

Problem 1

(3 marks)

We are given n numbers stored in a queue. And you are given two stacks S_1 and S_2 . You have to use the two stacks to sort the numbers. At the end all the numbers should be in S_1 with the largest number at the top of the stack and the smallest number at the bottom of the stack. You are **not** allowed to use the queue in any way except to dequeue the numbers. Write an algorithm for this **in words**. No pseudocode. **If you use any pseudocode or code you will get a 0.** Please compute and write out the time complexity of your algorithm.

Problem 2 In this problem we will implement integers base p for $p \geq 2$. We call the ADT $\text{IntBase}(p)$. The ground set for this ADT is \mathbb{Z} (the set of integers). Our implementation is based on two ADTs defined in the ADT note shared on the course page: $\text{Intmod}(p)$ and AList . Specifically we will use $\text{Intmod}(p)\text{list}$. The idea is this: We will store the number as a list of $\text{Intmod}(p)$ in "reverse" order. eg. Consider the base 10 number 39, its $\text{IntBase}(5)$ representation will be $\boxed{4} \mid \boxed{2} \mid \boxed{1}$ which is the reversal of 124 which is the base 5 representation of 39.

Assumptions: You can use the following operations from the ADT note without implementing them

- Int : all operations including those in Exer 1.
- $\text{Intmod}(p)$: all operations given in Sec 2.2.
- $\text{Intmod}(p)\text{-List}$: all list operations of Definition 5.

Problem 2.1 (2 marks) Extend the $\text{Intmod}(p)$ ADT by adding a function $\text{Intmod}(p)\text{-overflow}(x, y)$ where x and y are $\text{Intmod}(p)$. If we view x and y as integers and $x + y \geq p$ where $+$ is the usual summation on integers then this function returns 1 else it returns 0. Recall that $\text{Intmod}(p)$ is implemented as an Int . Write an implementation of this operation using only the methods mentioned above.

Problem 2.2 (2 marks) Now write $\text{IntBase}(p)\text{-Create}(a)$. This operation takes an Int a as argument and returns a list as defined above.

Problem 2.3 (3 marks) Finally we write $\text{IntBase}(p)\text{-Sum}(x, y)$ which takes two arguments x and y of type $\text{IntBase}(p)$ and returns an $\text{IntBase}(p)$ which is the sum of x and y in Base p .