



# Geometry Workbook Solutions

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Area and perimeter

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MATH

## AREA OF A RECTANGLE

- 1. The base of a rectangle is 8 feet. Find its height if the area of the rectangle is  $80 \text{ ft}^2$ .

*Solution:*

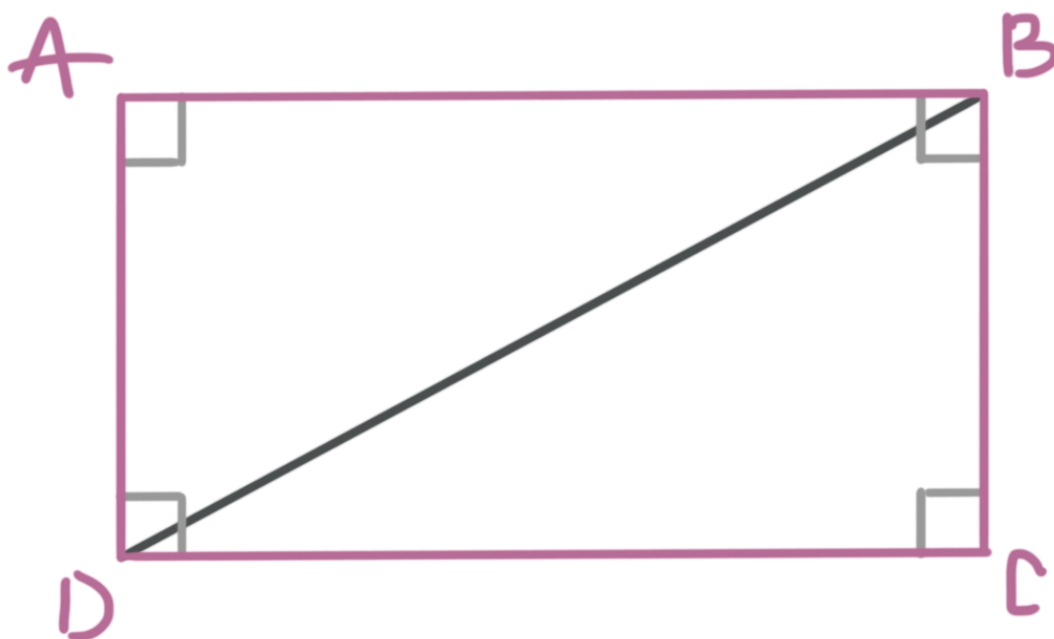
We can use the formula for the area of the rectangle to plug in everything we know, and then solve for the height.

$$A = bh$$

$$80 = 8h$$

$$h = 10 \text{ feet}$$

- 2. In rectangle  $ABCD$ ,  $BD = 13$  and  $AB = 12$ . Find the area of this rectangle.



*Solution:*

Use the Pythagorean Theorem to find the length of  $\overline{AD}$ .

$$AD^2 + AB^2 = BD^2$$

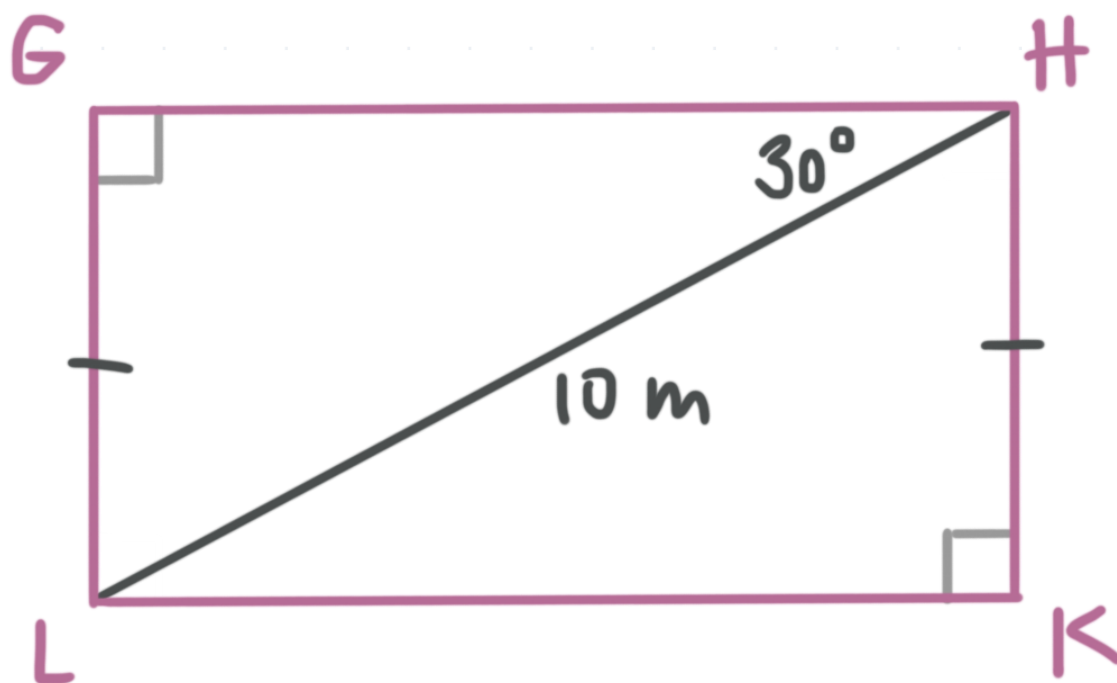
$$AD^2 + 12^2 = 13^2$$

$$AD^2 = 25$$

$$AD = 5$$

Therefore, the area of the rectangle is  $A = bh = (5)(12) = 60$ .

■ 3. In rectangle  $GHLK$ ,  $LH = 10$  and  $m\angle GHL = 30^\circ$ . Find the exact area of the rectangle.



*Solution:*

$\triangle GHL$  is a special right triangle with degree measures  $30 - 60 - 90$ . The diagonal of the rectangle is 10 and is the hypotenuse of  $\triangle GHL$ . The shortest leg of the triangle is  $\overline{GL}$  and this side is half the length of the hypotenuse.  $GL = 5$  and  $\overline{GH}$  is the product of the shorter leg and  $\sqrt{3}$ . Therefore,  $GH = 5\sqrt{3}$ . The area of the rectangle is

$$A = bh = (5)(5\sqrt{3}) = 25\sqrt{3}$$

■ 4. The area of a small square flower garden is  $49 \text{ ft}^2$ . Suppose we wish to make the garden bigger by adding 6 feet to one of the sides. How much more square footage is available in this new rectangular garden?

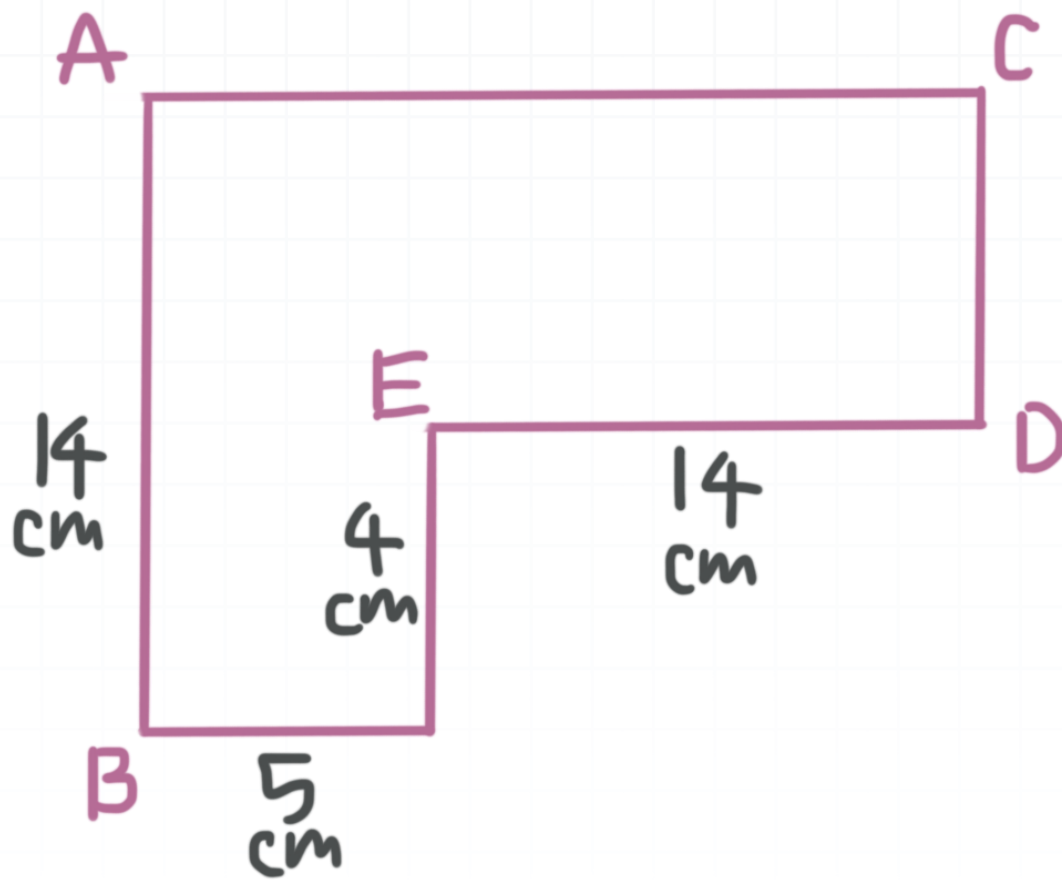
*Solution:*

The original square garden has dimensions 7 feet by 7 feet. By adding 6 feet onto one of the sides, we get a new rectangle with dimensions 13 feet by 7 feet. The new garden has an area of  $(13)(7) = 91 \text{ ft}^2$ . To find the area gained, take  $91 - 49 = 42 \text{ ft}^2$ .



## AREA OF A RECTANGLE USING SUMS AND DIFFERENCES

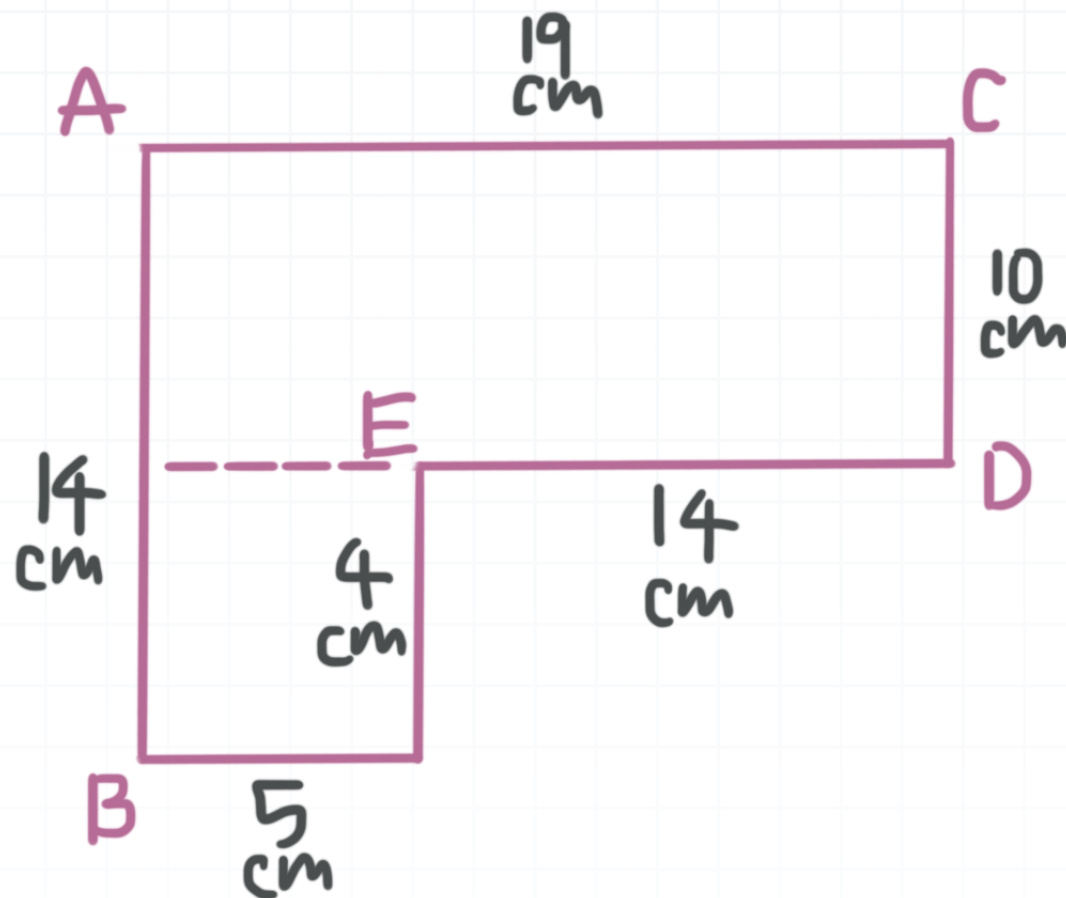
- 1. Find the area of the figure.



*Solution:*

Segment the figure into two rectangles, and fill out the rest of the figure.





The area of the larger rectangle is  $A_1 = lw = (19)(10) = 190 \text{ cm}^2$ .

The area of the smaller rectangle is  $A_2 = lw = (5)(4) = 20 \text{ cm}^2$ .

Then the area of the whole figure is

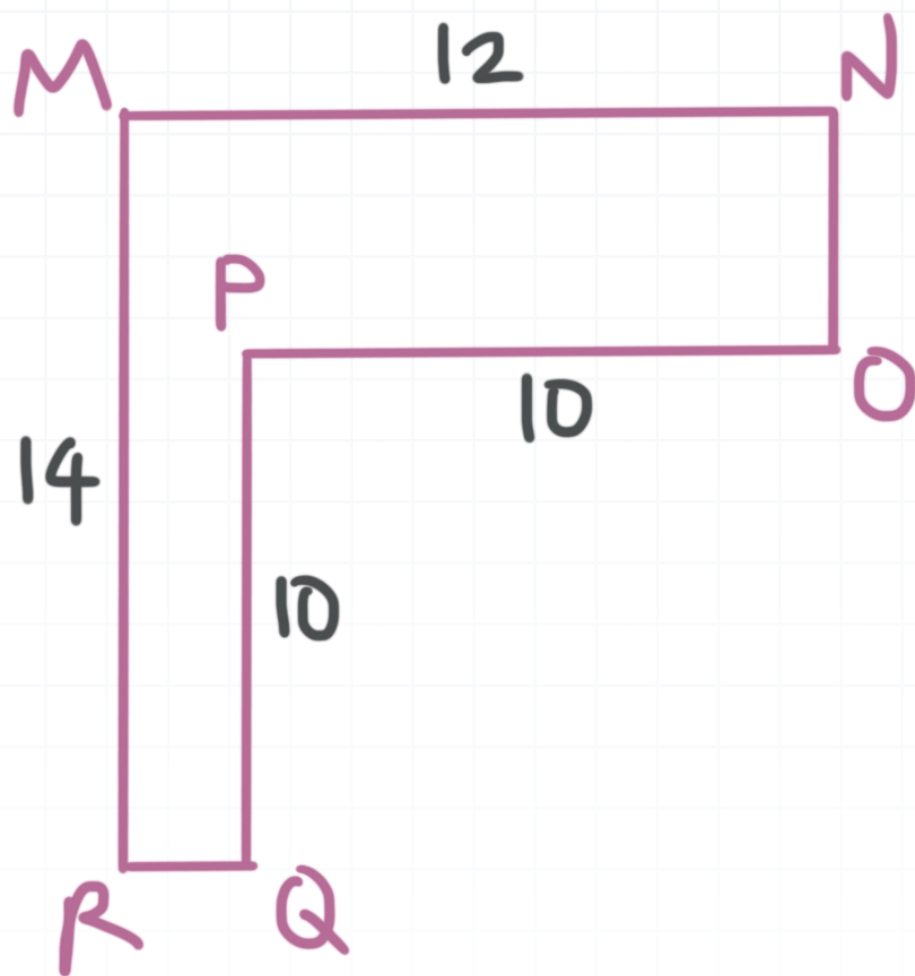
$$A = A_1 + A_2$$

$$A = 190 \text{ cm}^2 + 20 \text{ cm}^2$$

$$A = 210 \text{ cm}^2$$

■ 2. Find the area of the figure.



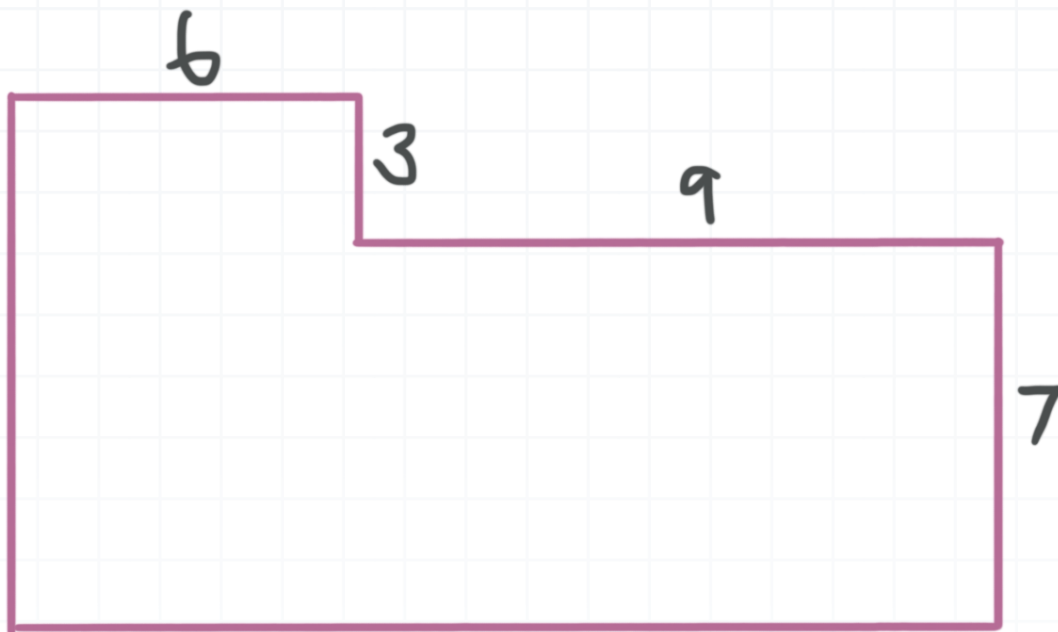


*Solution:*

The area of larger rectangle with three vertices at  $M$ ,  $N$ , and  $R$  is  $A = (14)(12) = 168$ . The area of the smaller rectangle with three vertices at  $P$ ,  $O$ , and  $Q$  is  $A = (10)(10) = 100$ . Using the difference method, the area of the figure is  $168 - 100 = 68$ .

■ 3. Find the area of the figure.





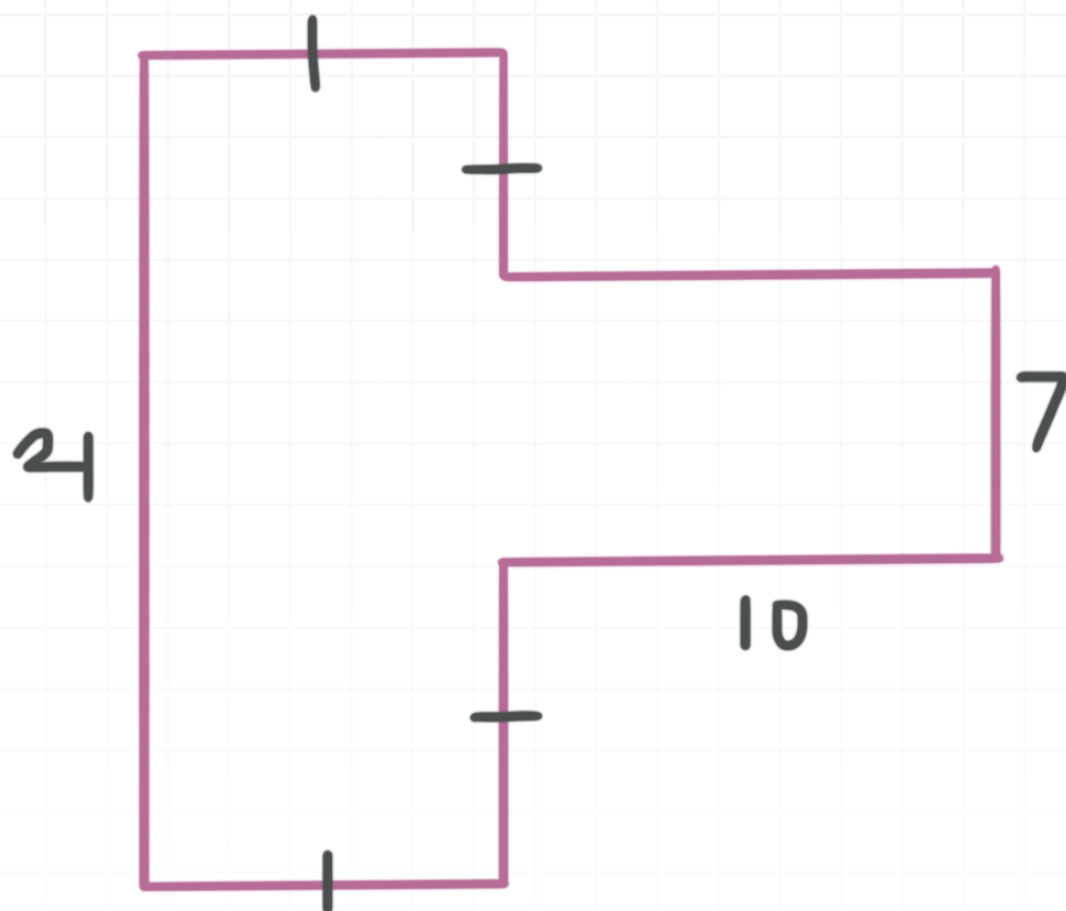
*Solution:*

The area of the little rectangle in the upper left is  $A = (6)(3) = 18$ . The area of the larger rectangle at the bottom is  $A = (6 + 9)(7) = 105$ . Using the sum method, the area of the figure is  $18 + 105 = 123$ .

■ 4. Find the area of the figure.







*Solution:*

The area of the rectangle on the left is  $A = (21)(7) = 147$ . The area of the rectangle on the right is  $A = 10(7) = 70$ . Using the sum method, the area of the figure is  $A = 147 + 70 = 217$ .



## PERIMETER OF A RECTANGLE

- 1. A rectangle has a base of 10 meters. The height is 4 meters greater than the base. Find the perimeter of this rectangle.

*Solution:*

By the formula for the perimeter of a rectangle, we get

$$P = 2b + 2h$$

$$P = 2(10) + 2(10 + 4)$$

$$P = 20 + 18$$

$$P = 48$$

- 2. The area of a rectangle is  $40 \text{ ft}^2$ . Find the perimeter of this rectangle if the length of the rectangle is 3 feet longer than the width.

*Solution:*

First, we'll write the equation for the area and plug in what we know.

$$A = bh$$



$$40 = b(b + 3)$$

$$40 = b^2 + 3b$$

$$0 = b^2 + 3b - 40$$

$$0 = (b + 8)(b - 5)$$

$$b = -8, 5$$

The base of the rectangle can't be defined by a negative number, so the base must be 5 feet long. The height is therefore  $h = 5 + 3 = 8$  feet, and the perimeter is

$$p = 2b + 2h$$

$$p = 2(5) + 2(8)$$

$$p = 10 + 16$$

$$p = 26$$

■ 3. Find the perimeter of a rectangle with vertices at  $A(-3,0)$ ,  $B(0,4)$ ,  $C(4,1)$ , and  $D(1, -3)$ .

*Solution:*

We need to use the distance formula to calculate the distance between adjacent points, which will give us the length of each side of the rectangle.



$$d_{AB} = \sqrt{(4 - 0)^2 + (0 - (-3))^2} = 5$$

$$d_{BC} = \sqrt{(1 - 4)^2 + (4 - 0)^2} = 5$$

$$d_{CD} = \sqrt{((-3) - 1)^2 + (1 - 4)^2} = 5$$

$$d_{AD} = \sqrt{(-3 - 0)^2 + (1 - (-3))^2} = 5$$

Therefore, the perimeter is

$$p = AB + BC + CD + AD$$

$$p = 5 + 5 + 5 + 5$$

$$p = 20$$

■ 4. Find the value of  $x$  if the base of the rectangle has length  $x + 4$ , the height of the rectangle is  $x$ , and the perimeter of a rectangle is 20 units.

*Solution:*

Plug what you know into the formula for the perimeter of a rectangle.

$$P = 2b + 2h$$

$$20 = 2(x + 4) + 2(x)$$

$$20 = 2x + 8 + 2x$$



$$20 = 4x + 8$$

$$12 = 4x$$

$$x = 3$$



## AREA OF A PARALLELOGRAM

- 1. Find the area of a parallelogram with  $b = 14$  yards and  $h = 10$  yards.

*Solution:*

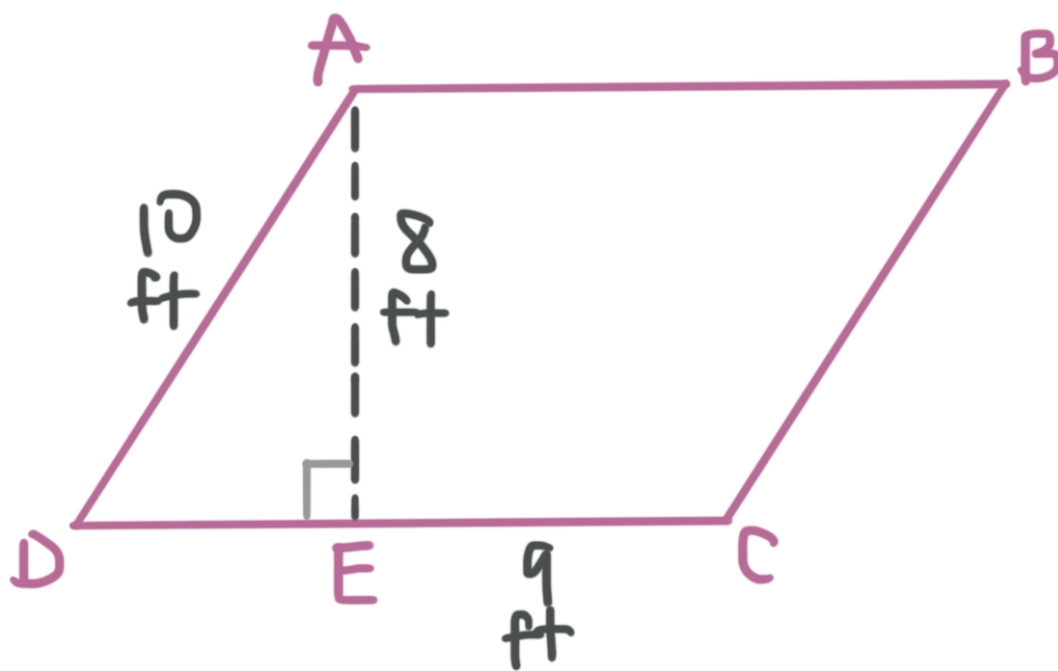
The area of a parallelogram is given by the product of its base and height.

$$A = bh$$

$$A = (14)(10)$$

$$A = 140 \text{ yd}^2$$

- 2. Find the area of the parallelogram.



*Solution:*

Find the missing side,  $ED$ , of the right triangle using Pythagorean Theorem.

$$ED^2 + 8^2 = 10^2$$

$$ED = 6$$

Find the length of the base of the parallelogram,  $\overline{DC}$ .

$$DC = 6 + 9$$

Then the area is

$$A = bh = (15)(8) = 120$$

■ 3. Find the area of parallelogram  $JKLM$ , if  $J(0,0)$ ,  $K(1,3)$ ,  $L(-5,3)$ , and  $M(-6,0)$ .

*Solution:*

Graph the parallelogram and find the base and height. The base is  $b = 6$  and the height is  $h = 3$ . Then the area is

$$A = bh = (6)(3) = 18$$



- 4. A parallelogram has a base that is 3 feet longer than it is tall. The area of the parallelogram is 88 square feet. Find the height of the parallelogram.

*Solution:*

Using the equation for area, we can find the height.

$$A = bh$$

$$88 = (h + 3)(h)$$

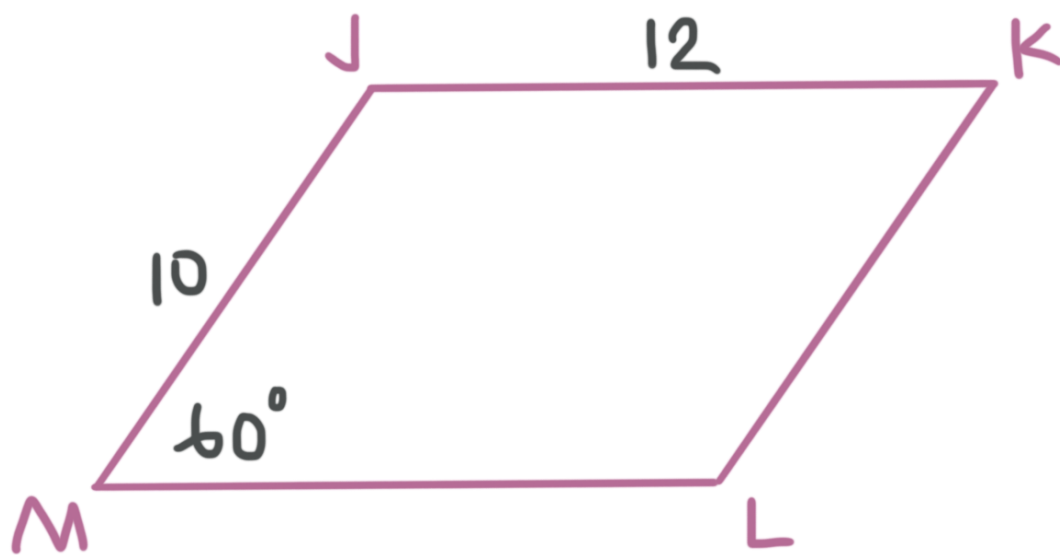
$$88 = h^2 + 3h$$

$$0 = h^2 + 3h - 88$$

$$0 = (h + 11)(h - 8)$$

$$h = 8$$

- 5. Find the exact area of the parallelogram.





*Solution:*

The height forms a right angle with the base. A  $30 - 60 - 90$  triangle is formed with 10 as its hypotenuse. The height can be found by applying  $30 - 60 - 90$  rules to get  $h = 5\sqrt{3}$ . Then the area is the parallelogram is

$$A = bh = 12(5\sqrt{3}) = 60\sqrt{3}$$



## AREA OF A TRAPEZOID

- 1. Find the area of a trapezoid with base lengths 16 and 18, and height 10.

*Solution:*

If we plug what we've been given into the formula for the area of a trapezoid, we get

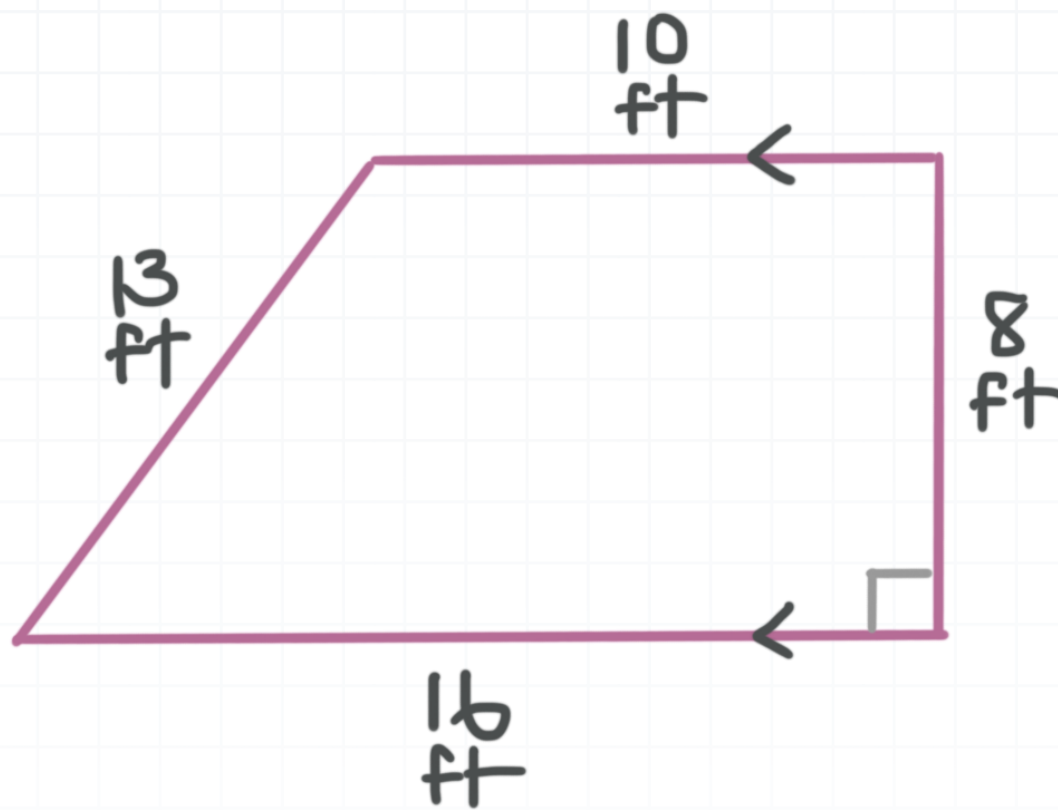
$$A = \frac{1}{2}(\text{height})(\text{base}_1 + \text{base}_2)$$

$$A = \frac{1}{2}(10)(16 + 18)$$

$$A = 170$$

- 2. Find the area of the trapezoid.





*Solution:*

If we plug what we've been given into the formula for the area of a trapezoid, we get

$$A = \frac{1}{2}(\text{height})(\text{base}_1 + \text{base}_2)$$

$$A = \frac{1}{2}(8)(16 + 10)$$

$$A = 104$$

■ 3. Find the exact area of the trapezoid that has congruent 2-meter bases and a height of 4 meters.



*Solution:*

The area of the trapezoid is

$$A = \frac{1}{2}(\text{height})(\text{base}_1 + \text{base}_2)$$

$$A = \frac{1}{2}(4)(2 + 2)$$

$$A = \frac{1}{2}(16)$$

$$A = 8$$

■ 4. The area of a trapezoid is  $60 \text{ m}^2$ . One of the bases has a measure of 7 m and the height of the trapezoid is 10 m. Find the length of the other base.

*Solution:*

We can plug what we know into the formula for the area of a trapezoid, and then solve for the length of the second base.

$$A = \frac{1}{2}(\text{height})(\text{base}_1 + \text{base}_2)$$

$$60 = \frac{1}{2}(10)(7 + \text{base}_2)$$

$$120 = 10(7 + \text{base}_2)$$

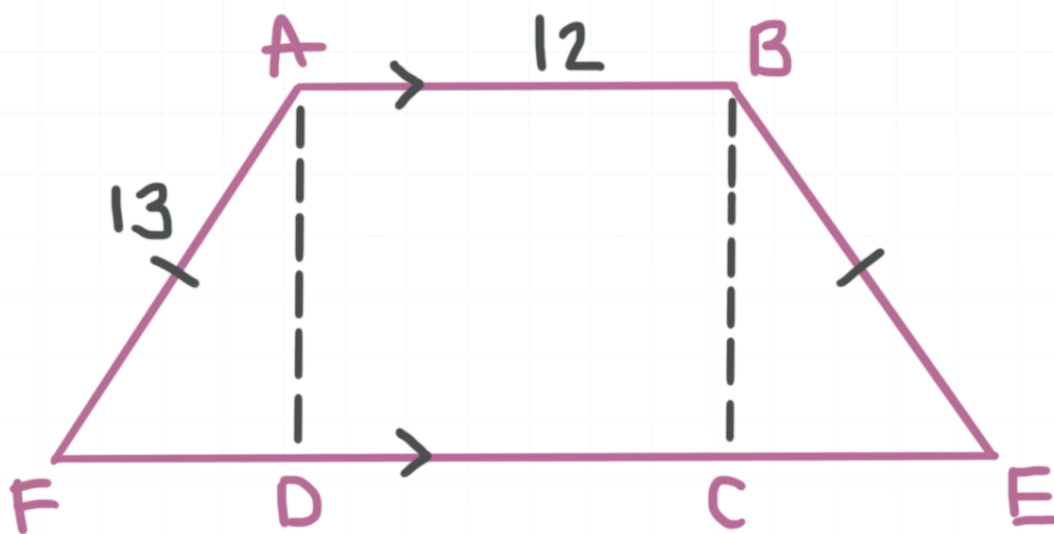


$$120 = 70 + 10\text{base}_2$$

$$50 = 10\text{base}_2$$

$$\text{base}_2 = 5$$

- 5. Find the area of trapezoid  $ABEF$ , if  $ABCD$  is a square.



*Solution:*

We know that  $AB = AD$  because  $ABCD$  is a square. The height of the trapezoid is 12. Use the Pythagorean Theorem to find  $FD$  and  $CE$ .

$$FD^2 + AD^2 = AF^2$$

$$FD^2 + 12^2 = 13^2$$

$$FD = 5 = CE$$

Then  $\overline{FE} = 5 + 12 + 5 = 22$ . Therefore, the area of the trapezoid is



$$A = \frac{1}{2}(\text{height})(\text{base}_1 + \text{base}_2)$$

$$A = \frac{1}{2}(12)(22 + 12)$$

$$A = 204$$



## AREA OF A TRIANGLE

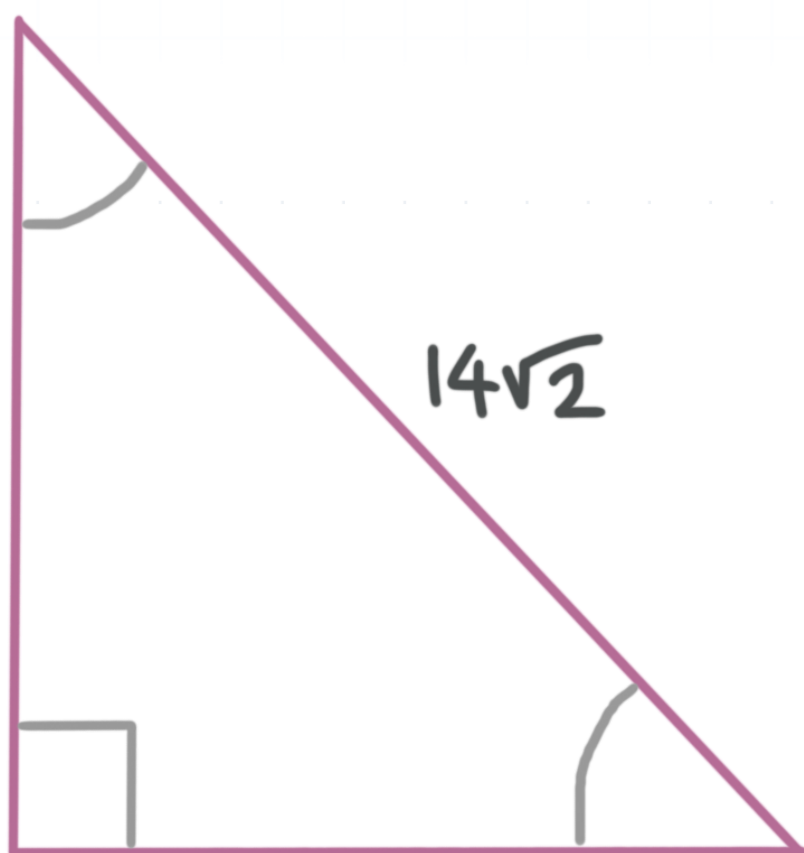
- 1. Find the area of a triangle that has base length 16 and height 14.

*Solution:*

The area of the triangle is

$$A = \frac{1}{2}bh = \frac{1}{2}(16)(14) = 112$$

- 2. Find the area of the triangle.

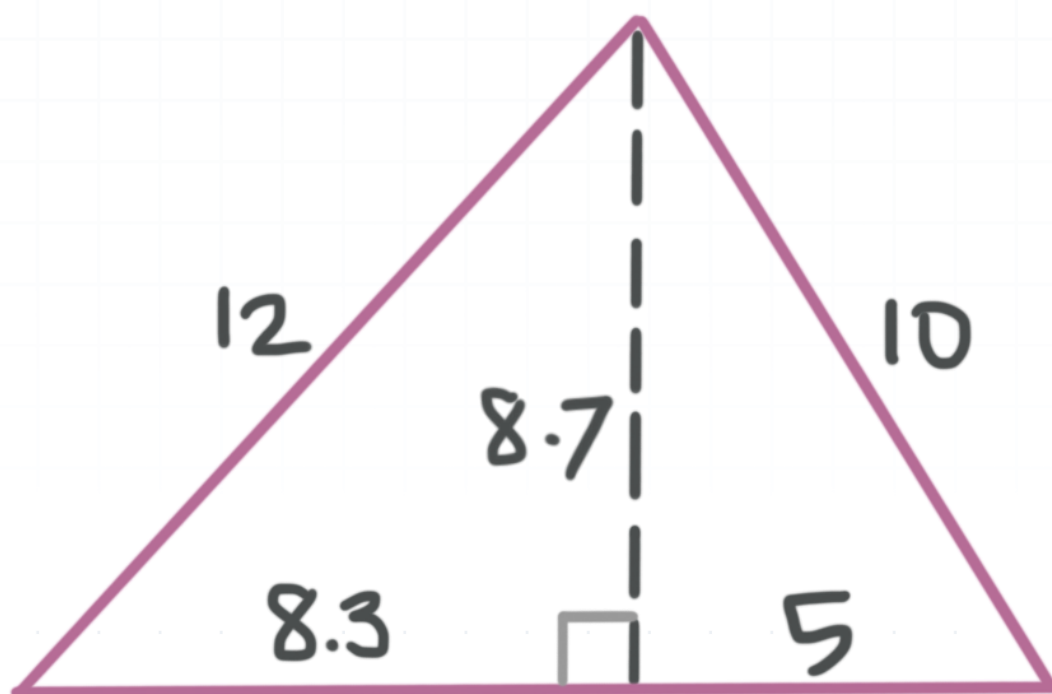


*Solution:*

Using 45 – 45 – 90 rules, we find that the base of the triangle has length  $b = 14$  and height  $h = 14$ . Then the area of the triangle is

$$A = \frac{1}{2}bh = \frac{1}{2}(14)(14) = 98$$

■ 3. Find the area of the triangle.



*Solution:*

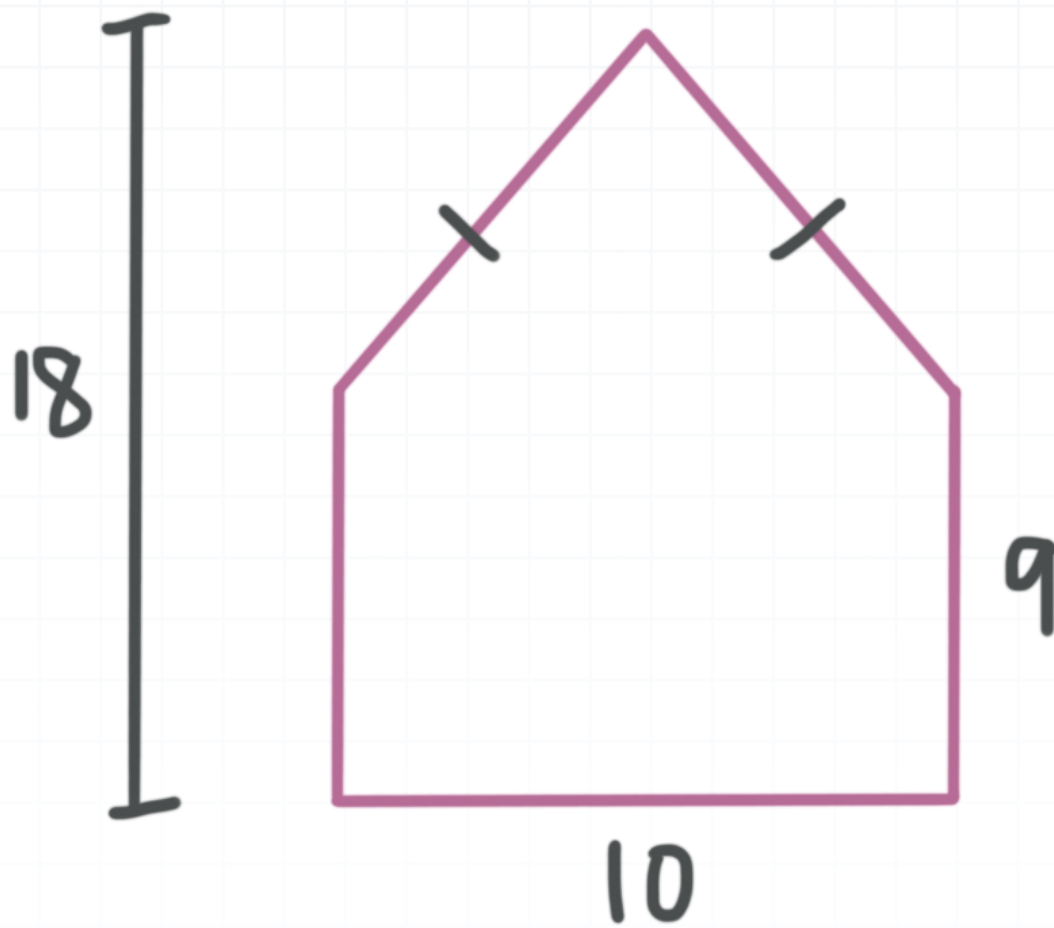
The area of the triangle is

$$A = \frac{1}{2}bh = \frac{1}{2}(13.3)(8.7) = 57.855$$





- 4. Find the area of the figure below.



*Solution:*

The area of the rectangle is

$$A_R = bh = (10)(9) = 90$$

The area of the triangle is

$$A_T = \frac{1}{2}(bh) = \frac{1}{2}(10)(9) = 45$$

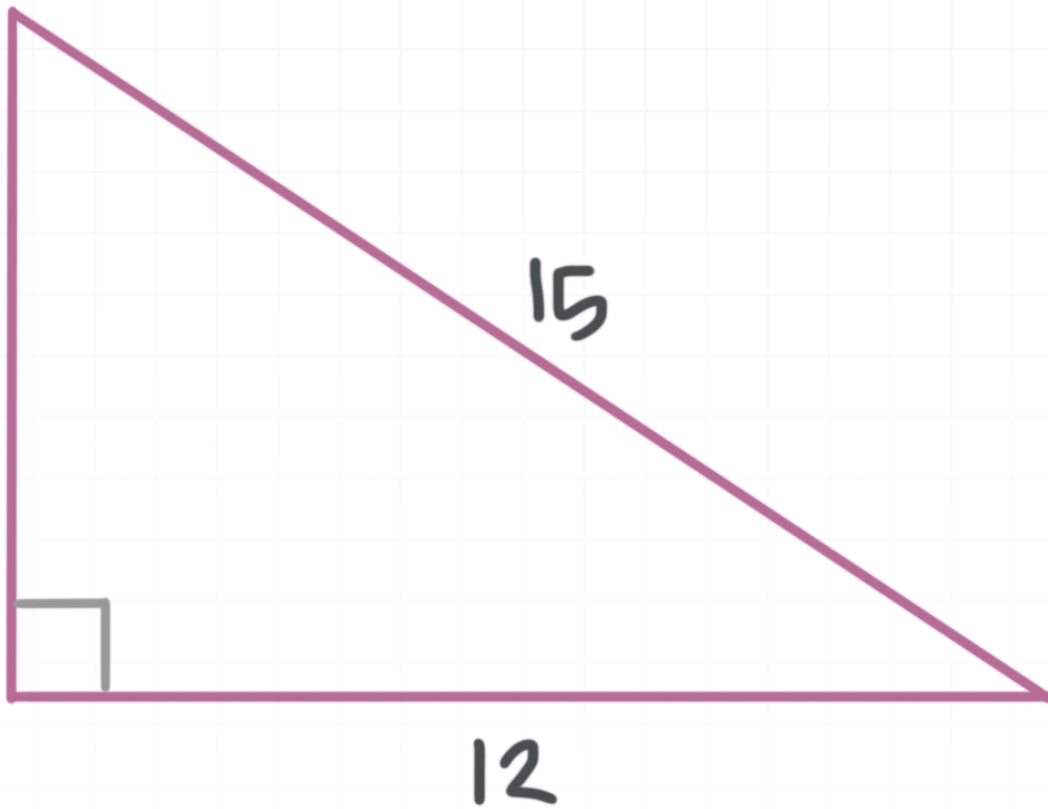
Therefore, the area of the entire region is

$$A = A_R + A_T = 90 + 45 = 135$$



## PERIMETER OF A TRIANGLE

- 1. Find the perimeter of the triangle.



*Solution:*

Let the missing side be  $x$ .

$$x^2 + 12^2 = 15^2$$

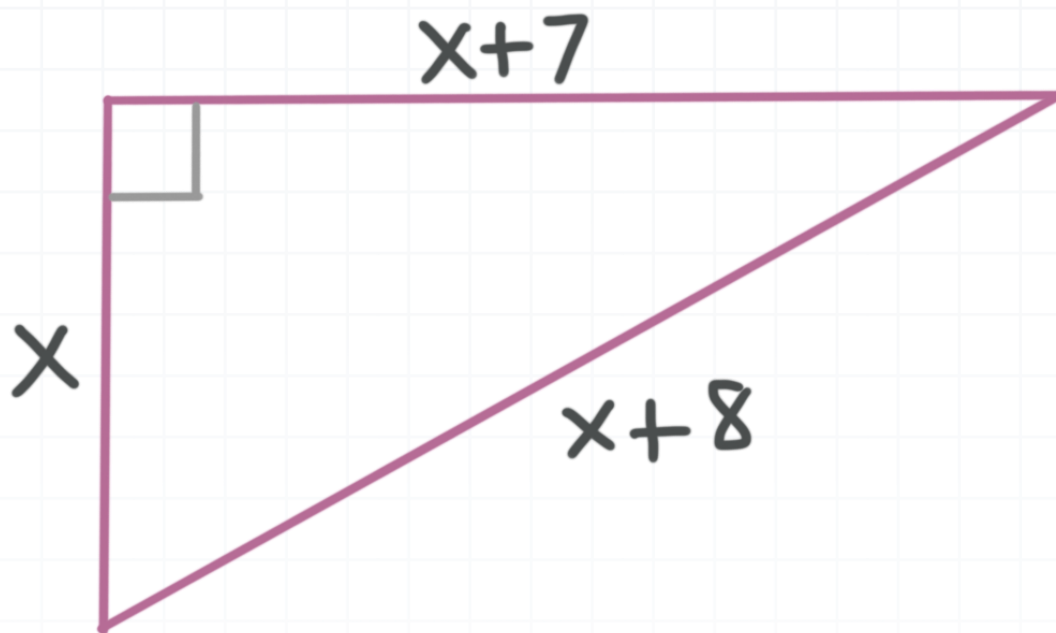
$$x^2 = 15^2 - 12^2 = 81$$

$$x = \sqrt{81} = 9$$

The perimeter of the triangle is  $9 + 12 + 15 = 36$ .



- 2. Find the perimeter of the triangle.



*Solution:*

The perimeter can be found by plugging the side lengths into the Pythagorean Theorem.

$$x^2 + (x + 7)^2 = (x + 8)^2$$

$$x^2 + x^2 + 14x + 49 = x^2 + 16x + 64$$

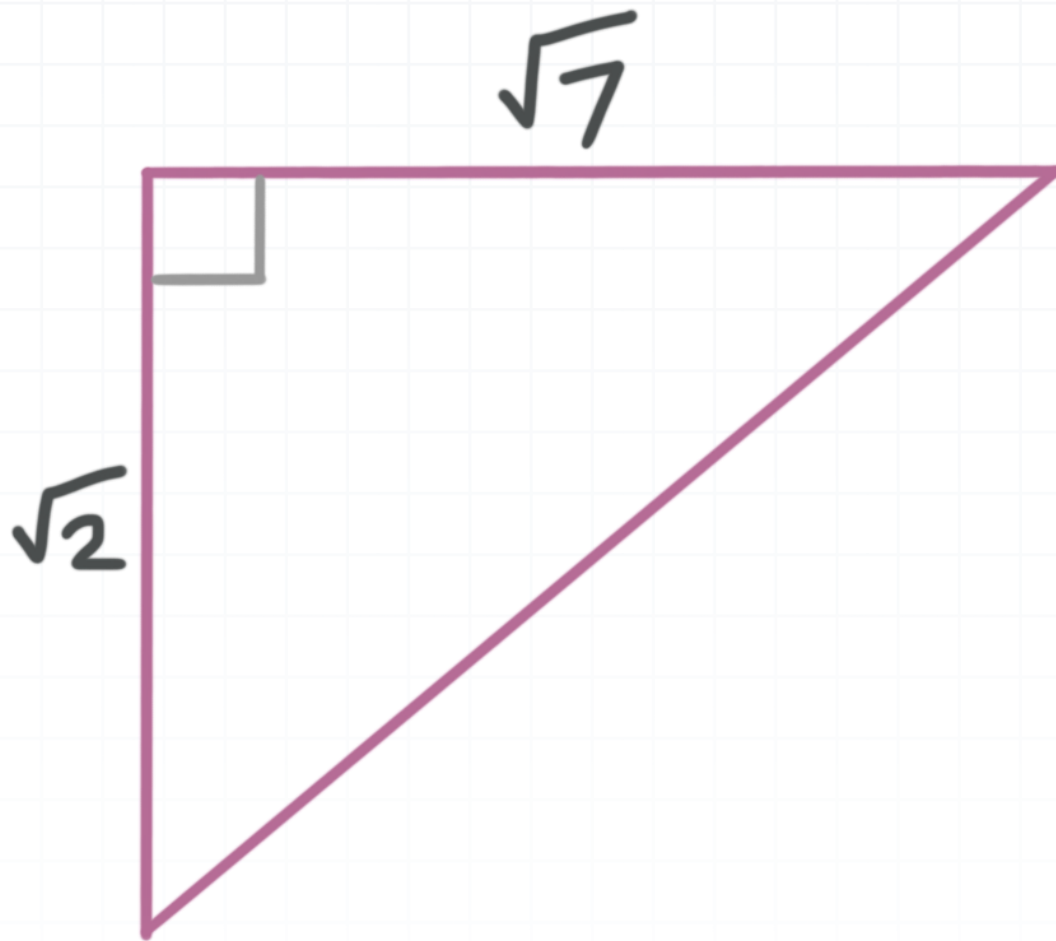
$$x^2 - 2x - 15 = 0$$

$$(x - 5)(x + 3) = 0$$

So  $x = 5$  or  $x = -3$ . But one of the legs of the triangle is  $x$ , which means  $x$  cannot have a negative value, because that would mean we'd have a negative side length. Therefore,  $x = 5$  and the side lengths must be 5, 12, and 13. Which means the perimeter of the triangle is  $5 + 12 + 13 = 30$ .



- 3. Find the exact perimeter of the triangle.



*Solution:*

Plug the side lengths into the Pythagorean Theorem to find the length of the hypotenuse.

$$(\sqrt{2})^2 + (\sqrt{7})^2 = c^2$$

$$2 + 7 = c^2$$

$$c^2 = 9$$

$$c = \sqrt{9} = 3$$

Therefore, the perimeter of the triangle is  $\sqrt{2} + \sqrt{7} + 3$ .



- 4. Find the perimeter of a right, isosceles triangle, to the nearest hundredth, in which one of the legs measures 5 inches.

*Solution:*

Draw a right, isosceles triangle and note that both legs must be 5 inches long. Find the hypotenuse using the Pythagorean Theorem.

$$c^2 = 5^2 + 5^2$$

$$c^2 = 50$$

$$c = \sqrt{50} = 5\sqrt{2}$$

Then the perimeter is

$$P = 5 + 5 + 5\sqrt{2} = 10 + 5\sqrt{2} = 10 + 7.07 \approx 17.07 \text{ inches}$$



## AREA OF A CIRCLE

- 1. Find the area of a circle to the nearest hundredth with a diameter of 44 inches.

*Solution:*

If the diameter is 44 inches, then the radius is half that: 22 inches. Plug the radius into the formula for the area of a circle.

$$A = \pi r^2$$

$$A = \pi(22)^2$$

$$A = 1,520.53$$

- 2. The area of a circle is 300 cm<sup>2</sup>. Find the length of the radius to the nearest tenth of a centimeter.

*Solution:*

Plug the area into the formula for the area of a circle, and then solve for the radius,  $r$ .

$$A = \pi r^2$$



$$300 = \pi r^2$$

$$r^2 = \frac{300}{\pi} = 95.5$$

$$r = \sqrt{95.5} = \approx 9.8$$

- 3. Find the exact area of a circle with a circumference of  $18\pi$ .

*Solution:*

Plug the circumference into the formula for the circumference of a circle.

$$C = d\pi$$

$$18\pi = d\pi$$

$$d = 18$$

Because the diameter has length 18, the length of the radius is  $r = 9$ .

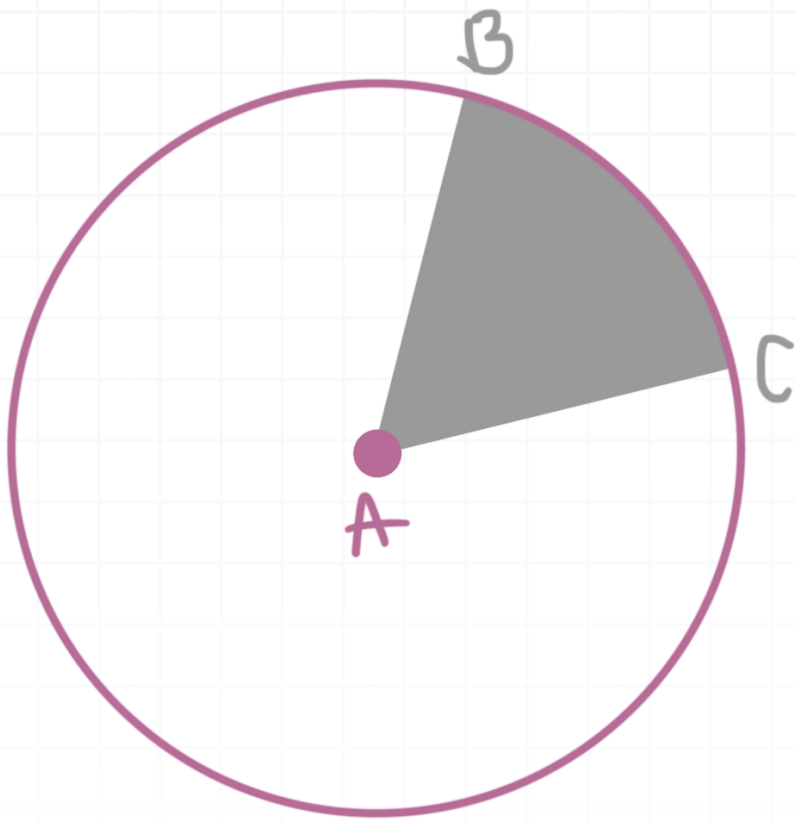
Therefore, the area of a circle is

$$A = \pi(9)^2$$

$$A = 81\pi$$

- 4. Find the area of the shaded region to the nearest tenth if  $m\angle BAC = 60^\circ$  and  $AC = 16$  feet.





*Solution:*

The shaded area represents  $60/360$ , or  $1/6$  of the total area. The area of the full circle is

$$A = \pi r^2 = \pi(16)^2 \approx 804.2$$

so the area of the shaded region, which is  $1/6$ th of the circle, is

$$A = \frac{1}{6}(804.2) \approx 134.0$$





## CIRCUMFERENCE OF A CIRCLE

- 1. To the nearest hundredth, find the circumference of a circle that has a radius of 14 feet.

*Solution:*

The circumference of the circle is

$$C = 2\pi r = 2\pi(14) = 28\pi \approx 87.96$$

- 2. Find the area of a circle with a circumference of 400 ft.

*Solution:*

We can use the formula for circumference.

$$C = 2\pi r$$

$$400 = 2\pi r$$

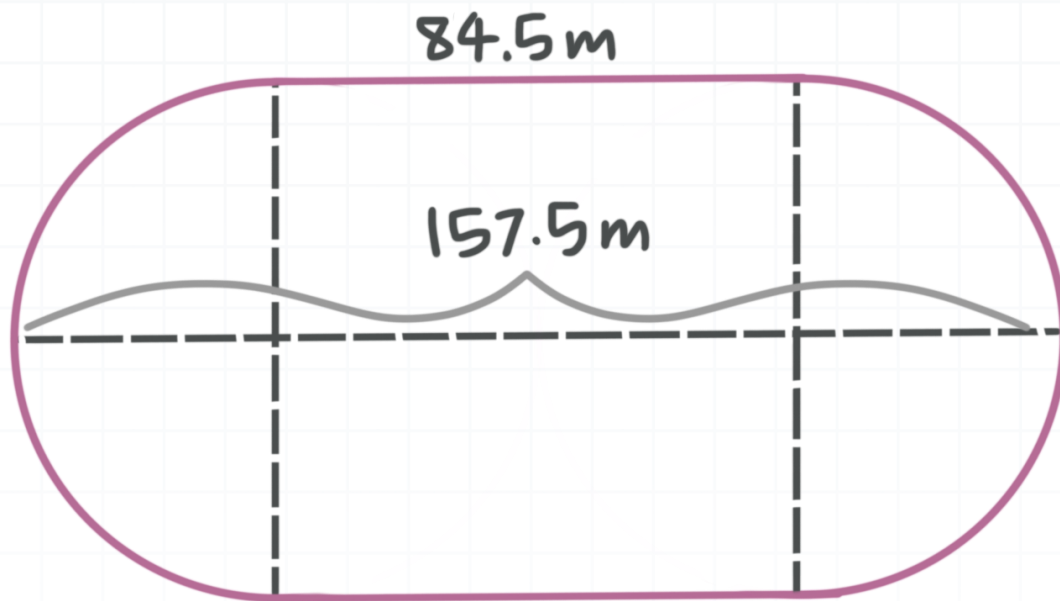
$$r = \frac{200}{\pi} \approx 63.66$$

Then the area of the circle is

$$A = \pi(63.66)^2 \approx 12,731.61$$



- 3. To the nearest tenth, find the distance around the following track.



*Solution:*

The length is comprised of two straight stretches and two semicircles. The length of the radius of each semicircle must be

$$\frac{(157.5 - 84.5)}{2} = 36.5$$

The circumference of each semicircle is

$$\frac{1}{2}(2)(36.5)\pi \approx 114.67$$

$$84.5 + 84.5 + 114.67 + 114.67 = 398.3 \text{ meters}$$



