

Week 6.

(4) 偉力公司生產函數 $q = 10L^{0.5}K^{0.5}$ 且 $w=r=10$ 但 K 被固定為 K_0 .

(A) 求 STC , VC , MC .

$$q = 10L^{0.5}K^{0.5} \rightarrow L^* = \frac{q^2}{100K}$$

$$STC = 10L^* + 10K = \frac{q^2}{10K} + 10K$$

$$AC = q/10K + 10K/q, \quad MC = q/5K$$

(B) 由 (A) 反推 TC .

$$\frac{\partial STC}{\partial K} = \frac{-q^2}{10K^2} + 10 = 0 \quad K = \frac{q}{10} \quad \text{代入 } STC$$

$$TC = STC(K = \frac{q}{10}) = \frac{q^2}{10 \times (\frac{q}{10})} + 10 \times \frac{q}{10} = q + q = 2q$$

(7) $TC = q^3 - 12q^2 + q + 50$

(A) $q=10$ 的 AFC .

$$AFC = \frac{50}{10} = 5 = \frac{FC}{q}$$

(B) $AVC = q^2 - 12q + 1 \Rightarrow \frac{\partial AVC}{\partial q} = 2q - 12 = 0 \Rightarrow q = 6$

(C) 根據生產與成本對偶性.

當 AVC 遞增, APL 遞減, $\text{ans} \Rightarrow q \geq 6$.

(D) $MC = 3q^2 - 24q + 1 \Rightarrow \frac{\partial MC}{\partial q} = 6q - 24 = 0 \Rightarrow q = 4$

根據生產與成本對偶性, MC 遞增時, MP_L 遞減, ans 為 $q \geq 4$.

Week6

Q4&Q7