

Task 1 (4 pts)

1)  $f(x) + g(x) = x^{10} + x^9 + x^8 + x^5 + x^4 + x$

2)  $f(x) - g(x) = x^{10} + x^9 + x^8 + x^5 + x^4 + x$

Similarity is caused by  $\mathbb{Z}_2$ .

3)  $f(x)g(x) = (x^{10} + x^9 + x^5 + x^3 + 1)(x^8 + x^4 + x^3 + x + 1) =$   
 $= x^{18} + x^{14} + x^{13} + x^{12} + x^{12} + x^{11} + x^{11} + x^{10} + x^{10} + x^9 + x^9 + x^8 + x^8 + x^7 + x^7 + x^6 + x^6 + x^5 + x^5 + x^4 + x^4 + x^3 + x^3 + x^2 + x^2 + x + x + 1 =$   
 $x^{18} + x^{17} + x^{14} + x^{13} + x^{12} + x^5 + x + 1$

4) 
$$\begin{array}{r} x^{10} + x^9 + x^5 + x^3 + 1 \\ x^{10} + x^6 + x^5 + x^3 + x^2 \\ \hline x^9 + x^6 + x^2 + 1 \\ x^9 + x^5 + x^4 + x^2 + x \\ \hline x^6 + x^5 + x^4 + x + 1 = r(x) \end{array} \quad \begin{array}{r} x^8 + x^4 + x^3 + x + 1 \\ x^2 + x = q(x) \end{array}$$

5)  $f(x) = x^3 + 1 = a(x) \cdot b(x) = (x+1)(x^2+x+1)$   

$$\begin{array}{r} x^3 + 1 \\ x^3 + x^2 \\ \hline x^2 + 1 \\ x^2 + x \\ \hline x + 1 \\ x + 1 \\ \hline 0 \end{array}$$

6)  $f(x) \cdot g(x) = (x^2 + x + 1)(x^3 + 1) = x^5 + x^2 + x^4 + x + x^3 + 1$   

$$\begin{array}{r} x^5 + x^4 + x^3 + x^2 + x + 1 \\ x^5 + x^2 + x \\ \hline x^4 + x^3 + 1 \\ x^4 + x + 1 \\ \hline x^3 + x + 1 \end{array}$$

Result:  $x^3 + x = f(x)g(x) \mod h(x)$

7)  $\gcd(f(x), g(x))$ : 
$$\begin{array}{r} x^5 + x^4 + 1 \\ x^5 + x^2 + x + 1 \\ \hline x^4 + x^2 + x \end{array}$$

$$\begin{array}{r} x^5 + x^2 + x + 1 \\ x^5 + x^3 + x^2 \\ \hline x^3 + x + 1 \end{array}$$

Result:  $x^3 + x + 1 = \gcd(f(x), g(x))$

8)  $f(x) = x^7 + x^4 + x + 1 = A$ ;  $g(x) = x^8 + x^4 + x^3 + x + 1 = N$ ;  $A \cdot A^{-1} \equiv 1 \pmod{N}$ ;  $A^{-1} = ?$

$$\begin{array}{r} x^8 + x^4 + x^3 + x + 1 \quad \underline{1(x^7 + x^4 + x + 1)} \\ - x^8 + x^5 + x^2 + x \\ \hline x^5 + x^4 + x^3 + x^2 + 1 \end{array}$$

I)  $N = x \cdot A + (x^5 + x^4 + x^3 + x^2 + 1) \Leftrightarrow x^5 + x^4 + x^3 + x^2 + 1 = N + x \cdot A = Q$

$$\begin{array}{r} x^7 + x^4 + x + 1 \quad \underline{1(x^5 + x^4 + x^3 + x^2 + 1)} \\ - x^7 + x^6 + x^5 + x^4 + x^2 \\ \hline x^6 + x^5 + x^2 + x + 1 \\ x^6 + x^5 + x^4 + x^3 + x \\ \hline x^4 + x^3 + x^2 + 1 \end{array}$$

II)  $A = (x^5 + x^4 + x^3 + x^2 + 1)(x^2 + x) + (x^4 + x^3 + x^2 + 1) \Leftrightarrow x^4 + x^3 + x^2 + 1 = A + (x^2 + x)Q$

$$\begin{array}{r} x^5 + x^4 + x^3 + x^2 + 1 \quad \underline{1(x^4 + x^3 + x^2 + 1)} \\ - x^5 + x^4 + x^3 + x \\ \hline x^2 + x + 1 \end{array}$$

III)  $x^5 + x^4 + x^3 + x^2 + 1 = (x^4 + x^3 + x^2 + 1) \cdot x + (x^2 + x + 1) \Leftrightarrow x^2 + x + 1 = Q + x(A + (x^2 + x)Q)$

$$\begin{array}{r} x^4 + x^3 + x^2 + 1 \quad \underline{1(x^2 + x + 1)} \\ - x^4 + x^3 + x^2 \\ \hline x^2 + x + 1 \end{array}$$

IV)  $x^4 + x^3 + x^2 + 1 = (x^2 + x + 1) \cdot x^2 + 1 \Leftrightarrow 1 = A + (x^2 + x)Q + x^2(Q + x(A + (x^2 + x)Q))$

$$\begin{aligned} 1 &= A + (x^2 + x)(N + xA) + x^2(N + xA + x(A + (x^2 + x)(N + xA))) \\ &= A + x^2N + xN + x^3A + x^2A + x^2(N + xA + x(A + x^2N + xN + x^3A + x^2A)) \\ &= A + x^2N + xN + x^3A + x^2A + x^2(N + xA + xA + x^3N + x^2N + x^4A + x^3A) \\ &= A + x^2N + xN + x^3A + x^2A + x^2N + x^3A + x^3A + x^5N + x^4N + x^6A + x^5A \Rightarrow \\ &\Rightarrow A^{-1} = x^6 + x^5 + x^3 + x^2 + 1 \end{aligned}$$

Let's check it:  $A \cdot A^{-1} = (x^7 + x^4 + x + 1)(x^6 + x^5 + x^3 + x^2 + 1) =$

$$\begin{array}{r} x^{13} + x^{12} + x^{10} + x^9 + x^7 + x^{10} + x^9 + x^7 + x^6 + x^4 + x^7 + x^6 + x^4 + x^5 + x^3 + x^2 + 1 \\ - x^{13} + x^{12} + x^7 + x^6 + x^5 + x^2 + x + 1 \\ \hline x^{12} + x^9 + x^8 + x^7 + x^6 + x^2 + x + 1 \\ - x^{12} + x^8 + x^7 + x^5 + x^4 \\ \hline x^9 + x^5 + x^4 + x^2 + x + 1 \\ - x^9 + x^5 + x^4 + x^2 + x \\ \hline x^2 + x + 1 \end{array}$$

(1)  $\Rightarrow A^{-1}$  is correct

### Task 3 (3pts)

$A(x) = x^4 + x^3 + 1$ ;  $GF(2^4)$

$$e^0 = 1$$

$$e^1 = x = e$$

$$e^2 = x^2 = e^1 \cdot e \pmod{P}$$

$$e^3 = x^3 = e^2 \cdot e \pmod{P}$$

$$e^4 = x^3 + 1 = e^3 \cdot e \pmod{P}$$

$$e^5 = x^3 + x + 1 = e^4 \cdot e \pmod{P}$$

$$e^6 = x^3 + x^2 + x + 1 = e^5 \cdot e \pmod{P}$$

$$e^7 = x^2 + x + 1 = e^6 \cdot e \pmod{P}$$

$$e^8 = x^3 + x^2 + x = e^7 \cdot e \pmod{P}$$

$$e^9 = x^2 + 1 = e^8 \cdot e \pmod{P}$$

$$e^{10} = x^3 + x = e^9 \cdot e \pmod{P}$$

$$e^{11} = x^3 + x^2 + 1 = e^{10} \cdot e \pmod{P}$$

$$e^{12} = x + 1 = e^{11} \cdot e \pmod{P}$$

$$e^{13} = x^2 + x = e^{12} \cdot e \pmod{P}$$

$$e^{14} = x^3 + x^2 = e^{13} \cdot e \pmod{P}$$

$$e^{15} = 1 = e^{14} \cdot e \pmod{P} \text{ - final element. } e^{16} \text{ begins a new cycle.}$$

Powers of primitive elements are shown above 'e' symbol.

#### Task 4 (5 pts)

This task I decided to implement not only S-box, Shift Rows and Mix Column, but the whole AES algo with key expansion.

All results are shown on a screenshot below, code in Python3.9 included.



The implemented in Python3 AES ECB 128 contains example encryption and decryption of the plaintext “theruleroflondorheythisisshrinehandmaid” with the key “firelinkfirekeep”.

The **Task4** to run functions on a hex string is also implemented in the code.

All results and mid-states can be seen in the screenshot below.

```
PS G:\Horzine\Учеба\Univ\МАГА\1_курс\ОСЕНЬ3ИМА\МФМС\HW4> python.exe .\aes.py
[*] AES128 (ECB MODE)
[*] Plaintext: theruleroflondorheythisisshrinehandmaid
[*] Key: firelinkfirekeep
SubByteStep_State: [[201, 212, 1, 107], [124, 107, 118, 124], [240, 43, 114, 103], [240, 212, 103, 119]]
ShiftRowsStep_State: [[201, 212, 1, 107], [107, 118, 124, 124], [114, 103, 240, 43], [119, 240, 212, 103]]
MixColumnsStep_State: [[49, 190, 162, 30], [254, 97, 38, 137], [223, 103, 225, 232], [183, 141, 60, 36]]
AddRoundKeyStep_State: [[27, 248, 130, 85], [218, 44, 2, 200], [252, 42, 222, 178], [173, 252, 40, 64]]
SubByteStep_State: [[171, 242, 89, 119], [254, 99, 162, 43], [43, 164, 162, 99], [130, 119, 240, 173]]
ShiftRowsStep_State: [[171, 242, 89, 119], [99, 162, 43, 254], [162, 99, 43, 164], [173, 130, 119, 240]]
MixColumnsStep_State: [[231, 227, 147, 163], [61, 138, 5, 151], [123, 11, 189, 209], [102, 211, 5, 56]]
AddRoundKeyStep_State: [[205, 165, 179, 232], [25, 199, 33, 214], [88, 70, 130, 139], [124, 162, 17, 92]]
SubByteStep_State: [[197, 215, 168, 170], [197, 99, 208, 80], [71, 103, 33, 80], [48, 170, 80, 182]]
ShiftRowsStep_State: [[197, 215, 168, 170], [99, 208, 80, 197], [33, 80, 71, 103], [182, 48, 170, 80]]
MixColumnsStep_State: [[163, 190, 86, 44], [214, 172, 107, 194], [37, 247, 147, 81], [97, 130, 187, 231]]
AddRoundKeyStep_State: [[137, 248, 118, 103], [242, 225, 79, 131], [6, 186, 172, 11], [123, 243, 175, 131]]
[+] B64 (Encrypted): DsKTWF/DmcO5w53Dmck/w67ChcKdLk3Dq3p0ERoNwpvDgAhmLCHCnc0oOUXCvgwkSnJRXBo5w7okw4DDqgEYw5HDmCOP
[+] Decrypted: theruleroflondorheythisisshrinehandmaid
[*] Task:
Default state: [[200, 251, 84, 49], [119, 238, 205, 229], [195, 19, 206, 240], [79, 115, 165, 238]]
SubByteStep_State: [[232, 15, 32, 199], [245, 40, 189, 217], [46, 125, 139, 140], [132, 143, 6, 40]]
ShiftRowsStep_State: [[232, 15, 32, 199], [40, 189, 217, 245], [139, 140, 46, 125], [40, 132, 143, 6]]
MixColumnsStep_State: [[16, 202, 145, 234], [22, 101, 116, 183], [181, 38, 47, 194], [208, 51, 146, 214]]
Result: 0x10 0xca 0x91 0xea 0x16 0x65 0x74 0xb7 0xb5 0x26 0x2f 0xc2 0xd0 0x33 0x92 0xd6
PS G:\Horzine\Учеба\Univ\МАГА\1_курс\ОСЕНЬ3ИМА\МФМС\HW4>
```

### Code in Python3:

```
from string import *
from random import *
from base64 import *
from binascii import *

Nb = 4
Nk = 4
Nr = 10

Rcon = [
    [0x01, 0x02, 0x04, 0x08, 0x10, 0x20, 0x40, 0x80, 0x1b, 0x36],
    [0x00, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00],
    [0x00, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00],
    [0x00, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00]
]

Sbox = [
    [0x63, 0x7c, 0x77, 0x7b, 0xf2, 0x6b, 0x6f, 0xc5, 0x30, 0x01, 0x67,
    0x2b, 0xfe, 0xd7, 0xab, 0x76],
    [0xca, 0x82, 0xc9, 0x7d, 0xfa, 0x59, 0x47, 0xf0, 0xad, 0xd4, 0xa2, 0xaf,
    0x9c, 0xa4, 0x72, 0xc0],
    [0xb7, 0xfd, 0x93, 0x26, 0x36, 0x3f, 0xf7, 0xcc, 0x34, 0xa5, 0xe5, 0xf1,
    0x71, 0xd8, 0x31, 0x15],
    [0x04, 0xc7, 0x23, 0xc3, 0x18, 0x96, 0x05, 0x9a, 0x07, 0x12, 0x80,
    0xe2, 0xeb, 0x27, 0xb2, 0x75],
    [0x09, 0x83, 0x2c, 0x1a, 0x1b, 0x6e, 0x5a, 0xa0, 0x52, 0x3b, 0xd6,
    0xb3, 0x29, 0xe3, 0x2f, 0x84],
    [0x53, 0xd1, 0x00, 0xed, 0x20, 0xfc, 0xb1, 0x5b, 0x6a, 0xcb, 0xbe,
    0x39, 0x4a, 0x4c, 0x58, 0xcf],
    [0xd0, 0xef, 0xaa, 0xfb, 0x43, 0x4d, 0x33, 0x85, 0x45, 0xf9, 0x02, 0x7f,
    0x50, 0x3c, 0x9f, 0xa8],
    [0x51, 0xa3, 0x40, 0x8f, 0x92, 0x9d, 0x38, 0xf5, 0xbc, 0xb6, 0xda,
    0x21, 0x10, 0xff, 0xf3, 0xd2],
    [0xcd, 0x0c, 0x13, 0xec, 0x5f, 0x97, 0x44, 0x17, 0xc4, 0xa7, 0x7e, 0x3d,
    0x64, 0x5d, 0x19, 0x73],
```

```

[0x60, 0x81, 0x4f, 0xdc, 0x22, 0x2a, 0x90, 0x88, 0x46, 0xee, 0xb8,
0x14, 0xde, 0x5e, 0x0b, 0xdb],
[0xe0, 0x32, 0x3a, 0x0a, 0x49, 0x06, 0x24, 0x5c, 0xc2, 0xd3, 0xac,
0x62, 0x91, 0x95, 0xe4, 0x79],
[0xe7, 0xc8, 0x37, 0x6d, 0x8d, 0xd5, 0x4e, 0xa9, 0x6c, 0x56, 0xf4, 0xea,
0x65, 0x7a, 0xae, 0x08],
[0xba, 0x78, 0x25, 0x2e, 0x1c, 0xa6, 0xb4, 0xc6, 0xe8, 0xdd, 0x74,
0x1f, 0x4b, 0xbd, 0x8b, 0x8a],
[0x70, 0x3e, 0xb5, 0x66, 0x48, 0x03, 0xf6, 0x0e, 0x61, 0x35, 0x57,
0xb9, 0x86, 0xc1, 0x1d, 0x9e],
[0xe1, 0xf8, 0x98, 0x11, 0x69, 0xd9, 0x8e, 0x94, 0x9b, 0x1e, 0x87,
0xe9, 0xce, 0x55, 0x28, 0xdf],
[0x8c, 0xa1, 0x89, 0x0d, 0xbf, 0xe6, 0x42, 0x68, 0x41, 0x99, 0x2d,
0x0f, 0xb0, 0x54, 0xbb, 0x16]
]

```

```

SboxInv = [
[0x52, 0x09, 0x6a, 0xd5, 0x30, 0x36, 0xa5, 0x38, 0xbf, 0x40, 0xa3,
0x9e, 0x81, 0xf3, 0xd7, 0xfb],
[0x7c, 0xe3, 0x39, 0x82, 0x9b, 0x2f, 0xff, 0x87, 0x34, 0x8e, 0x43, 0x44,
0xc4, 0xde, 0xe9, 0xcb],
[0x54, 0x7b, 0x94, 0x32, 0xa6, 0xc2, 0x23, 0x3d, 0xee, 0x4c, 0x95,
0x0b, 0x42, 0xfa, 0xc3, 0x4e],
[0x08, 0x2e, 0xa1, 0x66, 0x28, 0xd9, 0x24, 0xb2, 0x76, 0x5b, 0xa2,
0x49, 0x6d, 0x8b, 0xd1, 0x25],
[0x72, 0xf8, 0xf6, 0x64, 0x86, 0x68, 0x98, 0x16, 0xd4, 0xa4, 0x5c, 0xcc,
0x5d, 0x65, 0xb6, 0x92],
[0x6c, 0x70, 0x48, 0x50, 0xfd, 0xed, 0xb9, 0xda, 0x5e, 0x15, 0x46,
0x57, 0xa7, 0x8d, 0x9d, 0x84],
[0x90, 0xd8, 0xab, 0x00, 0x8c, 0xbc, 0xd3, 0x0a, 0xf7, 0xe4, 0x58,
0x05, 0xb8, 0xb3, 0x45, 0x06],
[0xd0, 0x2c, 0x1e, 0x8f, 0xca, 0x3f, 0x0f, 0x02, 0xc1, 0xaf, 0xbd, 0x03,
0x01, 0x13, 0x8a, 0x6b],
[0x3a, 0x91, 0x11, 0x41, 0x4f, 0x67, 0xdc, 0xea, 0x97, 0xf2, 0xcf, 0xce,
0xf0, 0xb4, 0xe6, 0x73],
[0x96, 0xac, 0x74, 0x22, 0xe7, 0xad, 0x35, 0x85, 0xe2, 0xf9, 0x37,
0xe8, 0x1c, 0x75, 0xdf, 0x6e],
[0x47, 0xf1, 0x1a, 0x71, 0x1d, 0x29, 0xc5, 0x89, 0x6f, 0xb7, 0x62,
0x0e, 0xaa, 0x18, 0xbe, 0x1b],
[0xfc, 0x56, 0x3e, 0x4b, 0xc6, 0xd2, 0x79, 0x20, 0x9a, 0xdb, 0xc0, 0xfe,
0x78, 0xcd, 0x5a, 0xf4],
[0x1f, 0xdd, 0xa8, 0x33, 0x88, 0x07, 0xc7, 0x31, 0xb1, 0x12, 0x10,
0x59, 0x27, 0x80, 0xec, 0x5f],
[0x60, 0x51, 0x7f, 0xa9, 0x19, 0xb5, 0x4a, 0x0d, 0x2d, 0xe5, 0x7a, 0x9f,
0x93, 0xc9, 0x9c, 0xef],
[0xa0, 0xe0, 0x3b, 0x4d, 0xae, 0x2a, 0xf5, 0xb0, 0xc8, 0xeb, 0xbb, 0x3c,
0x83, 0x53, 0x99, 0x61],
[0x17, 0x2b, 0x04, 0x7e, 0xba, 0x77, 0xd6, 0x26, 0xe1, 0x69, 0x14,
0x63, 0x55, 0x21, 0x0c, 0x7d]
]

```

```

def mul02(x):
    s = x << 1
    s &= 0xff
    if (x & 128) != 0:
        s = s ^ 0x1b
    return s

```

```

def mul03(x):
    return mul02(x) ^ x

```

```

def MixColumns(block):
    block_n = [[] for k in range(4)]
    for i in range(4):
        col = [block[j][i] for j in range(4)]
        col = MixColumn(col)
        for i in range(4):
            block_n[i].append(col[i])
    return block_n

def MixColumn(column):
    r = [
        mul02(column[0]) ^ mul03(column[1]) ^ column[2] ^ column[3],
        mul02(column[1]) ^ mul03(column[2]) ^ column[3] ^ column[0],
        mul02(column[2]) ^ mul03(column[3]) ^ column[0] ^ column[1],
        mul02(column[3]) ^ mul03(column[0]) ^ column[1] ^ column[2],
    ]
    return r

def SubBytes(state):
    for i in range(len(state)):
        for j in range(len(state[i])):
            x = state[i][j] >> 4
            y = state[i][j] & 15
            state[i][j] = Sbox[x][y]
    return state

def SubBytesInv(state):
    for i in range(len(state)):
        for j in range(len(state[i])):
            x = state[i][j] >> 4
            y = state[i][j] & 15
            state[i][j] = SboxInv[x][y]
    return state

def ShiftRows(state):
    cnt = 1
    for i in range(1, Nb):
        state[i] = state[i][cnt:] + state[i][:cnt]
        cnt += 1
    return state

def ShiftRowsInv(state):
    cnt = 1
    for i in range(1, Nb):
        state[i] = state[i][-cnt:] + state[i][: -cnt]
        cnt += 1
    return state

def KeyExpansion(key):
    key_arr = [ord(symbol) for symbol in key]
    if (len(key_arr) < 4 * Nk):
        for i in range(4 * Nk - len(key)):
            key_arr.append(0x01)
    key_expanded = [[] for i in range(4)]
    for r in range(4):
        for c in range(Nk):
            key_expanded[r].append(key_arr[r + 4 * c])
    for col in range(Nk, Nb * (Nr + 1)):
        if (col % Nk == 0):
            tmp = [key_expanded[row][col - 1] for row in range(1, 4)]
            tmp.append(key_expanded[0][col - 1])

```

```

        for j in range(len(tmp)):
            sb_x = tmp[j] >> 4
            sb_y = tmp[j] & 15
            tmp[j] = Sbox[sb_x][sb_y]
        for row in range(4):
            s = (key_expanded[row][col - 4]) ^ (tmp[row]) ^
(Rcon[row][int(col/Nk - 1)])
            key_expanded[row].append(s)
    else:
        for row in range(4):
            s = key_expanded[row][col - 4] ^ key_expanded[row][col - 1]
            key_expanded[row].append(s)
    return key_expanded

def AddRoundKey(state, key_expanded, rnd = 0):
    for col in range(Nk):
        s0 = state[0][col] ^ key_expanded[0][Nb * rnd + col]
        s1 = state[1][col] ^ key_expanded[1][Nb * rnd + col]
        s2 = state[2][col] ^ key_expanded[2][Nb * rnd + col]
        s3 = state[3][col] ^ key_expanded[3][Nb * rnd + col]
        state[0][col] = s0
        state[1][col] = s1
        state[2][col] = s2
        state[3][col] = s3
    return state

def SplitBlocks(data):
    res = []
    for i in range(len(data) // 16):
        b = data[i * 16: i * 16 + 16]
        matrix = [[] for l in range(4)]
        for i in range(4):
            for j in range(4):
                matrix[i].append(b[i + j * 4])
        res.append(matrix)
    return res

def AESEncrypt(plain, key):
    plain = plain + (16 - len(plain) % 16) * chr(16 - len(plain) % 16)
    plain = [ord(sym) for sym in plain]
    states = SplitBlocks(plain)
    key_expanded = KeyExpansion(key)
    temp_states = []
    checker = False
    for state in states:
        temp_states.append(AddRoundKey(state, key_expanded))
    states = temp_states
    for rnd in range(1, Nr):
        temp_states = []
        for state in states:
            state = SubBytes(state)
            if (checker == False): print('SubByteStep_State: ', state)
            state = ShiftRows(state)
            if (checker == False): print('ShiftRowsStep_State: ', state)
            state = MixColumns(state)
            if (checker == False): print('MixColumnsStep_State: ', state)
            state = AddRoundKey(state, key_expanded, rnd)
            if (checker == False): print('AddRoundKeyStep_State: ', state)
            temp_states.append(state)
        checker = True
        states = temp_states

```

```

temp_states = []
res = []
for state in states:
    state = SubBytes(state)
    state = ShiftRows(state)
    state = AddRoundKey(state, key_expanded, rnd + 1)
    temp_states.append(state)
states = temp_states
for state in states:
    for col in range(4):
        for row in range(4):
            res.append(state[row][col])
return res

def AESDecrypt(cipher, key):
    states = SplitBlocks(cipher)
    key_expanded = KeyExpansion(key)
    temp_states = []
    for state in states:
        state = AddRoundKey(state, key_expanded, Nr)
        state = ShiftRowsInv(state)
        state = SubBytesInv(state)
        temp_states.append(state)
    states = temp_states
    rnd = Nr - 1
    while (rnd >= 1):
        temp_states = []
        for state in states:
            state = AddRoundKey(state, key_expanded, rnd)
            for k in range(3):
                state = MixColumns(state)
                state = ShiftRowsInv(state)
                state = SubBytesInv(state)
                temp_states.append(state)
        states = temp_states.copy()
        rnd = rnd - 1
    temp_states = []
    for state in states:
        temp_states.append(AddRoundKey(state, key_expanded, rnd))
    states = temp_states
    res = []
    for state in states:
        for col in range(4):
            for row in range(4):
                res.append(state[row][col])
    return res

plaintext = 'therulerooflondorheythisisshrinehandmaid'
key = 'firelinkfirekeep'
keytmp = key
print('[*] AES128 (ECB MODE)')
print('[*] Plaintext: ', plaintext)
print('[*] Key: ', keytmp)

encrypted = AESEncrypt(plaintext, keytmp)
encrypted_out = [chr(sym) for sym in encrypted]
#print('[+] Encrypted: ', encrypted_out)
encr = ''

for p in encrypted_out:

```



```
encr += p

print('[+] B64(Encrypted): ', b64encode(encr.encode()).decode('utf-8'))
decrypted = AESDecrypt(encrypted, key)
decrypted_out = [chr(sym) for sym in decrypted]
decr = ''

for p in decrypted_out:
    decr += p

decr = decr[::-ord(decr[len(decr)-1:])]
print('[+] Decrypted: ', decr)

print('[*] Task: ')
taskplain = unhexlify('C877C34FFBEE137354CDCEA531E5F0EE')
taskplain = taskplain + (16 - len(taskplain) % 16) * chr(16 - len(taskplain)
% 16).encode()
taskplain = [sym+0 for sym in taskplain]
states = SplitBlocks(taskplain)
state = states[0]
print('Default state: ', state)
state = SubBytes(state)
print('SubByteStep_State: ', state)
state = ShiftRows(state)
print('ShiftRowsStep_State: ', state)
state = MixColumns(state)
print('MixColumnsStep_State: ', state)
print('Result: ',end='')
for pack in state:
    for sym in pack:
        print(hex(sym), end=' ')
```