

11-

①

P_1, P_2, P_3, P_4 each 15 tons of product.

C_1, C_2, C_3 30, 16, 14 tons respectively

Minimize the transportation cost.

	C_1	C_2	C_3
P_1	100	100	50
P_2	650	110	100
P_3	60	65	75
P_4	150	90	70

Transportation cost for manufactured tonne is 0.5/km

\Rightarrow

	C_1	C_2	C_3
P_1	50	50	25
P_2	325	55	50
P_3	30	32.5	37.5
P_4	75	45	35

Distance table

	C_1	C_2	C_3	Supply
P_1	50	50	25	15
P_2	325	55	50	15
P_3	30	32.5	37.5	15
P_4	75	45	35	15
Demand	30	16	14	

BALANCED

Optimizar dada la solución

1^a poner ϵ si solución degenerada (no cumple $m+n-1$).

	U_i		
	$\frac{1}{18}$	$\frac{1}{18}$	$\frac{1}{17}$
5		$\frac{21}{15}$	$\frac{1}{4}$
3		$\frac{1}{6}$	
ϵ		2	
10		$\frac{1}{6}$	
V_j	17	8	17

Como los indicadores (triángulos) son no negativos, la solución es óptima.

$$\begin{cases}
 8 - U_1 - V_2 = 0 \\
 17 - U_1 - V_3 = 0 \\
 3 - U_2 - V_1 = 0 \\
 0 - U_3 - V_1 = 0 \\
 0 - U_3 - V_3 = 0
 \end{cases}$$

$$\begin{aligned}
 U_1 &= 0 \\
 V_2 &= 8 \\
 V_3 &= 17 \\
 U_2 &= -14 \\
 V_1 &= 17 \\
 U_3 &= -17
 \end{aligned}$$

13-

	B_1	B_2	B_3	B_4	Supply
P_1	60	40	45	55	130
P_2	70	55	65	60	200
P_3	80	60	85	75	170
	150	175	125	50	Balance

$P_1, P_2, P_3 \rightarrow 130, 200, 170$

$B_1, B_2, B_3, B_4 \rightarrow$
150, 175, 125, 50

Optimize solution

④

	15	6	4			U_i
	$\begin{matrix} 3 \\ \boxed{3} \end{matrix}$	$\begin{matrix} 4 \\ \boxed{4} \end{matrix}$	$\begin{matrix} 5 \\ \boxed{5} \end{matrix}$	$\begin{matrix} -20 \\ \boxed{2} \end{matrix}$	$\begin{matrix} -2 \\ \boxed{0} \end{matrix}$	0
	$\begin{matrix} -17 \\ \boxed{6} \end{matrix}$	$\begin{matrix} -11 \\ \boxed{3} \end{matrix}$	$\begin{matrix} 12 \\ \boxed{2} \end{matrix}$	$\begin{matrix} -23 \\ \boxed{2} \end{matrix}$	$\begin{matrix} -10 \\ \boxed{0} \end{matrix}$	8
	$\begin{matrix} -10 \\ \boxed{4} \end{matrix}$	5	21	1		
V_j	15	6	4	22	2	-1

$$\begin{aligned}
 15 - U_1 - V_1 &= 0 & \begin{cases} U_1 = 0 \\ V_1 = 15 \end{cases} \\
 6 - U_1 - V_2 &= 0 & \begin{cases} U_1 = 0 \\ V_2 = 6 \end{cases} \\
 4 - U_1 - V_3 &= 0 & \begin{cases} U_1 = 0 \\ V_3 = 4 \end{cases} \\
 12 - U_2 - V_3 &= 0 & \begin{cases} V_3 = 4 \\ U_2 = 8 \end{cases} \\
 5 - U_3 - V_2 &= 0 & \begin{cases} V_2 = 6 \\ U_3 = -1 \end{cases} \\
 21 - U_3 - V_4 &= 0 & \begin{cases} U_3 = -1 \\ V_4 = 22 \end{cases} \\
 1 - U_3 - V_5 &= 0 & \begin{cases} U_3 = -1 \\ V_5 = 2 \end{cases}
 \end{aligned}$$

$$6-1 \quad 4-\beta \rightarrow \beta=4$$

$$5-\beta \quad \beta$$

$$10 \quad 0$$

$$1 \quad 4$$

	15	10	0			U_i
	$\begin{matrix} 3 \\ \boxed{3} \end{matrix}$	$\begin{matrix} 4 \\ \boxed{4} \end{matrix}$	$\begin{matrix} 5 \\ \boxed{5} \end{matrix}$	$\begin{matrix} -28 \\ \boxed{2} \end{matrix}$	$\begin{matrix} -16 \\ \boxed{0} \end{matrix}$	9
	$\begin{matrix} -8 \\ \boxed{6} \end{matrix}$	$\begin{matrix} -6 \\ \boxed{3} \end{matrix}$	$\begin{matrix} 12 \\ \boxed{2} \end{matrix}$	$\begin{matrix} -22 \\ \boxed{2} \end{matrix}$	$\begin{matrix} -9 \\ \boxed{0} \end{matrix}$	8
	$\begin{matrix} -2 \\ \boxed{4} \end{matrix}$	1	4	21	1	
V_j	6	1	4	21	1	0

optimal solution

$$\begin{aligned}
 x_{11} &= 15 & x_{23} &= 12 & x_{35} &= 1 \\
 x_{12} &= 6 & x_{32} &= 1 & & \\
 x_{13} &= 0 & x_{33} &= 4 & &
 \end{aligned}$$

$$\begin{aligned}
 15 - U_1 - V_1 &= 0 & \begin{cases} U_1 = 9 \\ V_1 = 6 \end{cases} \\
 10 - U_1 - V_2 &= 0 & \begin{cases} V_2 = 1 \\ U_1 = 9 \end{cases} \\
 12 - U_2 - V_3 &= 0 & \begin{cases} V_3 = 4 \\ U_2 = 8 \end{cases} \\
 1 - U_3 - V_2 &= 0 & \begin{cases} U_3 = 0 \\ V_2 = 1 \end{cases} \\
 4 - U_3 - V_3 &= 0 & \begin{cases} U_3 = 0 \\ V_3 = 4 \end{cases} \\
 21 - U_3 - V_4 &= 0 & \begin{cases} U_3 = 0 \\ V_4 = 21 \end{cases} \\
 1 - U_3 - V_5 &= 0 & \begin{cases} U_3 = 0 \\ V_5 = 1 \end{cases}
 \end{aligned}$$

1.51.

(5)

	H ₁	H ₂	H ₃	H ₄	Supply
I ₁		9	11	8	400
I ₂		7	12	10	200
I ₃		11	10	16	620
Demand	300	340	400	440	

Not balanced

	H ₁	H ₂	H ₃	H ₄	Supply
I ₁		9		400	400
I ₂	200		11	8	400
I ₃	100	340	12	16	200
I ₄		10	12	16	620
Dm	0	0	0	0	260

1	1	1	-	-
3	(3)	-	-	-
1	1	1	1	1
0	-	-	-	-

9	10	(11)	8
2	1	1	2
2	1	1	(8)
11	10	12	(16)
12	10	(12)	-