

Week 6 Exercise:

- Considering the same example you solved in the previous assignment (radiative heat transfer between two parallel plates), how many shields with $\epsilon = 0.1$ should you add in order to have the new heat transfer rate to be 1% of the case without shields?

If the values are not equal

$Q_{\text{from previous example}} = 3625.4$

$1\% \text{ of } \dot{Q} = 36.254$

$\epsilon = 0.1$

$36.253 = (\sigma(T_1^4 - T_2^4)) / ((1/\epsilon_1 + 1/\epsilon_2 - 1))$

$\dot{Q} \text{ (N shields)} = A\sigma(T_1^4 - T_2^4) / (N+1)(1/\epsilon + 1/\epsilon - 1) = 1/(N+1) \dot{Q} \text{ (no shields)}$

$1\% \text{ of previous case } \dot{Q} = 1/100 \times 3625.3 \text{ W/m}^2 = 36.253 \text{ W/m}^2$

$36.253 \text{ W/m}^2 = (5.67 \times 10^{-8}) \times (800^4 - 500^4) / ((N+1)(1/0.1 + 1/0.1 - 1))$

$36.253 \text{ W/m}^2 = 19680.57 / ((N+1)(19))$

$N+1 = 28.57$

$N = 27.57 \sim 28$

If the values are equal

$\epsilon_1 = \epsilon_2 = \epsilon_{3.1} = \epsilon_{3.2} = 0.1$

$T_1 = 800 \text{ K}$

$T_2 = 500 \text{ K}$

$(\dot{Q})/A = \sigma(T_1^4 - T_2^4) / ((1/\epsilon + 1/\epsilon - 1)) \quad (\dot{Q})/A = (5.67 \times 10^{-8}) \times (800^4 - 500^4) / ((1/0.1 + 1/0.1 - 1)) = 1035.81 \text{ W/m}^2$

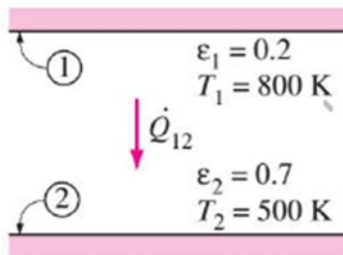
$1035.81 \times 1\% = 10.35$

$\left[(\sigma(T_1^4 - T_2^4) / (N+1)(1/\epsilon + 1/\epsilon - 1)) = 1/(N+1) \right]$

$$\left[\left(\frac{1}{(N+1)} \right) Q = \frac{1}{(100)} Q \right]$$

99 SURFACES TO LOWER THE RADIATION 1 %

-Find the radiative heat exchange between two parallel plates considering the two emissivities to be 0.1. What can you conclude from the result?



if $\epsilon_1 = 0.2$; $\epsilon_2 = 0.7$

$$R_{\text{Total}} = \frac{1}{0.2} + \frac{1}{0.7} - 1 = 5.43$$

$$\dot{Q}_{12} = A\sigma (T_1^4 - T_2^4) / \left(\frac{1}{\epsilon_1} + \frac{1}{\epsilon_2} - 1 \right) = (A * (5.67 * 10^{-8}) * (800^4 - 500^4)) / (1/0.2 + 1/0.7 - 1) = 3625.4 * A \text{ W}$$

if $\epsilon_1 = \epsilon_2 = 0.1$;

$$R_{\text{Total}} = \frac{1}{0.1} + \frac{1}{0.1} - 1 = 19$$

$$\dot{Q}_{12} = (A * (5.67 * 10^{-8}) * (800^4 - 500^4)) / (1/0.1 + 1/0.1 - 1) = 1035.8 * A \text{ W}$$