

## Theoretical task 7.

*Recommendations: all solutions should be short, mathematically strict (unless qualitative explanation is needed), precise with respect to the stated question and clearly written. Solutions may be submitted in any readable format, including images.*

*Submission link: [here](#)*

1. Does the principal component analysis (PCA) transformation require the preliminary feature standardization procedures (centering / scaling)? Explain your answer.
2. Consider some high-dimensional dataset  $X$ . Would different runs of t-SNE (with the same "perplexity" and "maximum iterations" hyper-parameters) produce the same result. Why?
3. There is a dataset  $X$  containing  $10^6$  100-dimensional objects. It has been compressed with PCA (full transformation matrix  $P \in \mathbb{R}^{100 \times 100}$ ) and the compressed dataset  $\hat{X}$  contains  $10^6$  20-dimensional objects.
  - (a) Can one transform new unseen dataset  $Y$  to the same compressed feature space? How?
  - (b) Can one reconstruct the original uncompressed dataset given only  $P$  and  $\hat{X}$ ? How?
4. Provide an example of the two-dimensional ( $d = 2$ ) dataset in the binary classification problem for which the preliminary application of PCA compression to dimensionality  $d = 1$  would hurt the classification accuracy dramatically. Explain, why PCA can hurt the classification accuracy?