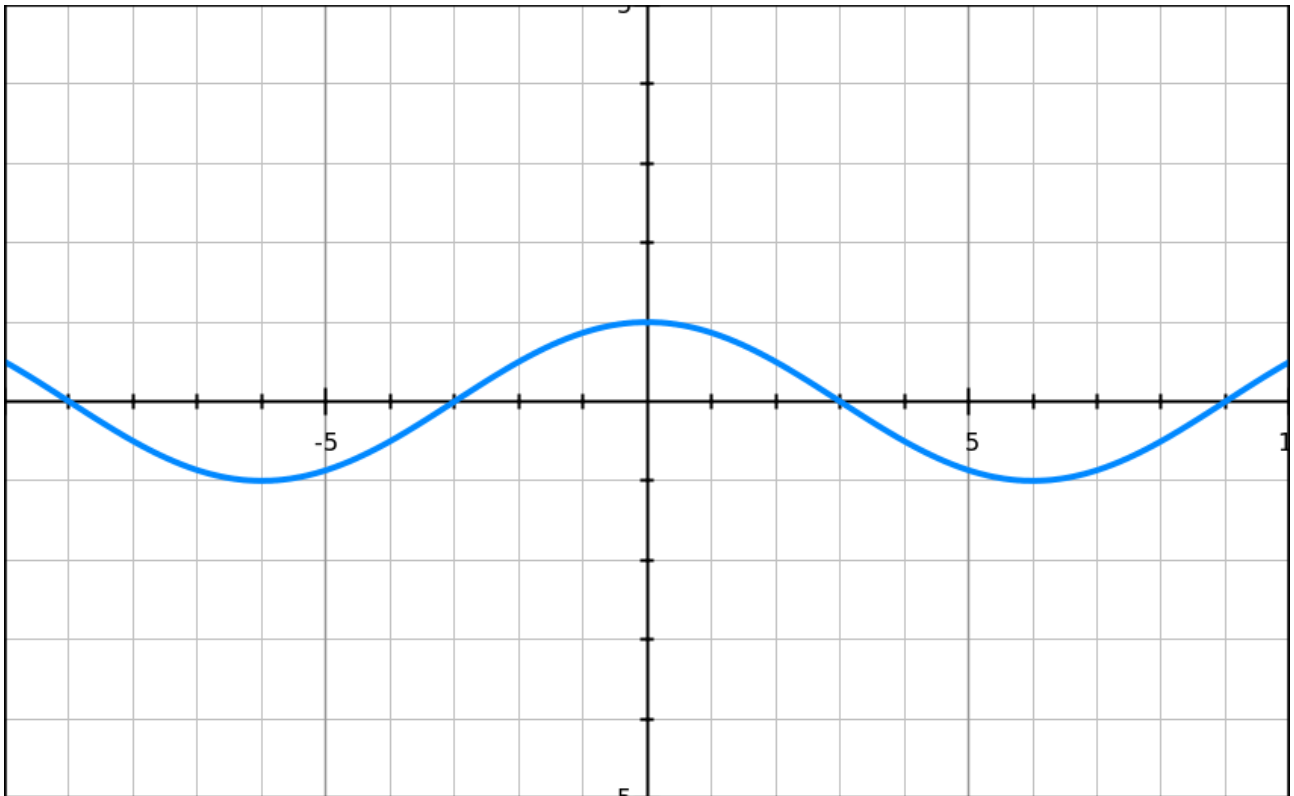
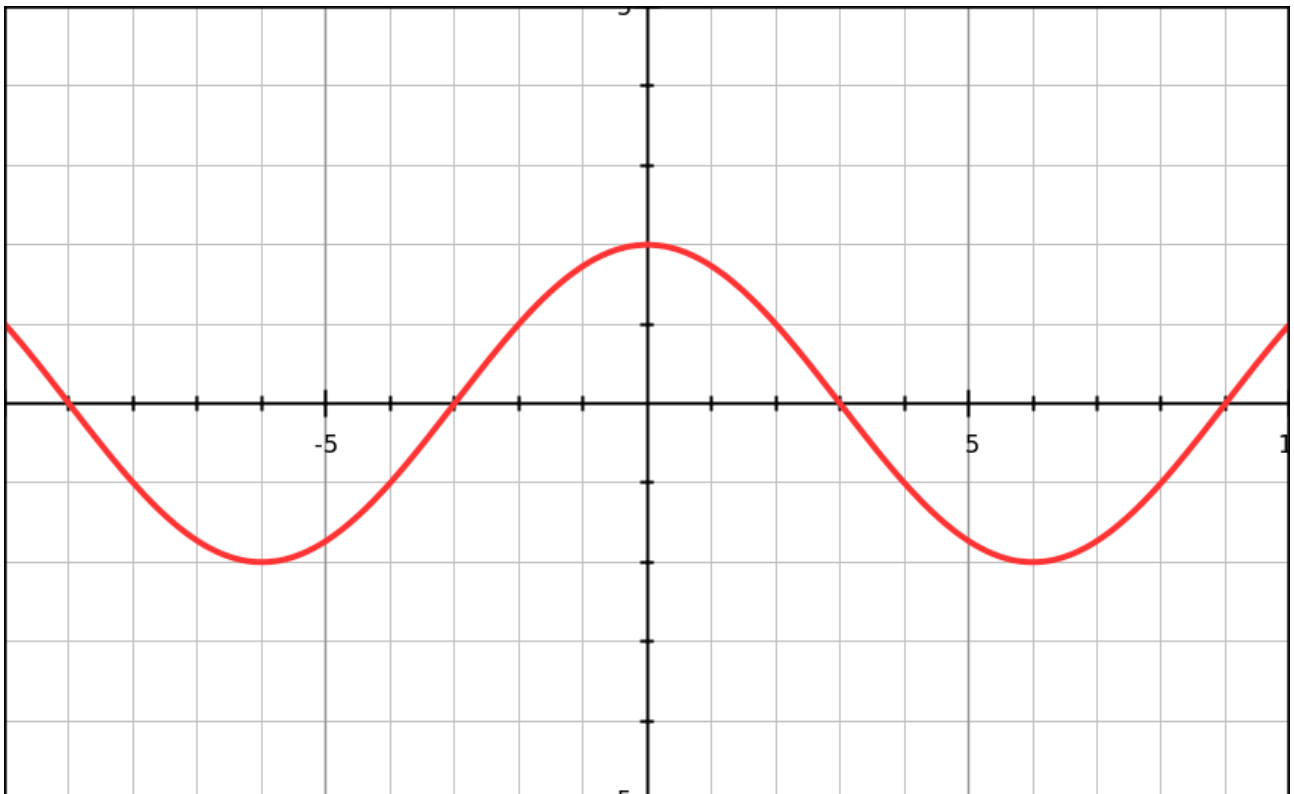


**BLG 354E HW1**  
**Baran Kaya 150130032**

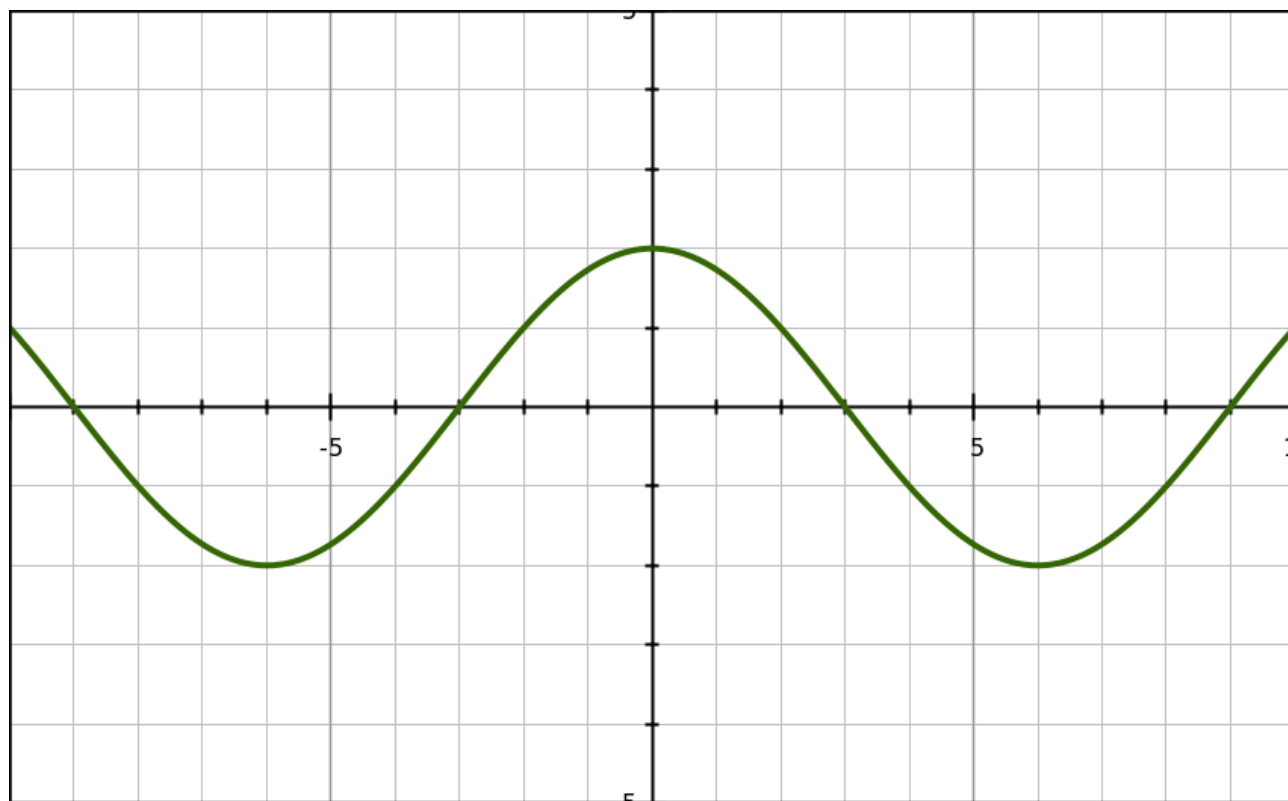
1) ID: 1       $\cos((\pi/6)*x)$



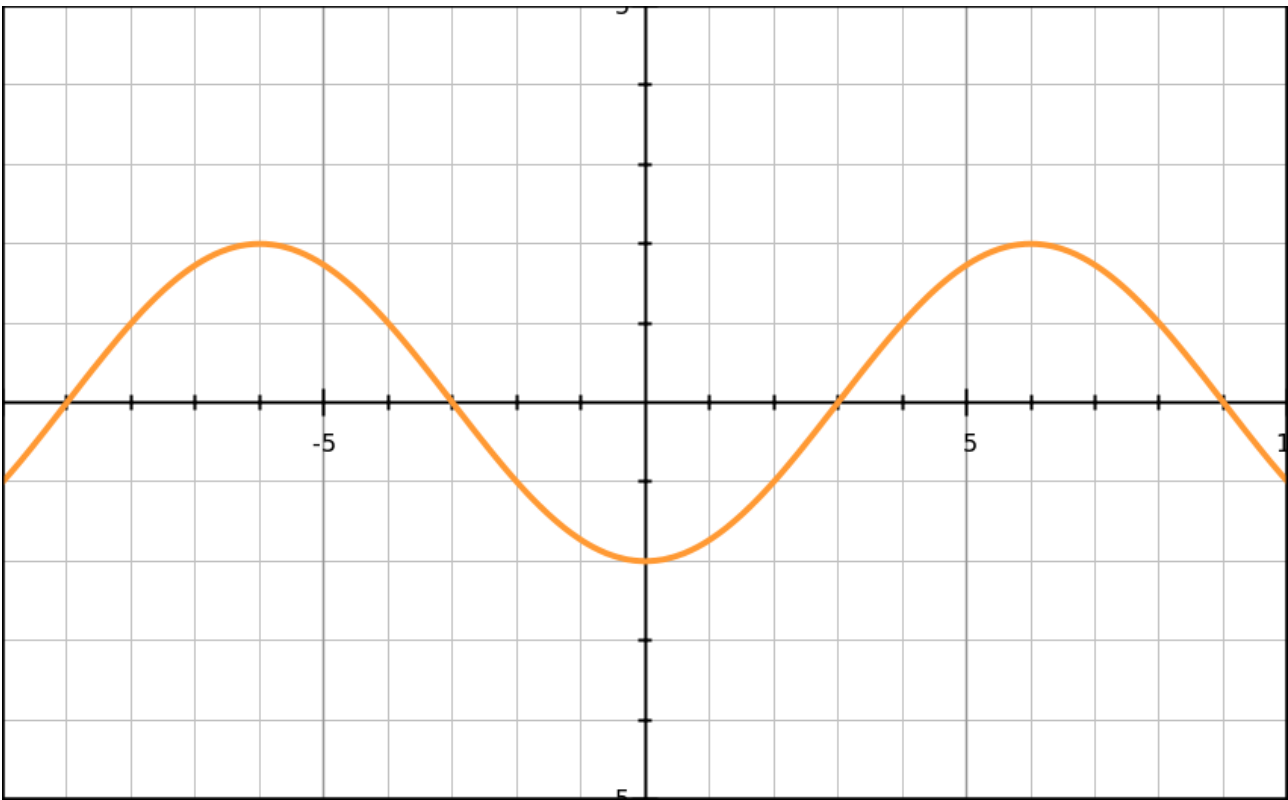
ID: 2       $2*\cos((\pi/6)*x)$



ID: 3       $2\cos((\pi/6)x+(4\pi))$

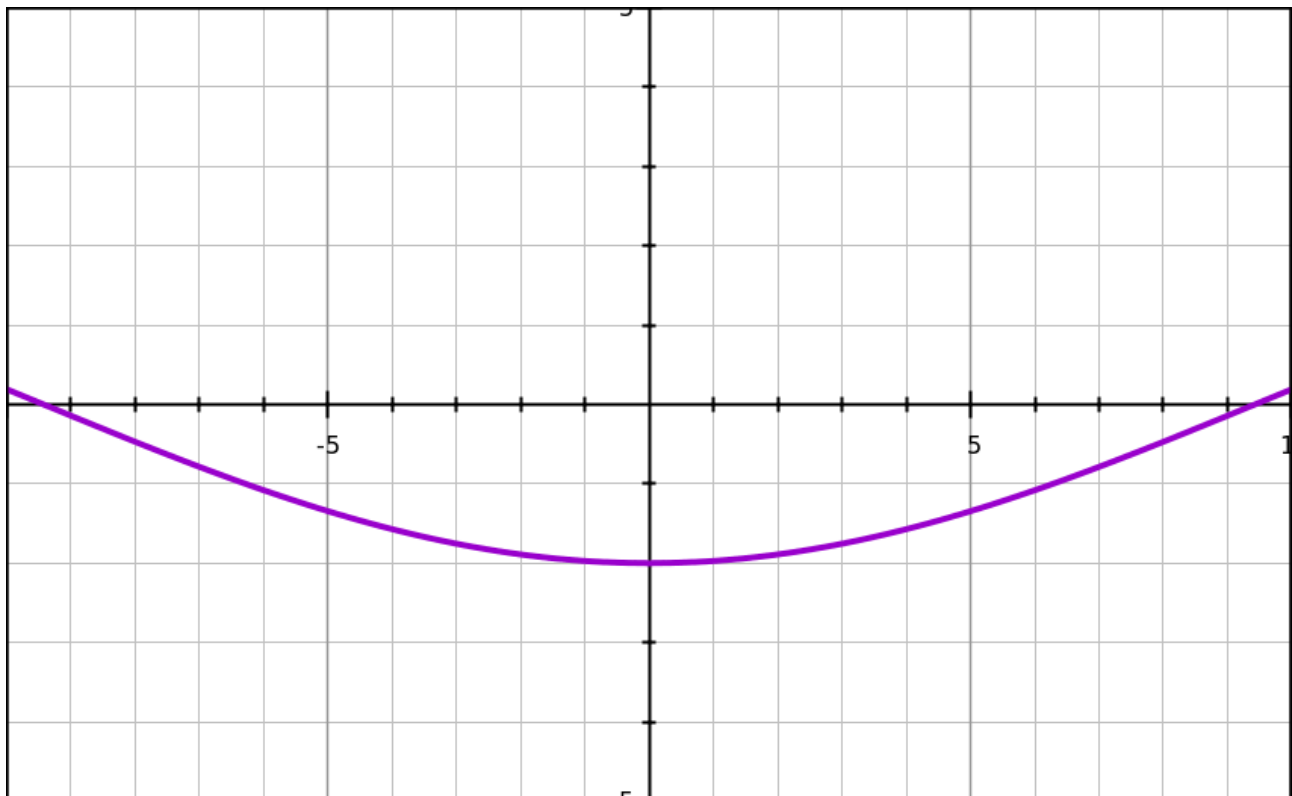


ID: 4       $2\cos((\pi/6)x+\pi)$



ID: 5

$$2\cos((1/6)x + \pi)$$



- 1st and the 2nd signals' difference is amplitude.
- 2nd and 3rd signals are the same. 3rd one is time-shifted. Period is  $2\pi$  and that is why they are looking the same.
- 3rd and 4th signals' difference is their  $\phi$  value. Period is  $2\pi$  and 4th signal's shift is just  $\pi$ .
- 4th and 5th signals' difference is  $\phi$  value.  $1/6$  is bigger than  $\pi/6$ . That is why 5th signal's x coordinates are bigger than 4th one.

**Update:** These graphs plotted like cts-time ones but they have to be discrete-time graphs.

2)  $x_1 = \cos(t)$ ,  $x_2 = \sin(\pi t)$

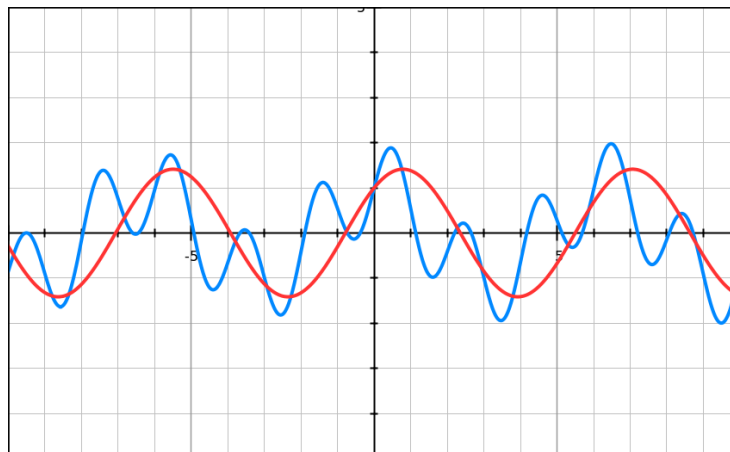
a)  $x_1$  period =  $2\pi / \omega_0 = 2\pi / 1 = 2\pi$

$x_2$  period =  $2\pi / \omega_0 = 2\pi / \pi = 2$

b)  $x_3(t) = x_1(t) + x_2(t) = \cos(t) + \sin(\pi t)$

- Period of  $x_3 = 2\pi / 2 = \pi \rightarrow$  It is irrational it cannot be periodic.

Blue:  $x_3(t)$     Red:  $\cos(t) + \sin(t)$



### 3) In rar file

4)  $y(t) = t \cdot u(t) \cdot x(t)$

a)  $x_1 \rightarrow y_1, x_2 \rightarrow y_2$  then  $a \cdot x_1 + b \cdot x_2 \rightarrow a \cdot y_1 + b \cdot y_2$

$$y_1(t) = t \cdot u(t) \cdot x_1(t)$$

$$y_2(t) = t \cdot u(t) \cdot x_2(t)$$

$$x_3 = x_1 + x_2 = t \cdot u(t) \cdot x_1(t) + t \cdot u(t) \cdot x_2(t)$$

$$y_3 = t \cdot u(t) \cdot x_3(t) = t \cdot u(t) \cdot (x_1(t) + x_2(t)) = t \cdot u(t) \cdot x_1(t) + t \cdot u(t) \cdot x_2(t)$$

- They are equal ( $y_3$  and  $x_3$ ) so this system is linear.

b) This system is memoryless because system does not require previous time  $x(t)$  data (et.  $x(t-1)$ ).

c) This system is casual because system does not require future time  $x(t)$  data. It only uses present time's data (et.  $x(t+2)$ ).

d)  $x(t) = t \cdot u(t) \cdot x(t)$

$$x(t-t_0) = t \cdot u(t) \cdot x(t-t_0)$$

$$y(t) = t \cdot u(t) \cdot x(t)$$

$$y(t-t_0) = (t-t_0) \cdot u(t-t_0) \cdot x(t-t_0)$$

- They are not equal ( $x(t-t_0)$  and  $y(t-t_0)$ ) so this system is time-variant.

### 5) In rar file

