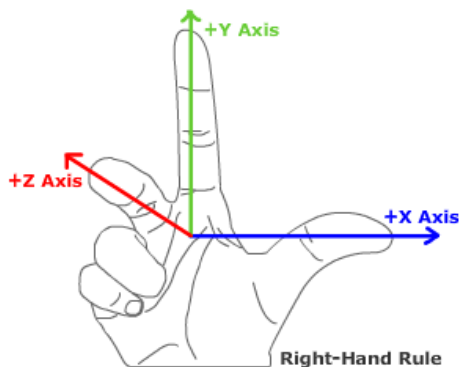


07. Kinematics, inverse kinematics, Programming of a simulated robotic arm

Repetition

3D transformations

- **Position:** 3 element offset vector



- **Orientation:** 3 x 3 rotation matrix
 - additional orientation representations: Euler angles, RPY, angle axis, quaternion
- **Pose** (pose): 4 x 4 transformation matrix
- **Coordinate system** (frame): zero point, 3 axis, 3 base vector, right-hand rule
- **Homogeneous transformations:** rotation and translation together
 - e.g. \mathbf{R} for rotation and \mathbf{v} for translation:

$$\mathbf{T} = \begin{bmatrix} \mathbf{R} & \mathbf{v} \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} r_{1,1} & r_{1,2} & r_{1,3} & v_x \\ r_{2,1} & r_{2,2} & r_{2,3} & v_y \\ r_{3,1} & r_{3,2} & r_{3,3} & v_z \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

- **Homogeneous coordinates:**

- **Vector:** add 0, $\mathbf{a}_H = \begin{bmatrix} \mathbf{a} \\ 0 \end{bmatrix} = \begin{bmatrix} a_x \\ a_y \\ a_z \\ 0 \end{bmatrix}$