

Week 6.

4.  $q = 10L^{0.5}K^{0.5}$   $w=r=10$   $\bar{K}_0$

(A)  $q = 10L^{0.5}K^{0.5} \rightarrow L^* = \frac{q^2}{100K}$

$$STC = 10L^* + 10K = \frac{q^2}{100K} + 10K$$

$$AC = \frac{q}{10K} + \frac{10K}{q}$$

$$MC = \frac{q}{5K}$$

(B)  $\frac{\partial STC}{\partial K} = \frac{-q^2}{10K^2} + 10 = 0 \rightarrow \bar{K} = \frac{q}{10}$

$$TC = STC = \frac{q^2}{10(\frac{q}{10})} + 10\frac{q}{10} = 2q$$

7.  $TC = q^3 - 12q^2 + q + 50$

(A)  $\frac{50}{10} = \frac{TC}{q} = 5$

(B)  $AVC = q^2 - 12q + 1 \rightarrow \frac{dAVC}{dq} = 2q - 12 = 0 \rightarrow q = 6$

(C)  $AVC \uparrow \rightarrow AP_L \downarrow, q \geq 6$

(D)  $MC = 3q^2 - 24q + 1 \rightarrow \frac{dMC}{dq} = 6q - 24 = 0 \rightarrow q = 4$   
 $MC \uparrow \rightarrow MP_L \downarrow, q \geq 4$