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At ASSIGNMENT - 4 A* ALGORITHM: 1. ROBOT NAVIGATION: CODE:

```
EMPTY = 0
WALL = 1
SELECTED = 2
class Node:
  def init (self, x, y, prev = None):
    self.x = x
    self.y = y
    self.prev = prev
  def __eq__(self, other):
    if isinstance(other, Node):
       return self.x == other.x and self.y == other.y
    elif isinstance(other, tuple):
       return self.x == other[0] and self.y == other[1]
  def __repr__(self):
    return str((self.x, self.y))
  def __hash__(self):
    return (self.x, self.y). hash ()
  def man dist(self, to) -> int:
    return abs(self.x - to.x) + abs(self.y - to.y)
  def heu(self, goal) -> int:
    return self.man_dist(goal)
  def neighbours(self, board) -> list:
    neigh = [
       (self.x, self.y - 1),
       (self.x - 1, self.y),
       (self.x + 1, self.y),
       (self.x, self.y + 1),
    1
```

```
ugly_neighbours = []
    for n in neigh:
      x, y = n
      if x < 0 or y < 0:
         ugly_neighbours.append((x, y))
       elif x \ge len(board) or y \ge len(board[0]):
         ugly_neighbours.append((x, y))
      elif board[x][y] == WALL:
         ugly neighbours.append((x, y))
    for ugly in ugly neighbours:
      neigh.remove(ugly)
    return [Node(n[0], n[1], self) for n in neigh]
Board = list[list[Node]]
def display board(board, initial: Node, goal: Node) -> None:
  print(", '-' * len(board[0] * 3))
  for i, row in enumerate(board):
    print(end='|')
    for j, col in enumerate(row):
      if Node(i, j) == initial:
         ch='S'
      elif Node(i, j) == goal:
         ch='G'
      elif col == EMPTY:
         ch=' '
      elif col == WALL:
         ch='*'
      elif col == SELECTED:
         ch='$'
      print("{:>3}".format(ch), end=")
    print(end='|\n')
  print(", '-' * len(board[0]) * 3)
def start(board, initial: Node, goal: Node) -> Node:
  opened = []
  closed = [Node(initial.x, initial.y)]
```

```
d board = []
  for row in board:
    d_board.append([])
    for col in row:
      d board[-1].append(col)
  previous = set()
  while len(closed) > 0:
    closed.sort(key = lambda n: n.heu(initial) + n.heu(goal))
    current = closed.pop(0)
    opened.append(current)
    if current in previous:
      continue
    else:
      previous.add(current)
    d board[current.x][current.y] = SELECTED
    print("\n\nOpen List : ", opened)
    print("\nClose List : ", closed)
    display board(d board, initial, goal)
    if current == goal:
       print("\n\n\nReached goal!")
      break
    for neighbour in current.neighbours(board):
      if neighbour not in previous:
         closed.append(neighbour)
  return current
def safety_check(board, initial: tuple[int, int], goal: tuple[int, int]):
  if board[initial[0]][initial[1]] == WALL:
    raise ValueError("\nInitial Position cannot be a wall")
  if board[goal[0]][goal[1]] == WALL:
    raise ValueError("\nGoal Position cannot be a wall")
def main():
  board = [
    [0, 0, 0, 0, 0, 0, 0, 0, 0, 0,]
    [0, 1, 0, 0, 1, 1, 1, 1, 0,],
    [0, 1, 0, 0, 0, 0, 0, 1, 0,],
```

```
[0, 0, 1, 1, 1, 1, 1, 1, 0,],
    [0, 0, 0, 0, 0, 0, 0, 0, 0, 0,]
  ]
  initial = (3, 0)
  goal = (2, 5)
  safety_check(board, initial, goal)
  end = start(board, Node(initial[0], initial[1]), Node(goal[0], goal[1]))
  print("\n\n\nBest route : ")
  path = []
  while end:
    path.append((end.x, end.y))
    end = end.prev
  d_board = []
  for row in board:
    d_board.append([])
    for col in row:
       d_board[-1].append(col)
  for (x, y) in path:
    d_board[x][y] = SELECTED
  display_board(d_board, initial, goal)
if __name__ == '__main___':
  main()
```

1. CITY PROBLEM:

```
SOURCE = "Pune"
DESTINATION = "Aurangabad"
DISTANCE FROM DESTINATION = {
  "Solapur": 340,
  "Satara": 177,
  "Navi Mumbai": 181,
  "Nashik": 133,
  "Ahmednagar": 180,
  "Aurangabad": 0,
  "Nanded": 451,
  "Latur": 373,
 "Pune": 424,
}
GRAPH = \{\}
def put_city(city1: str, city2: str, weight: int) -> None:
  global GRAPH
  if city1 in GRAPH:
    GRAPH[city1].append((city2, weight))
  else:
    GRAPH[city1] = [(city2, weight)]
  if city2 in GRAPH:
    GRAPH[city2].append((city1, weight))
  else:
    GRAPH[city2] = [(city1, weight)]
def generate_map() -> None:
  put city("Pune", "Navi Mumbai", 106)
 put_city("Pune", "Satara", 112)
  put_city("Pune", "Solapur", 234)
  put city("Solapur", "Satara", 203)
  put city("Solapur", "Latur", 104)
 put_city("Nanded", "Latur", 113)
  put city("Nanded", "Aurangabad", 221)
 put_city("Nashik", "Aurangabad", 159)
```

```
put_city("Nanded", "Ahmednagar", 267)
  put_city("Pune", "Ahmednagar", 120)
  put_city("Nashik", "Pune", 165)
  put_city("Nashik", "Navi Mumbai", 136)
def distance(from_: str, to: str) -> int:
  if from == to:
    return 0
  array = GRAPH[from ]
  for name, weight in array:
    if name == to:
      return weight
  return 10 ** 10
class Node:
  def init (self, city: str, prev: object, weight: int) -> None:
    self.city = city
    self.prev = prev
    self.weight = weight
  def __repr__(self) -> str:
    return self.city
  def eq (self, other) -> bool:
    if isinstance(other, Node):
      return self.city == other.city
    elif isinstance(other, str):
      return self.city == other
    else:
      return False
def objective(city, parent) -> int:
  return distance(city, parent) + DISTANCE FROM DESTINATION[city]
def main() -> None:
  generate_map()
  print("\nStart city : Pune")
  print("\nDestination city : Aurangabad")
  current = Node(SOURCE, None, 0)
  opened = []
```

```
closed = [current]
  while len(closed) > 0:
    print("\nOpened list : ", opened)
    print("\nClosed list : ", closed)
    closed.sort(
         key=lambda node: objective(node.city, current),
         reverse=True
    )
    current = closed.pop()
    if current not in opened:
      opened.append(current)
    if current == DESTINATION:
      print("\n\nReached Destination!!".center(40, ' '))
      break
    print("\nSelected City : ", current)
    print(f"\nThe neighbouring cities of {current} are : ")
    for name, dist in GRAPH[current.city]:
       print(f"{name:>12} with distance {dist}")
      if name not in opened:
         closed.append(Node(name, current, dist))
    print()
  path = []
  while current:
    path.append(current)
    current = current.prev
  print("\n\nComplete Path : ")
  for city in path[::-1]:
    if city.prev:
      print(f"{city.prev.city} to {city.city} with distance {city.weight}")
if __name__ == '__main___':
  main()
```

```
Start city: Pune
Destination city: Aurangabad
Opened list : []
Closed list: [Pune]
Selected City: Pune
The neighbouring cities of Pune are :
Navi Mumbai with distance 106
Satara with distance 112
      Solapur with distance 234
  Ahmednagar with distance 120
Nashik with distance 165
Opened list: [Pune]
Closed list : [Navi Mumbai, Satara, Solapur, Ahmednagar, Nashik]
Selected City: Navi Mumbai
The neighbouring cities of Navi Mumbai are :
Pune with distance 106
Nashik with distance 136
Opened list : [Pune, Navi Mumbai]
Closed list : [Solapur, Ahmednagar, Nashik, Satara, Nashik]
Selected City: Nashik
The neighbouring cities of Nashik are :
Aurangabad with distance 159
 Pune with distance 165
Navi Mumbai with distance 136
Opened list : [Pune, Navi Mumbai, Nashik]
Closed list: [Solapur, Ahmednagar, Satara, Nashik, Aurangabad]
```

```
Selected City: Navi Mumbai

The neighbouring cities of Navi Mumbai are:
    Pune with distance 186
    Nashik with distance 136

Opened list: [Pune, Navi Mumbai]

Closed list: [Solapur, Ahmednagar, Nashik, Satara, Nashik]

Selected City: Nashik

The neighbouring cities of Nashik are:
    Aurangabad with distance 159
    Pune with distance 155
    Navi Mumbai with distance 136

Opened list: [Pune, Navi Mumbai, Nashik]

Closed list: [Solapur, Ahmednagar, Satara, Nashik, Aurangabad]

Selected City: Nashik

The neighbouring cities of Nashik are:
    Aurangabad with distance 159
    Pune with distance 155
    Navi Mumbai with distance 136

Opened list: [Pune, Navi Mumbai, Nashik]

Closed list: [Solapur, Ahmednagar, Satara, Aurangabad, Aurangabad]

Reached Destination!!

Complete Path:
    Pune to Nashik with distance 165
    Nashik to Aurangabad with distance 159
```

2. <u>8 PUZZLE:</u>

```
GOAL = {
  1: 1, 2: 2, 3: 3,
  4: 8, 5: -1, 6: 4,
  7: 7, 8: 6, 9: 5,
t board = dict[int, int]
class Node:
  def init (self, board: dict[int, int], steps: int, prev=None, op=None):
    self.board = board.copy()
    self.steps = steps
    self.prev = prev
    self.operation = op
  def eq (self, other):
    return self.board == other.board
  def hash (self) -> int:
    return heuristic(self.board)
  def repr (self):
    return str(self.heu())
  def heu(self) -> int:
    return self.steps + heuristic(self.board)
def get_empty_pos(puzzle: t_board) -> int:
  for key in puzzle:
    if puzzle[key] == -1:
      return key
def move_up(puzzle: t_board):
  pos = get_empty_pos(puzzle)
  puzzle[pos], puzzle[pos - 3] = puzzle[pos - 3], puzzle[pos]
  return puzzle
```

```
def move down(puzzle: t board):
  pos = get empty pos(puzzle)
  puzzle[pos], puzzle[pos + 3] = puzzle[pos + 3], puzzle[pos]
  return puzzle
def move right(puzzle: t board):
  pos = get empty pos(puzzle)
  puzzle[pos], puzzle[pos + 1] = puzzle[pos + 1], puzzle[pos]
  return puzzle
def move left(puzzle: t board):
  pos = get empty pos(puzzle)
  puzzle[pos], puzzle[pos - 1] = puzzle[pos - 1], puzzle[pos]
  return puzzle
def get available operations(puzzle: t board):
  operations = {
    move up,
    move left, move right,
    move down,
  empty pos = get empty pos(puzzle)
  if empty pos in {1, 2, 3}:
    operations.remove(move_up)
  if empty pos in {7, 8, 9}:
    operations.remove(move_down)
  if empty pos in {3, 6, 9}:
    operations.remove(move right)
  if empty_pos in {1, 4, 7}:
    operations.remove(move left)
  return operations
def get operation name(op):
  return {
    move up: "\nMove Empty Slot UP",
    move down: "\nMove Empty Slot DOWN",
    move left: "\nMove Empty Slot LEFT",
    move right: "\nMove Empty Slot RIGHT",
  }[op]
```

```
def heuristic(puzzle: t board) -> int:
  score = 0
  for key in puzzle:
    if puzzle[key] != GOAL[key]:
       score += 1
  return score
def safe get(puzzle: t board, key: int) -> str:
  if puzzle[key] != -1:
    return puzzle[key]
  return '@'
def display board(puzzle: dict[int, int]):
  print(
    str(safe get(puzzle, 1)).center(3, ' ') +
    str(safe get(puzzle, 2)).center(3, ' ') +
    str(safe get(puzzle, 3)).center(3, ' ')
  )
  print('-' * 10)
  print(
    str(safe_get(puzzle, 4)).center(3, ' ') +
    str(safe get(puzzle, 5)).center(3, ' ') +
    str(safe_get(puzzle, 6)).center(3, ' ')
  )
  print('-' * 10)
  print(
    str(safe_get(puzzle, 7)).center(3, ' ') +
    str(safe get(puzzle, 8)).center(3, ' ') +
    str(safe_get(puzzle, 9)).center(3, ' ')
  )
def start(puzzle) -> Node:
  root = Node(puzzle, 0)
  opened = []
  closed = [root]
  steps = 0
  previous = set()
  best score = 1000
  while len(closed) > 0:
    #print("\n\nOpened:", opened)
```

```
#print("\nClosed:", closed)
    steps += 1
    closed.sort(key=lambda n: n.heu())
    current = closed.pop(0)
    opened.append(current)
    score = heuristic(current.board)
    if score == 0:
      return current
    if current in previous:
      continue
    else:
      previous.add(current)
    if score < best score:
      best_score = score
    for operation in get available operations(current.board):
      child = Node(operation(current.board.copy()), steps, current, operation)
      closed.append(child)
  return current
def main():
  puzzle = {
    1: 1, 2: -1, 3: 3,
    4: 8, 5: 2, 6: 6,
    7: 7, 8: 5, 9: 4,
  }
  print("\nInitial State : ")
  display_board(puzzle)
  print("\nGoal State : ")
  display_board(GOAL)
  node = start(puzzle)
  path: list[Node] = []
  while node:
    path.append(node)
```

```
node = node.prev
path = path[::-1]
path = path[1:]

for i, node in enumerate(path):
    print(f"\n\nStep {i + 1} ")
    if node.operation:
        print(get_operation_name(node.operation))

    display_board(node.board)
    print(f"\nObjective Function Score : {heuristic(node.board) + i + 1}")

if heuristic(path[-1].board) != 0:
    print("\nGoal State not Achieved!")
else:
    print("\nGoal State Achieved")

if __name__ == '__main__':
    main()
```

```
Move Empty Slot DOWN

1 2 3

------
8 6 4

------
7 5 @

Objective Function Score : 6

Step 4

Move Empty Slot LEFT

1 2 3

-----
8 6 4

------
7 @ 5

Objective Function Score : 6

Step 5

Move Empty Slot UP

1 2 3

-----
8 @ 4

------
7 6 5

Objective Function Score : 5

Goal State Achieved
```

BSF ALGORITHM:

3. ROBOT NAVIGATION:

```
EMPTY = 0
WALL = 1
SELECTED = 2

class Node:
    def __init__(self, x, y, prev = None):
        self.x = x
        self.y = y
        self.prev = prev

    def __eq__(self, other):
```

```
if isinstance(other, Node):
       return self.x == other.x and self.y == other.y
    elif isinstance(other, tuple):
       return self.x == other[0] and self.y == other[1]
  def __repr__(self):
    return str((self.x, self.y))
  def hash (self):
    return (self.x, self.y).__hash__()
  def man dist(self, to) -> int:
    return abs(self.x - to.x) + abs(self.y - to.y)
  def heu(self, goal) -> int:
    return self.man dist(goal)
  def neighbours(self, board) -> list:
    neigh = [
      (self.x, self.y - 1),
      (self.x - 1, self.y),
      (self.x + 1, self.y),
      (self.x, self.y + 1),
    1
    ugly_neighbours = []
    for n in neigh:
      x, y = n
      if x < 0 or y < 0:
         ugly neighbours.append((x, y))
      elif x \ge len(board) or y \ge len(board[0]):
         ugly_neighbours.append((x, y))
      elif board[x][y] == WALL:
         ugly_neighbours.append((x, y))
    for ugly in ugly neighbours:
      neigh.remove(ugly)
    return [Node(n[0], n[1], self) for n in neigh]
Board = list[list[Node]]
```

```
def display board(board, initial: Node, goal: Node) -> None:
 print(", '-' * len(board[0] * 3))
  for i, row in enumerate(board):
    print(end='|')
    for j, col in enumerate(row):
      if Node(i, j) == initial:
         ch='S'
      elif Node(i, j) == goal:
         ch='G'
      elif col == EMPTY:
         ch=' '
      elif col == WALL:
         ch='*'
      elif col == SELECTED:
         ch='$'
      print("{:>3}".format(ch), end=")
    print(end='|\n')
 print(", '-' * len(board[0]) * 3)
def start(board, initial: Node, goal: Node) -> Node:
  opened = []
  closed = [Node(initial.x, initial.y)]
  d board = []
  for row in board:
    d board.append([])
    for col in row:
      d board[-1].append(col)
  previous = set()
  while len(closed) > 0:
    closed.sort(key = lambda n: n.heu(goal))
    current = closed.pop(0)
    opened.append(current)
    if current in previous:
      continue
    else:
      previous.add(current)
    d board[current.x][current.y] = SELECTED
    print("\n\nOpen List : ", opened)
    print("\nClose List : ", closed)
```

```
display board(d board, initial, goal)
    if current == goal:
       print("\n\n\nReached goal!!!")
       break
    for neighbour in current.neighbours(board):
       if neighbour not in previous:
         closed.append(neighbour)
  return current
def safety_check(board, initial: tuple[int, int], goal: tuple[int, int]):
  if board[initial[0]][initial[1]] == WALL:
    raise ValueError("\nInitial Position cannot be a wall")
  if board[goal[0]][goal[1]] == WALL:
    raise ValueError("\nGoal Position cannot be a wall")
def main():
  board = [
    [0, 0, 0, 0, 0, 0, 0, 0, 0, 0]
    [0, 1, 0, 0, 1, 1, 1, 1, 0,],
    [0, 1, 0, 0, 0, 0, 0, 1, 0,],
    [0, 0, 1, 1, 1, 1, 1, 1, 0,]
    [0, 0, 0, 0, 0, 0, 0, 0, 0, 0,]
  ]
  initial = (3, 0)
  goal = (2, 5)
  safety check(board, initial, goal)
  end = start(board, Node(initial[0], initial[1]), Node(goal[0], goal[1]))
  print("\nBest Route : ")
  path = []
  while end:
    path.append((end.x, end.y))
    end = end.prev
  d board = []
  for row in board:
    d board.append([])
    for col in row:
       d_board[-1].append(col)
  for (x, y) in path:
```

```
d_board[x][y] = SELECTED
  display_board(d_board, initial, goal)

if __name__ == '__main__':
    main()
```

4. CITY PROBLEM:

```
SOURCE = "Pune"
DESTINATION = "Aurangabad"
DISTANCE_FROM_DESTINATION = {
  "Solapur": 340,
  "Satara": 177,
  "Navi Mumbai": 181,
  "Nashik": 133,
 "Ahmednagar": 180,
  "Aurangabad": 0,
  "Nanded": 451,
  "Latur": 373,
 "Pune": 424,
}
GRAPH = \{\}
def put_city(city1: str, city2: str, weight: int) -> None:
  global GRAPH
```

```
if city1 in GRAPH:
    GRAPH[city1].append((city2, weight))
    GRAPH[city1] = [(city2, weight)]
  if city2 in GRAPH:
    GRAPH[city2].append((city1, weight))
  else:
    GRAPH[city2] = [(city1, weight)]
def generate map() -> None:
  put city("Pune", "Navi Mumbai", 106)
 put city("Pune", "Satara", 112)
 put_city("Pune", "Solapur", 234)
  put city("Solapur", "Satara", 203)
 put_city("Solapur", "Latur", 104)
  put city("Nanded", "Latur", 113)
 put_city("Nanded", "Aurangabad", 221)
 put_city("Nashik", "Aurangabad", 159)
  put_city("Nanded", "Ahmednagar", 267)
  put_city("Pune", "Ahmednagar", 120)
 put city("Nashik", "Pune", 165)
  put_city("Nashik", "Navi Mumbai", 136)
def distance(from : str, to: str) -> int:
  if from == to:
    return 0
  array = GRAPH[from ]
  for name, weight in array:
    if name == to:
      return weight
  return 10 ** 10
class Node:
  def __init__(self, city: str, prev: object, weight: int) -> None:
    self.city = city
    self.prev = prev
    self.weight = weight
  def repr (self) -> str:
```

```
return self.city
  def __eq__(self, other) -> bool:
    if isinstance(other, Node):
      return self.city == other.city
    elif isinstance(other, str):
      return self.city == other
    else:
      return False
def objective(city) -> int:
  return DISTANCE_FROM_DESTINATION[city]
def main() -> None:
  generate_map()
  print("\nStart city : Pune")
  print("\nDestination city : Aurangabad")
  current = Node(SOURCE, None, 0)
  opened = []
  closed = [current]
  while len(closed) > 0:
    print("\nOpened list : ", opened)
    print("\nClosed list : ", closed)
    closed.sort(
         key=lambda node: objective(node.city),
         reverse=True
    )
    current = closed.pop()
    if current not in opened:
      opened.append(current)
    if current == DESTINATION:
      print("\n\nReached Destination!!".center(40, ' '))
      break
    print("\nSelected City : ", current)
    print(f"\nThe neighbouring cities of {current} are : ")
    for name, dist in GRAPH[current.city]:
      print(f"{name:>12} with distance {dist}")
```

```
if name not in opened:
        closed.append(Node(name, current, dist))
    print()

path = []
while current:
    path.append(current)
    current = current.prev

print("\n\nComplete Path : ")
for city in path[::-1]:
    if city.prev:
        print(f"{city.prev.city} to {city.city} with distance {city.weight}")

if __name__ == '__main__':
    main()
```

```
Start city: Pune

Destination city: Aurangabad

Opened list: []

Closed list: [Pune]

Selected City: Pune

The neighbouring cities of Pune are:
Navi Mumbai with distance 106

Satara with distance 112

Solapur with distance 1234

Ahmednagar with distance 120

Nashik with distance 165

Opened list: [Pune]

Closed list: [Navi Mumbai, Satara, Solapur, Ahmednagar, Nashik]

Selected City: Nashik

The neighbouring cities of Nashik are:
Aurangabad with distance 159

Pune with distance 155

Navi Mumbai with distance 136

Opened list: [Pune, Nashik]

Closed list: [Solapur, Navi Mumbai, Ahmednagar, Satara, Aurangabad, Navi Mumbai]

Reached Destination!!

Complete Path:
Pune to Nashik with distance 165

Nashik to Aurangabad with distance 159
```

5. <u>8 PUZZLE:</u>

```
GOAL = {
  1: 1, 2: 2, 3: 3,
  4: 8, 5: -1, 6: 4,
  7: 7, 8: 6, 9: 5,
t board = dict[int, int]
class Node:
  def init (self, board: dict[int, int], steps: int, prev=None, op=None):
    self.board = board.copy()
    self.steps = steps
    self.prev = prev
    self.operation = op
  def __eq__(self, other):
    return self.board == other.board
  def hash (self) -> int:
    return heuristic(self.board)
  def __repr__(self):
    return str(self.heu())
  def heu(self) -> int:
    return self.steps + heuristic(self.board)
def get empty pos(puzzle: t board) -> int:
  for key in puzzle:
    if puzzle[key] == -1:
      return key
def move_up(puzzle: t_board):
  pos = get_empty_pos(puzzle)
  puzzle[pos], puzzle[pos - 3] = puzzle[pos - 3], puzzle[pos]
  return puzzle
def move_down(puzzle: t_board):
```

```
pos = get empty pos(puzzle)
  puzzle[pos], puzzle[pos + 3] = puzzle[pos + 3], puzzle[pos]
  return puzzle
def move_right(puzzle: t_board):
  pos = get empty pos(puzzle)
  puzzle[pos], puzzle[pos + 1] = puzzle[pos + 1], puzzle[pos]
  return puzzle
def move left(puzzle: t board):
  pos = get empty pos(puzzle)
  puzzle[pos], puzzle[pos - 1] = puzzle[pos - 1], puzzle[pos]
  return puzzle
def get_available_operations(puzzle: t_board):
  operations = {
    move up,
    move left, move right,
    move_down,
  }
  empty_pos = get_empty_pos(puzzle)
  if empty pos in {1, 2, 3}:
    operations.remove(move up)
  if empty_pos in {7, 8, 9}:
    operations.remove(move down)
  if empty_pos in {3, 6, 9}:
    operations.remove(move right)
  if empty pos in {1, 4, 7}:
    operations.remove(move_left)
  return operations
def get operation name(op):
  return {
    move up: "\nMove Empty Slot UP",
    move down: "\nMove Empty Slot DOWN",
    move left: "\nMove Empty Slot LEFT",
    move right: "\nMove Empty Slot RIGHT",
  }[op]
```

```
def heuristic(puzzle: t_board) -> int:
  score = 0
  for key in puzzle:
    if puzzle[key] != GOAL[key]:
       score += 1
  return score
def safe_get(puzzle: t_board, key: int) -> str:
  if puzzle[key] != -1:
    return puzzle[key]
  return '@'
def display board(puzzle: dict[int, int]):
  print(
    str(safe_get(puzzle, 1)).center(3, ' ') +
    str(safe_get(puzzle, 2)).center(3, ' ') +
    str(safe get(puzzle, 3)).center(3, ' ')
  print('-' * 10)
  print(
    str(safe get(puzzle, 4)).center(3, ' ') +
    str(safe_get(puzzle, 5)).center(3, ' ') +
    str(safe get(puzzle, 6)).center(3, ' ')
  )
  print('-' * 10)
  print(
    str(safe_get(puzzle, 7)).center(3, ' ') +
    str(safe get(puzzle, 8)).center(3, ' ') +
    str(safe_get(puzzle, 9)).center(3, ' ')
  )
def start(puzzle) -> Node:
  root = Node(puzzle, 0)
  opened = []
  closed = [root]
  steps = 0
  previous = set()
  best_score = 1000
```

```
while len(closed) > 0:
    #print("Opened:", opened)
    #print("Closed:", closed)
    steps += 1
    closed.sort(key=lambda n: heuristic(n.board))
    current = closed.pop(0)
    opened.append(current)
    score = heuristic(current.board)
    if score == 0:
      return current
    if current in previous:
      continue
    else:
      previous.add(current)
    if score < best_score:
      best score = score
    for operation in get_available_operations(current.board):
      child = Node(operation(current.board.copy()),
              steps, current, operation)
      closed.append(child)
  return current
def main():
  puzzle = {
    1: 1, 2: 3, 3: -1,
    4: 8, 5: 2, 6: 6,
    7: 7, 8: 5, 9: 4,
  }
  print("\nInitial State : ")
  display_board(puzzle)
  print("\nGoal State : ")
  display_board(GOAL)
  print(f"The objective function score of this board is {heuristic(puzzle)}")
  node = start(puzzle)
  path: list[Node] = []
```

```
while node:
    path.append(node)
    node = node.prev
  path = path[::-1]
  path = path[1:]
  for i, node in enumerate(path):
    print(f''\setminus n\setminus step \{i + 1\}'')
    if node.operation:
       print(get_operation_name(node.operation))
    display_board(node.board)
    print(f"\nObjective Function Score : {heuristic(node.board) + i + 1}")
  if heuristic(path[-1].board) != 0:
    print("\nGoal State not Achieved!")
  else:
    print("\nGoal State Achieved")
if __name__ == '__main__':
  main()
```

```
Initial State:

1 3 @

8 2 6

7 5 4

Goal State:
1 2 3

7 6 5

The objective function score of this board is 6

Step 1

Move Empty Slot LEFT
1 @ 3

8 2 6

7 5 4

Objective Function Score: 6

Step 2

Move Empty Slot DOWN
1 2 3

8 @ 6

7 5 4

Objective Function Score: 5
```

```
8 6 @
Objective Function Score: 7
Step 4
Move Empty Slot DOWN
7 5 @
Objective Function Score : 7
Step 5
Move Empty Slot LEFT
7 @ 5
Objective Function Score : 7
Step 6
Move Empty Slot UP
8 @ 4
Objective Function Score : 6
Goal State Achieved
```