

COMPSCI 753

Algorithms for Massive Data

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Tutorial 2: Data stream algorithms

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1 Uniformly sampling

Suppose we have a stream of tuples with the schema

Score(university, courseID, studentID, score)

Assume that universities are unique, but courseID is unique only within a university and likewise, studentID is only unique within a university. For example,

UOA, CS752, sID-001, 10
UOA, CS753, sID-001, 9
UOA, CS753, sID-002, 8
AUT, CS752, sID-001, 9
AUT, CS752, sID-002, 7
AUT, CS753, sID-002, 5

Suppose we want to answer certain queries approximately from a $1/20$ samples of the data. For each query below, indicate how you would construct the sample, i.e. tell what the key attribute should be and the method for sampling.

1. For each course in a university, estimate the average number of students.
2. Estimate the fraction of students who have a GPA of 7 or more.
3. Estimate the fraction of courses where at least half the students got score above 7.

2 Bloom filter

Consider the same situation from our lecture with 8 billion bits and 1 billion members of the set S , calculate the false positive rate if we use numbers of hash functions as $\{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$?

3 Bloom filter

Suppose we have n bits of memory available and set S has m members. Instead of using k hash functions each mapping an element to a bit in the main memory, we could divide the n bits into k subarrays (assume n is divisible by k), and then use the i -th hash function, $i \in [1..k]$, to the i -th subarray.

1. As a function of n , m , and k , what is the probability of a false positive?
2. How does it compare with using k hash functions into a single array?

4 Misra-Gries algorithm

Run the Misra-Gries algorithm with $k = 3$ for the stream below:

$$\{32, 12, 14, 32, 7, 12, 32, 7, 6, 12, 4\}$$

5 CountMin sketch

Applying CountMin sketch to estimate the frequency of each element in the stream below:

$$\{1, 1, 1, 2, 4, 4, 3, 2, 3, 2, 3\}$$

Our CountMin sketch uses $d = 3$ hash functions:

$$h_1(x) = x + 1 \mod 3,$$

$$h_2(x) = 3x + 1 \mod 3,$$

$$h_3(x) = 5x + 2 \mod 3.$$