

$$\textcircled{1} \quad MRS_{XY} = \frac{\frac{\partial Y}{\partial X}}{\frac{\partial X}{\partial Y}} = \frac{P_X}{P_Y} = \frac{10}{20}$$

$$\Rightarrow 10X = 20Y \Rightarrow X = 2Y$$

$$\textcircled{2} \quad Y = \frac{1}{2}X \text{ 代入 } 10X + 20Y = M$$

$$10X + 10X = M \Rightarrow X = \frac{M}{20}$$

$$\textcircled{3} \quad \text{Max. } U = P(X, Y) = X^2Y$$

$$\text{s.t. } 300 = P_X X + 20Y$$

$$MRS_{XY} = \frac{\partial Y}{\partial X} = \frac{P_X}{20} \Rightarrow Y = \frac{P_X}{40} X \text{ 代入預算限制式}$$

$$300 = P_X X + 20 \left(\frac{P_X}{40} X \right) \Rightarrow X = \frac{200}{P_X}$$

④ 根據所得消費線與恩格爾曲線可知 X 財貨為
正常品，由需求線可知 X 財貨符合需求法則。