

$$\frac{dQ}{dL} = \frac{d}{dL} (10L + 16L^2 - 2L^3) = 10 + 32L - 6L^2$$

$$\frac{dAP_L}{dL} = \frac{d}{dL} \left(\frac{Q}{L} \right) = \frac{d}{dL} \left(10 + 16L - 2L^2 \right) = 16 - 4L$$

$$\frac{dMP_L}{dL} = \frac{d}{dL} \left(\frac{dQ}{dL} \right) = \frac{d}{dL} (10 + 32L - 6L^2) = 32 - 12L$$

3. $Q = 10L + 16L^2 - 2L^3$ $K=1$

TP_L $\frac{dQ}{dL} = 10 + 32L - 6L^2$

AP_L $\frac{Q}{L} = 10 + 16L - 2L^2$

MP_L $\frac{dAP_L}{dL} = 16 - 4L$

$\frac{dQ}{dL} = 10 + 32L - 6L^2$

$\frac{dAP_L}{dL} = 16 - 4L$

$\frac{dMP_L}{dL} = 32 - 12L$

k	L	Q	AP _L	MP _L
20	0	0	0	0
20	5	20	4	4
20	10	43	4.7	4.6
20	15	57	3.8	2.8
20	20	67.5	2	2
20	25	75	3	1.6

2. $Q = 21L + 9L^2 - L^3$

TP_L $= 21 + 18L - 3L^2$

AP_L $= 21 + 9L - L^2 \Rightarrow 9 - 2L = 0, L = 4.5$

MP_L $= 21 + 18L - 3L^2 \Rightarrow 18 - 6L = 0, L = 3$

3. $MP_L = 5$
 $Q = 500$
 $500 = f(10, 5)$

4. (A) $Q = 5A + 10B$
 (B) $m(\frac{L}{2}, K)$

111-164