

Problem 1: RSA with a low-entropy prime generator

Solution: Here, the main idea is that if the prime generator has a low-entropy, it is very likely that two of the sampled N will have a common factor. Since the gcd of two numbers can be calculated efficiently, we can easily factorize the number and thus break RSA.

```
1 def attack():
2     L=[] # A list for storing N
3     for i in range(200):
4         (N, e), ct = restart_system()
5         for i in L:
6             p=gcd(i,N)
7             if p!=1 and p!=N and p!=N:
8                 q=N//p
9                 phiN=(p-1)*(q-1)
10                d = inverse(e, phiN)
11                return dec(ct, N, d)
12        L.append(N)
13
```

Listing 1: RSA with a low-entropy prime generator

Problem 2: Another Attack on RSA Signatures

Solution:

Problem 3: Attack on RSA PKCS Padding: Bleichenbacher's attack

Solution: Here we implemented Bleichenbacher's attack as mentioned in [his paper](#). We also referred to [this](#) video for understanding the attack better.

```
1 def attack(cipher_text, N, e):
2     ct_bin = ''.join(format(byte, '08b') for byte in cipher_text)
3     k = len(cipher_text) # number of bytes in the cipher text
4     B = pow(2, 8*(k-2)) # bound
5     M = [(2*B, 3*B-1)] # set of intervals
6     i = 1 # number of successful s values found
7
8     # Implement ceil and floor functions as math.ceil and math.floor don't work for large
9     # numbers
10    s = ceil(N, (3 * B))
11    while True:
12        min_n = M[0][0]
13        max_n = M[0][1]
14        for r in M: # min_n, max_n based on previous step
15            if r[0] < min_n:
16                min_n = r[0]
17            if r[1] > max_n:
18                max_n = r[1]
19
20        if (i > 1 and len(M) == 1):
21            # Step 2.c from the paper
22            a, b = M[0]
23            r = floor(2*(b*s - 2*B), N)
24            counter = 1
25            while True:
26                s = ceil((2*B + r * N), b)
27                s_max = ceil((3*B + r * N), a)
```

```

27         found = False
28         while s <= s_max:
29             ct_mod = (pow(pow(s, e) * (bin_to_int(ct_bin)), 1, N))
30             if (rsa.check_padding(rsa.num_to_bytes(ct_mod))) :
31                 found = True
32                 break
33             s += 1
34         if found:
35             break
36         else:
37             if counter%1000 == 0: print(counter)
38             counter += 1
39             r += 1
40     else:
41         # Step 2.a,b from the paper
42         while True:
43             s += 1
44             ct_mod = (pow(pow(s, e) * (bin_to_int(ct_bin)), 1, N))
45             if (rsa.check_padding(rsa.num_to_bytes(ct_mod))) :
46                 break
47
48     # update the set M (Step 3 from the paper)
49     M_new = []
50
51     for m in M:
52         a, b = m
53         # Compute large values one time
54         r_min = (a*s - 3*B + 1) // N
55         r_max = (b*s - 2*B) // N
56
57         r = r_min
58         while r <= r_max:
59             a_new = max(a, ceil((2*B + r*N), s))
60             b_new = min(b, floor((3*B - 1 + r*N), s))
61             if a_new > b or b_new < a:
62                 r += 1
63                 continue
64
65             if a_new == b_new: # Answer found
66                 crackList = list(rsa.num_to_bytes(a_new))
67                 final_msg = []
68                 zeroFound = False
69                 for c in crackList[2:]:
70                     if(zeroFound):
71                         final_msg.append(c)
72                     if(c == 0 and not zeroFound): zeroFound = True
73                 return final_msg
74             M_new.append((a_new, b_new))
75             r += 1
76     M = M_new
77     i += 1
78

```

Listing 2: Bleichenbacher's attack