

left as an exercise to the reader