

$$(1) \hat{p} = \frac{105}{250} = 0.42$$

$$0.42 \pm Z_{0.05} \sqrt{\frac{0.42 \times 0.58}{250}} = 0.42 \pm 1.645 \times 0.03$$
$$= 0.42 \pm 0.05 \Rightarrow (0.37, 0.47)$$

$$(2) (a) \hat{p} = 0.3 \quad 1 - \alpha = 0.95, \quad e = \frac{\sigma}{\sqrt{n}} \times 2$$

$$n = \left(\frac{Z}{e}\right)^2 \times \hat{p} \times (1 - \hat{p})$$

$$n = \left(\frac{1.96}{0.03}\right)^2 \times 0.3 \times 0.7 = 896.37 \div 897$$

$$(b) \hat{p} = 0.42$$

$$n = \left(\frac{1.96}{0.03}\right)^2 \times 0.42 \times 0.58 = 1,039.99 \div 1040$$

$$(c) \hat{p} = 0.5$$

$$n = \left(\frac{1.96}{0.03}\right)^2 \times 0.5 \times 0.5 = 1057.11 \div 1058$$