432 Class 8 Slides

github.com/THOMASELOVE/2019-432

2019-02-19

Setup

```
library(broom); library(janitor); library(Epi)
library(skimr); library(simputation); library(ROCR)
library(Hmisc); library(rms) # the key for lrm
library(tidyverse)
```

Today's Materials

- A new logistic regression example
 - Modeling 10-year risk of coronary heart disease
 - based on a sample from the Framingham Heart Study

```
fram <- read_csv("data/fram_new.csv") %>% clean_names()
```

Codebook (4,240 subjects, 17 variables)

Variable	Interpretation (at baseline)	NAs
subj	subject ID code	0
sex	F or M	0
age	in years	0
smoker	current smoker?	0
cigs_day	mean cigarettes smoked per day	29
bp_meds	on at least one BP medication?	53
hx_stroke	history of stroke?	0
$\mathtt{hx}\mathtt{_htn}$	history of hypertension?	0
hx_dm	history of diabetes?	0
educ	4 ordered levels (1-4)	105

- variables with ? in Interpretation are 1 = yes, 0 = no
- educ: 1 = some HS, 2 = HS diploma, 3 = some college, 4 = college grad

Codebook (4,240 subjects, 17 variables)

Variable	Interpretation	NAs
tot_chol	baseline total cholesterol, mg/dl	50
sbp	baseline mean systolic BP, mm Hg	0
dbp	baseline mean diastolic BP, mm Hg	0
bmi	baseline body mass index, kg/m^2	19
heart_r	baseline heart rate, beats/min	1
glucose	baseline glucose level, mg/dl	388
chd_10	CHD in 10 years after baseline?	0

- Goal 1. Predict chd_10 using hx_htn
- Goal 2. Predict chd_10 using tot_chol and hx_htn
- Goal 3. Predict chd_10 using kitchen sink
- Goal 4. Fit a smaller model almost as good as the KS.

Skimming the Data, before Cleanup or Imputation

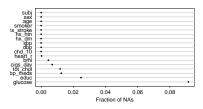
```
fram %>% select(-subj) %>% skim
Skim summary statistics
n obs: 4240
n variables: 16
-- Variable type:character ------
variable missing complete n min max empty n unique
                      4240 4240
      sex
-- Variable type:numeric -----
  variable missing complete
                                                      p0
                                                             p25
                                                                   p50
                                                                          p75
                                      mean
                                               sd
                                                                                p100
                                                                                         hist
                                            8.57
                                                                         56
                 0
                       4240 4240
                                   49.58
                                                           42
                                                                  49
       age
                                                   15.54
                                                           23.07
                                                                  25.4
                                                                        28.04
                                                                                56.8
       bmi
                19
                       4221 4240
                                   25.8
                                            4.08
  bp_meds
                       4187 4240
                                    0.03
                                            0.17
                                                            0
                                                                         0
   chd 10
                0
                       4240 4240
                                    0.15
                                            0.36
                                                    0
                                                            0
                                                                   0
                                                                         0
 cigs_day
                29
                       4211 4240
                                    9.01
                                           11.92
                                                            0
                                                                   0
                                                                        20
                                                                                70
      dbp
                 0
                       4240 4240
                                   82.9
                                           11.91
                                                   48
                                                           75
                                                                  82
                                                                        90
                                                                               142.5
               105
                                    1 98
                                           1 02
                                                            1
     educ
                       4135 4240
               388
                                   81.96
                                           23.95
                                                   40
  alucose
                       3852 4240
                                                                        87
                                                                               394
                       4239 4240
                                                   44
                                                                               143
  heart r
                                   75.88
                                           12.03
                                                           68
                                                                        83
    hx_dm
                       4240 4240
                                    0.026
                                            0.16
                                                                   0
                                                                         0
                                    0.31
                                            0.46
                                                     0
                                                                   0
   hx htn
                 0
                       4240 4240
hx stroke
                 0
                       4240 4240
                                    0.0059
                                            0.077
                                                    0
                                                                   0
                                                                         0
       sbp
                 0
                       4240 4240 132.35
                                           22.03
                                                   83.5
                                                                 128
                                                                        144
                                                                               295
                       4240 4240
                                    0.49
                                            0.5
                                                     0
                                                            0
    smoker
                50
                       4190 4240 236.7
                                           44 59
                                                          206
                                                                 234
                                                                               696
  tot chol
```

Plotting Missingness (with Hmisc, result on next slide)

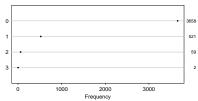
```
par(mfrow = c(2,2))
naplot(naclus(fram))
par(mfrow = c(1,1))
```

Plotting Missingness (with Hmisc)

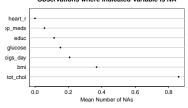
Fraction of NAs in each Variable

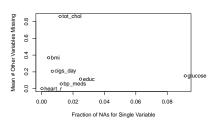


Number of Missing Variables Per Observation



Mean Number of Other Variables Missing for Observations where Indicated Variable is NA





Simple Imputation into fram1

Turn educ into ed_f, a factor.

```
ed_f 1 2 3 4
1_Some_HS 1720 0 0 0
2_HS_grad 0 1358 0 0
3_Some_Col 0 0 689 0
4_Col_grad 0 0 0 473
```

Final Data Set?

fram2 %>% select(-subj) %>% skim

```
fram2 %>% select(-subj) %>% skim
Skim summary statistics
n obs: 4240
n variables: 16
-- Variable type:character ------
variable missing complete n min max empty n_unique
             0 4240 4240 1 1 0 2
     sex
variable missing complete n n_unique
                                                      top_counts ordered
    ed_f 0 4240 4240 4 1_S: 1720, 2_H: 1358, 3_S: 689, 4_C: 473 FALSE
-- Variable type:numeric -----
 variable missing complete n mean sd p0 p25 p50 p75 p100
                   4240 4240 49.58
                                    8 57
                                                42
                                                      49
                                                            56
     age
                   4240 4240 25.8
                                    4.07
                                          15.54
                                                23 08
                                                      25.38
                                                            28.04
     bmi
                                                                  56.8 _
 bp_meds 0 4240 4240 0.029
chd_10 0 4240 4240 0.15
cigs_day 0 4240 4240 9.07
dbp 0 4240 4240 82.9
                   4240 4240 0.029
                                    0.17
                             0.15
                                    0.36
                                                             0
                                   11 91
                                                            20
                                                                  70
                                   11.91
                                                            90
                                                                 142.5
             0 4240 4240
                            81.7
                                   22.94
                                          40
                                                            85
  alucose
                                                                 394
                   4240 4240 75.88
                                   12.02
                                          44
                                                68
                                                            83
                                                                 143
  heart r
   hx dm
                   4240 4240 0.026
                                  0.16
                   4240 4240 0.31
                                    0.46
  hx htn
                  4240 4240
                             0.0059 0.077
hx stroke
                                                      0
                                                             0
                 4240 4240 132.35 22.03
                                          83.5
     sbp
                                                           144
                                                                      4240 4240
                             0.49 0.5
   smoker
 tot chol
                   4240 4240 236.73 44.36 107
                                               206
                                                     234
                                                           263
                                                                 696
```

Goal 1. Predict chd_10 using hx_htn

Predict chd_10 using hx_htn

```
fram2 %>%
  tabyl(hx_htn, chd_10) %>%
  adorn_percentages() %>%
  adorn_pct_formatting() %>%
  adorn_ns(position = "front") %>%
  adorn_title()
```

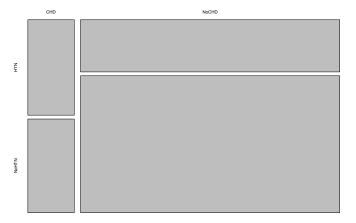
```
chd_10
hx_htn 0 1
0 2604 (89.1%) 319 (10.9%)
1 992 (75.3%) 325 (24.7%)
```

Convert to Standard Epidemiological Format

A mosaic plot?

```
plot(table(fram2$out_1, fram2$htn_1))
```

table(fram2\$out_1, fram2\$htn_1)



Two-by-Two Table Analysis (from the Epi package)

```
twoby2(table(fram2$htn_1, fram2$out_1))
```

```
2 by 2 table analysis:
```

Outcome : CHD

Comparing : HTN vs. NoHTN

```
CHD NoCHD P(CHD) 95% conf. interval HTN 325 992 0.2468 0.2242 0.2708 NoHTN 319 2604 0.1091 0.0983 0.1210
```

```
95% conf. interval
Relative Risk: 2.2612 1.9656 2.6013
Sample Odds Ratio: 2.6744 2.2542 3.1728
Conditional MLE Odds Ratio: 2.6737 2.2454 3.1843
Probability difference: 0.1376 0.1122 0.1640
```

A Logistic Regression model with glm

```
Call: glm(formula = chd_10 ~ hx_htn, family = binomial, data
```

Coefficients:

(Intercept) hx_htn -2.0996 0.9837

Degrees of Freedom: 4239 Total (i.e. Null); 4238 Residual

Null Deviance: 3612

Residual Deviance: 3487 AIC: 3491

Interpretation of the Model

```
exp(coef(m_01)); exp(confint(m_01))
```

```
(Intercept) hx_htn
0.1225038 2.6743730
```

Waiting for profiling to be done...

```
2.5 % 97.5 % (Intercept) 0.1088612 0.1373705 hx_htn 2.2543282 3.1733406
```

Compare this to the twoby2 result:

Sample Odds Ratio: 2.6744 2.2542 3.1728 Conditional MLE Odds Ratio: 2.6737 2.2454 3.1843

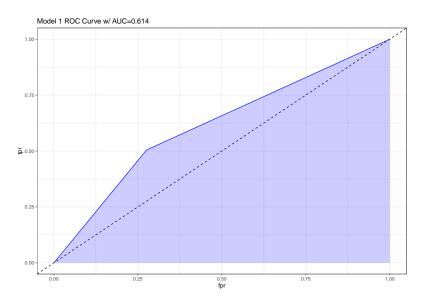
Using broom

```
tidy(m_01)
```

glance(m_01)

Building the ROC Curve with ROCR

ROC Curve for our Model



C statistic isn't a "one stop" measure of accuracy

The C statistic tells you about discrimination but nothing about calibration.

- The poor C statistic indicates that m_01 has poor discrimination.
 - If m_01 predicts Harry has a higher Pr(CHD) than Sally, we cannot really trust that will be an accurate ordering.
- But this isn't any indication of m_01's calibration.
 - Even a large C statistic (near 1) doesn't tell you anything about whether a group of people with Pr(CHD) = 0.20 would actually have anything close to a 20% chance of CHD.
 - A large C statistic indicates that the model puts subjects in the correct order (low risk of CHD to high risk,) but we can still get the actual risks wrong if the calibration is poor.

Using 1rm from the rms package to fit Logistic Regression Models

A Logistic Regression model with 1rm

```
d <- datadist(fram2)
options(datadist = "d")

m_01_lrm <- lrm(chd_10 ~ hx_htn, data = fram2, x = T, y = T)</pre>
```

```
> m_01_1rm
Logistic Regression Model
 lrm(formula = chd_10 \sim hx_htn, data = fram2, x = T, y = T)
                   Model Likelihood Discrimination Rank Discrim.
                  Ratio Test Indexes
LR chi2 125.30 R2 0.051
                                                      Indexes
0bs
     4240
                                                    C 0.614
     3596
                  d.f. 1
                                     g 0.421
                                                    Dxy 0.229
 0
     644
                  Pr(> chi2) <0.0001
                                     gr 1.524
                                                    gamma 0.456
                                     gp 0.059
max |deriv| 1e-09
                                                    tau-a 0.059
                                     Brier 0.125
         Coef S.E. Wald Z Pr(>|Z|)
 Intercept -2.0996 0.0593 -35.39 <0.0001
 hx_htn 0.9837 0.0872 11.28 <0.0001
```

1rm output Piece by Piece

```
Model Likelihood
Ratio Test

Obs 4240 LR chi2 125.30

O 3596 d.f. 1

1 644 Pr(> chi2) <0.0001

max |deriv| 1e-09
```

- Likelihood-ratio test = drop in deviance test
 - How much does a goodness-of-fit statistic move as a result of this model?
 - Deviance = -2 log(likelihood function)

1rm output Piece by Piece, 2

Discrimination		Rank I	oiscrim.
	Indexes		Indexes
R2	0.051	C	0.614
g	0.421	Dxy	0.229
gr	1.524	gamma	0.456
gp	0.059	tau-a	0.059
Brier	0.125		

Nagelkerke pseudo- R^2 statistic = 1 if the model predicts the outcome perfectly and the likelihood function is 1.

- an adjusted version (to a 0-1 scale) of the Cox-Snell pseudo-R²
- compares the log likelihood of our model to the log likelihood for a null model.
- so it's similar to the R² for a linear model in terms of improvement from a null model to a fitted model
- neither a percentage of explained variability nor the square of any

1rm output Piece by Piece, 3

Discrimination		Rank D	iscrim.
	Indexes		Indexes
R2	0.051	C	0.614
g	0.421	Dxy	0.229
gr	1.524	gamma	0.456
gp	0.059	tau-a	0.059
Brier	0.125		

- gp = Gini's index on the probability scale, which we want to be as large as possible
 - Gini's mean difference is the mean absolute difference between any two distinct predictions.
 - This measures the average "purity" in the predictions, essentially.
- R also presents g and gr, which are the same thing on the log odds, and odds scale.
- The **lower** the Brier score, the better the predictions are calibrated.
 - This is a nice measure of the accuracy of probabilistic predictions.

1rm output Piece by Piece, 4

Discrimination		Rank Discrim.	
	Indexes		${\tt Indexes}$
R2	0.051	C	0.614
g	0.421	Dxy	0.229
gr	1.524	gamma	0.456
gp	0.059	tau-a	0.059
Brier	0.125		

- C = C statistic = area under the ROC curve
- Dxy = Somers' d, and C = 0.5 + Dxy/2
- gamma = Goodman and Kruskal's Γ , which is a measure of the rank correlation between the observed and predicted values of CHD = 1.
 - ullet Values range from -1 (perfect negative association) to +1 (perfect agreement.)
- tau-a = Kendall's τ , is another measure of such an association.

Validating our Summary Statistics

validate(m_01_lrm)

```
index.orig training test optimism
                     0.2340
Dxy
             0.2288
                            0.2288
                                     0.0052
R2
            0.0508 0.0532 0.0508
                                     0.0025
            0.0000 0.0000 -0.0201
Intercept
                                     0.0201
            1.0000 1.0000
                                     0.0160
Slope
                            0.9840
                                     0.0072
Emax
            0.0000
                     0.0000
                            0.0072
D
             0.0293
                     0.0307 0.0293 0.0014
U
            -0.0005
                    -0.0005 0.0000
                                    -0.0005
Q
             0.0298 0.0312 0.0293
                                     0.0019
В
             0.1248 0.1240
                            0.1248
                                    -0.0008
             0.4214 0.4303 0.4214
                                     0.0089
g
             0.0590 0.0600
                            0.0590
                                     0.0011
gp
         index.corrected
Dxy
                 0.2236 40
R.2.
                 0.0483 40
```

Coefficients Summary from m_01_lrm

```
Coef S.E. Wald Z Pr(>|Z|)
Intercept -2.0996 0.0593 -35.39 <0.0001
hx_htn 0.9837 0.0872 11.28 <0.0001
```

Conclusions?

Assessing Effect Sizes

Effects

```
summary(m_01_lrm)
```

```
Factor Low High Diff. Effect S.E. Lower 0.95 hx_htn 0 1 1 0.98371 0.0872 0.81281 Odds Ratio 0 1 1 2.67440 NA 2.25420 Upper 0.95 1.1546 3.1728
```

Response : chd_10

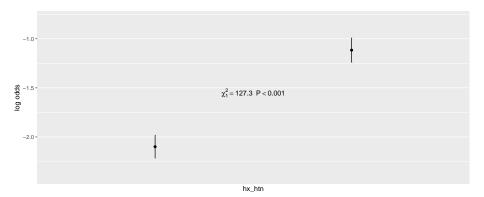
Plotting the Effect Sizes



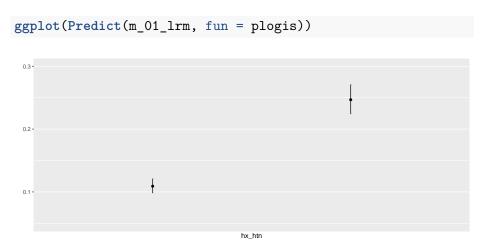
The plot shows 90%, 95% and 99% confidence intervals.

Can we see the prediction results?

```
ggplot(Predict(m_01_lrm),
          anova = anova(m_01_lrm), pval = TRUE)
```

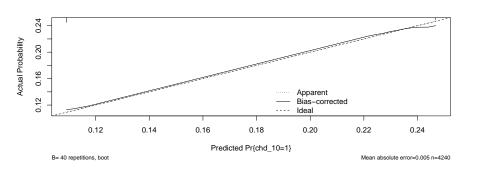


What about on a better scale?



Is this m_01_lrm well calibrated?

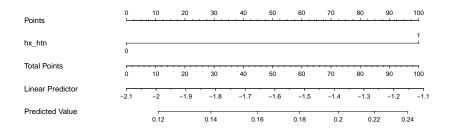
plot(calibrate(m 01 lrm))



n=4240 Mean absolute error=0.005 0.9 Quantile of absolute error=0.007

Mean squared error=2e-05

Nomogram for m_01_lrm



Goal 2. Predict chd_10 using hx_htn and tot_chol

glm fit (Don't forget family = binomial!)

```
Call: glm(formula = chd_10 ~ hx_htn + tot_chol, family = bind
    data = fram2)
```

Coefficients:

```
(Intercept) hx_htn tot_chol
-2.855553 0.934387 0.003229
```

Degrees of Freedom: 4239 Total (i.e. Null); 4237 Residual

Null Deviance: 3612

Residual Deviance: 3475 AIC: 3481

Does m_02 improve on m_01 by ANOVA?

```
anova(m_01, m_02)
```

Analysis of Deviance Table

```
Model 1: chd_10 ~ hx_htn

Model 2: chd_10 ~ hx_htn + tot_chol

Resid. Df Resid. Dev Df Deviance

1 4238 3486.9

2 4237 3475.5 1 11.411
```

```
pchisq(11.41, 1, lower.tail = FALSE)
```

```
[1] 0.0007304983
```

Does m_02 improve on m_01 by AIC/BIC?

```
glance(m_01)
```

```
glance(m_02)
```

anova(m_02)

Analysis of Deviance Table

Model: binomial, link: logit

Response: chd_10

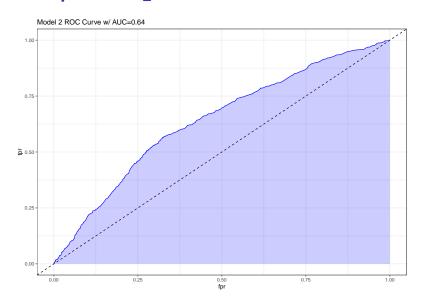
Terms added sequentially (first to last)

Df Deviance Resid. Df Resid. Dev NULL 4239 3612.2 hx_htn 1 125.302 4238 3486.9 tot_chol 1 11.411 4237 3475.5

summary(m_02)

```
> summary(m_02)
Call:
glm(formula = chd_10 \sim hx_htn + tot_chol, family = binomial.
   data = fram2)
Deviance Residuals:
            10 Median 30
   Min
                                  Max
-1.3188 -0.5493 -0.4814 -0.4494 2.2276
Coefficients:
           Estimate Std. Error z value Pr(>|z|)
hx_htn 0.934387 0.088454 10.564 < 2e-16 ***
tot chol 0.003229 0.000951 3.396 0.000684 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
   Null deviance: 3612.2 on 4239 degrees of freedom
Residual deviance: 3475.5 on 4237 degrees of freedom
AIC: 3481.5
Number of Fisher Scoring iterations: 4
```

ROC plot for m_02



Fitting with 1rm

```
m 02 1rm
Logistic Regression Model
lrm(formula = chd_10 \sim hx_htn + tot_chol, data = fram2, x = TRUE,
   V = TRUE
                  Model Likelihood Discrimination
                                                   Rank Discrim.
                     Ratio Test
                                      Indexes
                                                     Indexes
     4240 LR chi2 136.71
Obs
                                    R2 0.055
                                                   c 0.640
 0
      3596 d.f.
                                    g 0.510
                                                   Dxy 0.281
          644
                 Pr(> chi2) < 0.0001
                                                   gamma 0.282
                                    gr 1.665
max |deriv| 4e-07
                                    gp 0.069
                                                   tau-a 0.072
                                    Brier 0.125
        Coef S.E. Wald Z Pr(>|Z|)
Intercept -2.8556 0.2325 -12.28 <0.0001
hx_htn 0.9344 0.0885 10.56 <0.0001
tot_chol 0.0032 0.0010 3.40 0.0007
```

Validating our Summary Statistics

validate(m_02_lrm)

```
index.orig training test optimism
                     0.2766
Dxy
             0.2805
                             0.2806
                                    -0.0040
R2
             0.0553
                     0.0550
                             0.0548
                                     0.0001
Intercept
             0.0000
                     0.0000
                             0.0061
                                    -0.0061
             1.0000 1.0000 1.0085
                                    -0.0085
Slope
Emax
             0.0000
                     0.0000
                             0.0029
                                     0.0029
D
             0.0320
                     0.0319
                             0.0317 0.0002
U
            -0.0005
                    -0.0005 -0.0001
                                    -0.0004
Q
             0.0325 0.0324
                             0.0318 0.0005
В
             0.1245 0.1252 0.1246
                                     0.0006
             0.5098 0.4996 0.5018
                                    -0.0022
g
             0.0690
                     0.0681
                             0.0681
                                     0.0001
gp
         index.corrected
Dxy
                 0.2845 40
                 0.0552 40
R.2.
```

ANOVA with 1rm

anova(m_02_lrm)

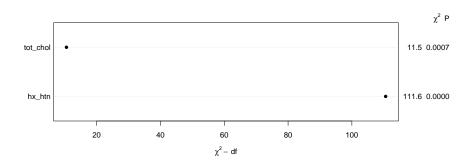
Wald Statistics

Response: chd_10

```
Factor Chi-Square d.f. P
hx_htn 111.59 1 <.0001
tot_chol 11.53 1 7e-04
TOTAL 137.85 2 <.0001
```

ANOVA plot in 1rm

plot(anova(m_02_lrm))



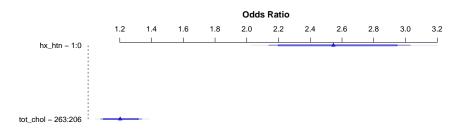
Estimated Effect Sizes

```
summary(m_02_1rm)
```

```
Effects
                             Response : chd_10
Factor
          Low High Diff. Effect S.E. Lower 0.95
               1 1 0.93439 0.088455 0.761020
hx htn
            0
Odds Ratio
            0
               1 1 2.54570 NA 2.140500
          206 263 57 0.18407 0.054208 0.077827
tot chol
Odds Ratio 206 263 57 1.20210 NA 1.080900
Upper 0.95
1.10780
3.02760
0.29032
1.33690
```

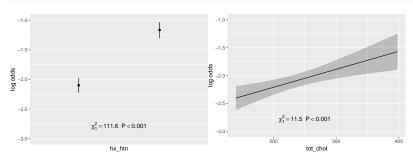
Plotting the Effect Sizes

```
plot(summary(m_02_lrm))
```



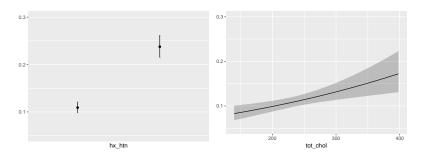
Can we see the prediction results?

```
ggplot(Predict(m_02_lrm),
          anova = anova(m_02_lrm), pval = TRUE)
```



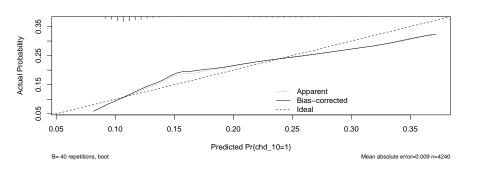
What about on a better scale?

ggplot(Predict(m_02_lrm, fun = plogis))



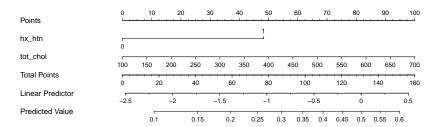
Calibration of mod_02_1rm

plot(calibrate(m 02 lrm))



n=4240 Mean absolute error=0.009 Mean squared error=0.0000 0.9 Quantile of absolute error=0.018

Nomogram of mod_02_1rm



Goal 3. Kitchen Sink Model

Focus on model with 1rm first!

```
m_03 \leftarrow glm(chd_10 \sim hx_htn + tot_chol + sex + age +
                      smoker + cigs day + bp meds +
                      hx stroke + hx dm + ed f + sbp + dbp +
                      bmi + heart r + glucose,
                 data = fram2, family = binomial)
d <- datadist(fram2)</pre>
options(datadist = "d")
m_03_{rm} \leftarrow r_{chd_10} \sim hx_{htn} + tot_{chol} + sex + age +
                      smoker + cigs_day + bp_meds +
                      hx_stroke + hx_dm + ed_f + sbp + dbp +
                      bmi + heart_r + glucose,
                 data = fram2, x = TRUE, y = TRUE)
```

m_03_1rm (first section of output)

```
> m 03 1rm
Logistic Regression Model
 lrm(formula = chd_10 \sim hx_htn + tot_chol + sex + age + smoker +
    cigs_day + bp_meds + hx_stroke + hx_dm + ed_f + sbp + dbp +
    bmi + heart_r + glucose, data = fram2, x = TRUE, y = TRUE)
                      Model Likelihood
                                          Discrimination
                                                            Rank Discrim
                         Ratio Test
                                             Indexes
                                                               Indexes
             4240
                     LR chi2 405.40
                                          R2
                                                   0.159
                                                                   0.733
 Obs
                                                            C
  0
             3596
                     d.f.
                                          q
                                                   1.016
                                                            Dxy
                                                                   0.466
              644
                     Pr(> chi2) < 0.0001
                                                   2.763
                                                            gamma
                                                                   0.466
                                          gr
                                                   0.120
                                                                   0.120
 max |deriv| 6e-10
                                          gp
                                                            tau-a
                                                   0.115
                                          Brier
```

m_03_lrm (second section of output)

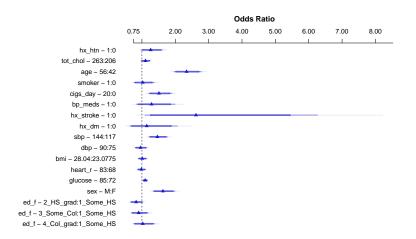
Coef	S.E.	Wald Z	Pr(> Z)
-7.9981	0.6583	-12.15	<0.0001
			0.0842
0.4886	0.1012	4.83	<0.0001
0.0607	0.0063	9.67	<0.0001
0.0248	0.1451	0.17	0.8642
0.0207	0.0057	3.60	0.0003
0.2534	0.2206	1.15	0.2506
0.9633	0.4439	2.17	0.0300
0.1353	0.2989	0.45	0.6507
-0.1906	0.1120	-1.70	0.0889
-0.1005	0.1397	-0.72	0.4719
0.0255	0.1533	0.17	0.8679
0.0141	0.0035	3.98	<0.0001
-0.0029	0.0060	-0.48	0.6294
0.0019	0.0118	0.16	0.8712
-0.0012	0.0039	-0.32	0.7524
0.0071	0.0022	3.28	0.0010
	-7.9981 0.2331 0.0018 0.4886 0.0607 0.0248 0.0207 0.2534 0.9633 0.1353 -0.1906 -0.1005 0.0255 0.0141 -0.0029 0.0019 -0.0012	-7.9981 0.6583 0.2331 0.1287 0.0018 0.0010 0.4886 0.1012 0.0607 0.0063 0.0248 0.1451 0.0207 0.0057 0.2534 0.2206 0.9633 0.4439 0.1353 0.2989 -0.1906 0.1120 -0.1005 0.1397 0.0255 0.1533 0.0141 0.0035 -0.0029 0.0060 0.0019 0.0118	0.0607 0.0063 9.67 0.0248 0.1451 0.17 0.0207 0.0057 3.60 0.2534 0.2206 1.15 0.9633 0.4439 2.17 0.1353 0.2989 0.45 -0.1906 0.1120 -1.70 -0.1005 0.1397 -0.72 0.0255 0.1533 0.17 0.0141 0.0035 3.98 -0.0029 0.0060 -0.48 0.0019 0.0118 0.16 -0.0012 0.0039 -0.32

Validating our Summary Statistics

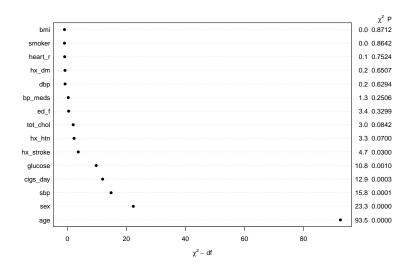
validate(m_03_lrm)

```
index.orig training test optimism
                     0.4813 0.4587
Dxy
             0.4659
                                     0.0226
R2
             0.1590 0.1701 0.1532
                                     0.0169
             0.0000 0.0000 -0.0838
Intercept
                                     0.0838
             1.0000 1.0000
                            0.9425
                                     0.0575
Slope
Emax
             0.0000 0.0000
                            0.0287
                                     0.0287
D
             0.0954 0.1025 0.0917 0.0107
U
            -0.0005
                    -0.0005 0.0003
                                    -0.0008
Q
             0.0958 0.1029 0.0914
                                     0.0115
В
             0.1152 0.1142 0.1159
                                    -0.0017
                                     0.0662
             1.0164 1.0550 0.9888
g
             0.1203 0.1242
                            0.1179
                                     0.0063
gp
         index.corrected
Dxy
                 0.4433 40
                 0.1422 40
R.2.
```

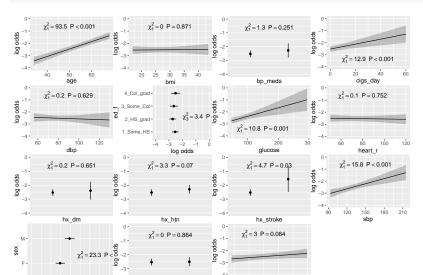
plot(summary(m_03_lrm))



plot(anova(m_03_lrm))

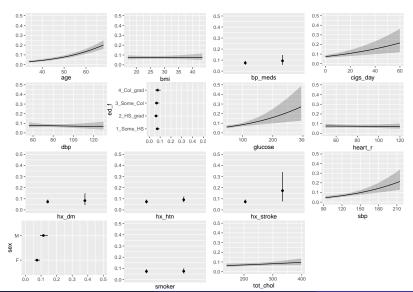


Can we see the prediction results?



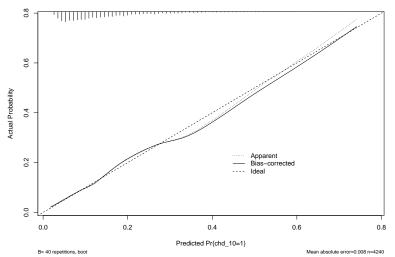
What about on a better scale?

ggplot(Predict(m_03_lrm, fun = plogis))



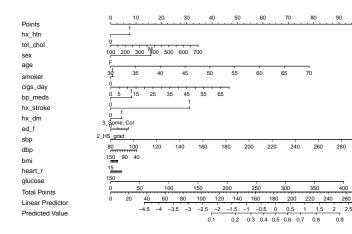
Calibration of mod_03_lrm

plot(calibrate(m_03_lrm))



Nomogram of mod_03_1rm

plot(nomogram(m_03_lrm, fun = plogis))



100

300

Comparing our Three Nested Models

```
anova(m_01, m_02, m_03)
Analysis of Deviance Table
Model 1: chd 10 ~ hx htn
Model 2: chd_10 ~ hx_htn + tot_chol
Model 3: chd 10 ~ hx htn + tot chol + sex + age + smoker + ci
   bp meds + hx stroke + hx dm + ed f + sbp + dbp + bmi + hea
   glucose
  Resid. Df Resid. Dev Df Deviance
1
      4238 3486.9
    4237 3475.5 1 11.411
2
3
      4222 3206.8 15 268.682
```

Model 2 vs. Model 3 at a glance

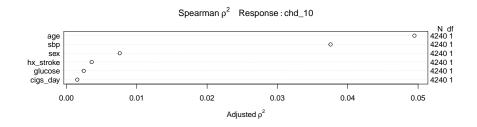
glance(m_02)

glance(m_03)

Fitting a 6-predictor, but still useful model

What looks useful?

By ANOVA on m_03_1rm it looks like age, sex, sbp, cigs_day, glucose, hx_stroke for sure.



New Model 4

```
m 04 \leftarrow glm(chd 10 \sim rcs(age, 5) + rcs(sbp, 3) + sex +
                     hx_stroke + glucose + cigs_day,
                 data = fram2, family = binomial)
dd <- datadist(fram2)</pre>
options(datadist = "dd")
m 04 1rm < -1rm(chd 10 ~ rcs(age, 5) + rcs(sbp, 3) + sex +
                     hx stroke + glucose + cigs day,
                 data = fram2, x = TRUE, y = TRUE)
```

m_04 lrm

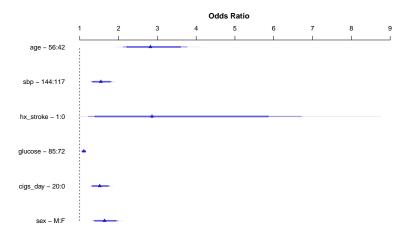
```
> m 04 1 rm
Logistic Regression Model
 lrm(formula = chd_10 \sim rcs(age, 5) + rcs(sbp, 3) + sex + hx_stroke +
    glucose + cigs_day, data = fram2, x = TRUE, y = TRUE)
                    Model Likelihood
                                       Discrimination
                                                       Rank Discrim.
                       Ratio Test
                                          Indexes
                                                          Indexes
            4240
                   LR chi2 401.44
                                       R2
                                          0.158
                                                              0.731
Obs
            3596
                                                       Dxy
 0
                   d.f.
                                 10
                                              1.041
                                                              0.461
                                       g
             644
                   Pr(> chi2) <0.0001
                                       gr 2.833
                                                              0.461
                                                       gamma
 max |deriv| 2e-06
                                       gp 0.120
                                                       tau-a
                                                              0.119
                                       Brier 0.115
         Coef S.E. Wald Z Pr(>|Z|)
 Intercept -8.7201 2.4092 -3.62 0.0003
       0.0732 0.0576 1.27 0.2037
 age
 age'
     0.2871 0.3539 0.81 0.4172
 age'' -1.1057 0.9608 -1.15
                            0.2498
 age'''
       1.4723 0.9640 1.53 0.1267
 sbp
        0.0147 0.0066 2.23 0.0256
sbp'
         0.0030 0.0080 0.37 0.7080
sex=M 0.4935 0.0973 5.07 <0.0001
hx_stroke 1.0514 0.4345 2.42 0.0155
 glucose 0.0076 0.0016 4.69 <0.0001
 cigs_day
          0.0208 0.0039 5.39 < 0.0001
```

Validating our Summary Statistics

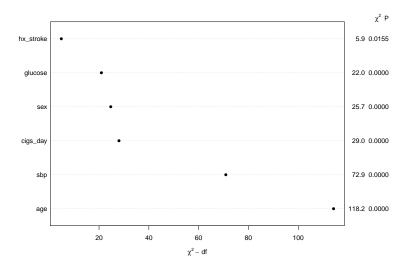
validate(m_04_lrm)

```
index.orig training test optimism
                     0.4585 0.4566
Dxy
             0.4611
                                     0.0019
R2
            0.1575 0.1593 0.1540
                                     0.0052
            0.0000 0.0000 -0.0321
Intercept
                                     0.0321
            1.0000 1.0000
                            0.9851
                                     0.0149
Slope
Emax
            0.0000 0.0000
                            0.0095
                                     0.0095
D
             0.0944 0.0959 0.0922
                                     0.0037
U
            -0.0005
                    -0.0005 0.0000
                                    -0.0005
Q
             0.0949 0.0964 0.0922
                                     0.0042
В
             0.1152 0.1157
                            0.1156
                                     0.0001
             1.0414 1.0450 1.0237
                                     0.0212
g
             0.1198 0.1206
                            0.1181
                                     0.0025
gp
         index.corrected
Dxy
                 0.4592 40
                 0.1523 40
R.2.
```

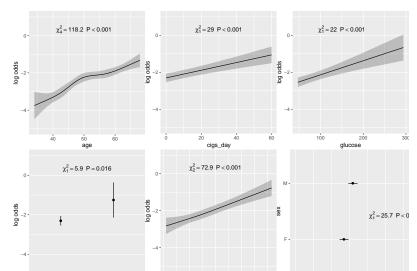
plot(summary(m_04_lrm))



plot(anova(m_04_lrm))

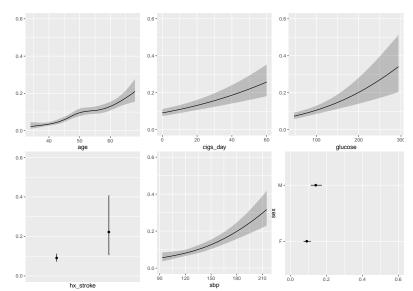


Can we see the prediction results?



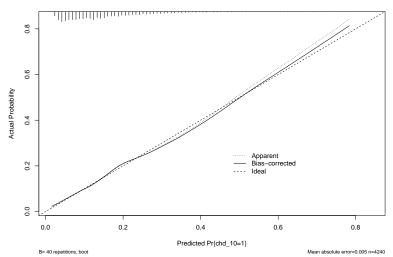
What about on a better scale?

ggplot(Predict(m_04_lrm, fun = plogis))

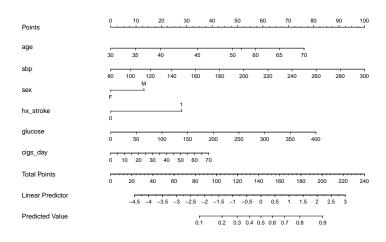


Calibration of mod_04_lrm

plot(calibrate(m_04_lrm))



Nomogram of mod_04_1rm



Comparing Models 3 and 4 (which aren't nested)

glance(m_03) # kitchen sink but no non-linear terms

```
glance(m_04) # six predictors but with non-linear terms
```

Checking Residuals?

- Yes/No outcomes contain less information than quantitative outcomes
- Residuals cannot be observed predicted
 - There are several different types of residuals defined
- Assumptions of logistic regression are different
 - Model is deliberately non-linear
 - Error variance is a function of the mean, so it isn't constant
 - Errors aren't assumed to follow a Normal distribution
 - Only thing that's the same: leverage and influence

So, plot 5 (residuals/leverage/influence) can be a little useful, but that's it.

We'll need better diagnostic tools for generalized linear models.

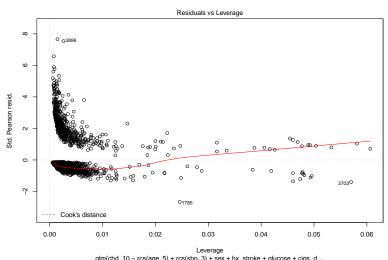
Any observations particularly influential on Model 4?

```
which.influence(m_04_lrm, cutoff = 0.3)
$Intercept
```

```
[1] "3896"
$glucose
[1] "1785" "3703"
```

Influence and Model 4?

 $plot(m_04, which = 5)$



glm(chd_10 ~ rcs(age, 5) + rcs(sbp, 3) + sex + hx_stroke + glucose + cigs_d ...

Next Time

Project 1 Discussions in Small Groups