

$$\text{Max } U = f(X, Y) = X^{\frac{2}{3}} Y^{\frac{1}{3}}$$

$$\text{s.t. } 300 = 10X + 20Y$$

$$X=20, Y=5$$

奶茶 ↑ 20 元

$$\Rightarrow \text{s.t. } 300 = 20X + 20Y$$

$$MR_{XY} = \frac{\frac{2Y}{X}}{\frac{1}{Y}} = \frac{P_X}{P_Y} = \frac{20}{20} = 1$$

$$Y = \frac{1}{2} X$$

$$\text{最適: } X=10, Y=5$$

$$U = X^{\frac{2}{3}} Y^{\frac{1}{3}} = 20^{\frac{2}{3}} \cdot 5^{\frac{1}{3}} = 2000^{\frac{1}{3}}, Y = \frac{1}{2} \text{ 代入}$$

$$U = \left(\frac{1}{2} X^3\right)^{\frac{1}{3}} = 2000^{\frac{1}{3}}$$

$$X = (4000)^{\frac{1}{3}} \approx 15.87401, Y = (500)^{\frac{1}{3}}$$

$$\text{替代效果: 由 } (X, Y) = (20, 5) \Rightarrow (4000)^{\frac{1}{3}}, (500)^{\frac{1}{3}}$$

$$X \text{ 的替代效果} = 4000^{\frac{1}{3}} - 20 < 0$$

$$\text{所得效果: 由 } (X, Y) = (4000)^{\frac{1}{3}}, (500)^{\frac{1}{3}} \Rightarrow (10, 5)$$