

習題 3

(A)

$$\begin{aligned} MR_A = MC : 100 - 2q_A = 20 &\Rightarrow q_A = 40 \Rightarrow P_A = 60 \\ MR_B = MC : 80 - 2q_B = 20 &\Rightarrow q_B = 30 \Rightarrow P_B = 50 \end{aligned}$$

(B)

$$\begin{aligned} \text{Max } \pi &= TR - TC \\ q^* &= p(q) \cdot q - TC(q) \\ &= (90 - 0.5q) \cdot q - 20q \\ \frac{\partial \pi}{\partial q} &= 0 \Leftrightarrow q^* = 70, p^* = 55 \\ q^* = 70, p^* = 55 &\Rightarrow \pi^* = 55 \times 70 - 20 \times 70 = 2450 = PS \\ CS &= CS_A + CS_B \\ &= \frac{1}{2} (100 - 55) \times 45 + \frac{1}{2} (80 - 55) \times 25 \\ &= 1012.5 + 312.5 = 1325 \\ SW &= PS + CS = 1325 + 2450 = 3775 \end{aligned}$$

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$$\begin{aligned} \text{Max } \pi &= \text{基本費} + \text{使用費} = 2[CS_B] + [P - 20](q_A + q_B) \\ CS_B &= (80 - P) \times q_B / 2 = \frac{(80 - P)^2}{2} \\ \text{H) } U &= (P - 20)(180 - 2P) \\ \text{Max } \pi &= 2CS_B + U \\ &= -P^2 + 60P + 2800 \\ \frac{\partial \pi}{\partial P} &= 0, P^* = 30 \\ CS_B &= 1250 \\ q_A &= 70, q_B = 50, Q = 120 \\ \pi &= 3700 = PS \\ CS &= CS_A + CS_B \\ &= \frac{1}{2} (100 - 30) \times 70 + \frac{1}{2} (80 - 30) \times 50 \\ &= 3700 \\ CS^* &= CS - 2F = 3700 - 2F = 1200 \\ SW &= \pi + CS^* = 3700 + 1200 = 4900 \end{aligned}$$