gradient-based learning.