

Digital Assignment 1

ADITYA BAJPAI
(19BEE0330)

- ① Find the product of 9×14 by multiple algorithm.

$A = 9 \rightarrow 1001$ (Multiplicand)
 $B = 14 \rightarrow 1110$ (Multiplier)

$$\begin{array}{r}
 1001 \\
 \times 1110 \\
 \hline
 0000 \\
 1001 \\
 1001 \\
 + 1001 \\
 \hline
 111110
 \end{array}$$

	E	A	Q	Sc
	0	0000	1110	100 (4)
$B_n = 0$ Shr EAQ	0	0000	0111	011 (3)
$B_n = 1$ Add A+B		+ 1001		
	0	1001	0111	
Shr EAQ	0	0100	1011	010 (2)
$Q_n = 1$ Add A+B		+ 1001		
Shr	0	1101	1011	
Shr EAQ	0	0110	1101	001 (1)
$Q_n = 1$ Add A+B		+ 1001		
	0	1111	1101	
Shr EAQ	0	0111	1110	000 (0)

② Booth Algorithm $A = 11$ $B = -13$

$$A = 11 \rightarrow 01011$$

$$B = -13 \rightarrow 01101 \rightarrow \begin{array}{r} 10010 \\ +1 \\ \hline 10011 \end{array}$$

$$\text{Multiplier} = M = 01011$$

$$-M = 10100 + 1 = 10101$$

$$\text{Multiplier} = Q = 10011$$

	A	Q	Q-1	SC
	00000	10011	0	5
10 $\rightarrow A - M$	$+10101$			
	10101	10011		
Shr A & Q-1	11010	11001	1	4
11 \rightarrow Shr A & Q-1	11101	01100	1	3
01 $\rightarrow A + M$	$+01011$			
	01000	01100	1	
Shr A & Q-1	00100	00110	0	2
00 \rightarrow Shr A & Q-1	00010	00011	0	1
10 $\rightarrow A - M$	$+10101$			
	10111	00011	0	
Shr A & Q-1	<u>11011</u>	<u>10001</u>	1	0

$$(1101110001)_2$$

2's complement $\rightarrow (1101110001)_2$

1's complement $\rightarrow (1101110000)_2$

$\rightarrow (0010001111)_2$

$$= 2^7 + 2^3 + 2^2 + 2^1 + 2^0$$

$$= -143$$

$$11 \times (-13) = -143$$

③ Division Algorithm

dividend = 17, divisor = 04

$$(17)_{10} = (10001)_2 \quad M = 00100$$

$$(4)_{10} = (00100)_2 \quad \bar{M} + 1 = 11100$$

n	M	A(rem)	Q (quo)
5	00100	00000	10001
	00100	00001	0001-
	00100	11101	0001-
	00100	11101	00010
4	00100	00001	00010
	00100	00010	0010-
	00100	11110	0010-
	00100	11110	00100
3	00100	00010	00100
	00100	00100	0100-
	00100	00000	0100-
2	00100	00000	01001
	00100	00000	1001-
	00100	11100	1001-
	00100	11100	10010
1	00100	00000	10010
	00100	00001	0010-
	00100	11101	0010-
0	00100	11101	00100
	00100	00001	00100

4. $a = 0.75$ $b = -0.355$

Addition Subtraction floating point numbers
 $0.75 + (-0.355)$ Addition

Convert to Binary

$$0.75 \times 2 = 1.5 (1) \quad 0.355 \times 2 = 0.71 (0)$$

$$0.5 \times 2 = 1.0 (1) \quad 0.71 \times 2 = 1.42 (1)$$

$$= 0.1100$$

$$0.42 \times 2 = 0.84 (0)$$

$$= 1.1 \times 2^{-1}$$

$$0.84 \times 2 = 1.68 (1)$$

$$= 1.100 \times 2^{-1}$$

$$= 0.0101$$

$$= 0.1010 \times 2^{-1}$$

$$A = 00001.1000$$

$$B = -0.0001010$$

$$\begin{array}{r} 11110101 \\ + \quad 1 \\ \hline 11110110 \end{array}$$

$$\begin{array}{r} 00011000 \\ + 11110110 \\ \hline 00011110 \end{array}$$

$$0000.1110 \times 2^{-1} = 0.01110$$

Subtraction

$$0.75 - (-0.355) = 0.75 + 0.355$$

$$0.75 = 0.1100 = 1.1 \times 2^{-1}$$

$$0.355 = 0.0101 = 0.101 \times 2^{-1} = 0.1010 \times 2^{-1}$$

$$\begin{array}{r} 000111000 \\ 00001010 \\ \hline = 1.0010 \end{array}$$

⑤ Floating point multiplication for
operands $(0.22 * 0.145)$

$$\begin{array}{l}
 \cancel{0.22 \times 2 = 0.44 = 0} \\
 0.22 \times 2 = 0.44 = 0 \quad 0.145 \times 2 = 0.29 = 0 \\
 0.44 \times 2 = 0.88 = 0 \quad 0.29 \times 2 = 0.58 = 0 \\
 0.88 \times 2 = 1.76 = 1 \quad 0.58 \times 2 = 1.16 = 1 \\
 0.76 \times 2 = 1.52 = 1 \quad 0.16 \times 2 = 0.32 = 0 \\
 0.52 \times 2 = 1.04 = 1 \quad 0.32 \times 2 = 0.64 = 0 \\
 0.04 \times 2 = 0.08 = 0 \quad 0.64 \times 2 = 1.28 = 1
 \end{array}$$

$$\begin{array}{l}
 (0.22)_{10} = (0.00110)_2 \quad | \quad (0.145)_{10} = (0.001001)_2 \\
 = 1.110 \times 2^{-3} \quad \quad \quad = 1.001 \times 2^{-3}
 \end{array}$$

$$\boxed{-3 - 3 = -6}$$

$$\begin{array}{r}
 1.110 \\
 \times 1.001 \\
 \hline
 1110 \\
 00000 \\
 000000 \\
 1110000 \\
 \hline
 1.11110 \times 2^{-6}
 \end{array}$$

$$\boxed{(0.0319)_{10} = (0.00000111111)_2}$$