

Student Id:
Name Surname:
Signature:

10.03.2016

BLG311E – FORMAL LANGUAGES AND AUTOMATA

2016 SPRING

QUIZ 2

Consider the statement $ts(\alpha) \subseteq st(\alpha)$. Prove the statement if correct. Give a counter example over the set $A = \{a, b, c, d\}$ if wrong.

Duration: 15 mins

Solution:

Counter example:

$$\alpha = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix} \quad s(\alpha) = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix} \quad ts(\alpha) = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \end{bmatrix}$$
$$t(\alpha) = \begin{bmatrix} 0 & 1 & 1 & 1 \\ 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix} \quad st(\alpha) = \begin{bmatrix} 0 & 1 & 1 & 1 \\ 1 & 0 & 1 & 1 \\ 1 & 1 & 0 & 1 \\ 1 & 1 & 1 & 0 \end{bmatrix} \quad ts(\alpha) \not\subseteq st(\alpha)$$