



Probabilistic Graphical Models

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Feedback — Sampling Methods

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Winter 2011-2012

You achieved a score of **8.00** out of **8.00**

Question 1

Forward Sampling. One strategy for obtaining an estimate to the conditional distribution $P(\mathbf{y} | \mathbf{e})$ using forward sampling to estimate $P(\mathbf{y}, \mathbf{e})$ and $P(\mathbf{e})$ separately and then use the Hoeffding Bound to obtain a bound on both the numerator and the denominator. When does the resulting bound provide meaningful guarantees? True or False. Recall that we need $M \geq \frac{\ln(2/\delta)}{2\epsilon^2}$ between the true value and our estimate. Recall that we need $M \geq \frac{\ln(2/\delta)}{2\epsilon^2}$ ϵ that holds with probability $1 - \delta$ for our estimate.

Your Answer	Score	Explanation
<input checked="" type="radio"/> It provides a meaningful guarantee, but only when ϵ is small relative to $P(\mathbf{e})$ and $P(\mathbf{y}, \mathbf{e})$	1.00	True. When ϵ isn't small with the value of the estimated ratio from the true value of $P(\mathbf{y} \mathbf{e})$ ϵ and hence the absolute error $P(\mathbf{y}, \mathbf{e})$ is small.
Total	1.00	

Question 2

Rejecting Samples. Consider the process of rejection sampling to generate samples from the target distribution $P(X | \mathbf{e})$. If we want to obtain M samples, what is the expected number of samples that would need to be drawn from $P(X)$?

Your Answer	Score	Explanation
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 $M/P(e)$ 

1.00

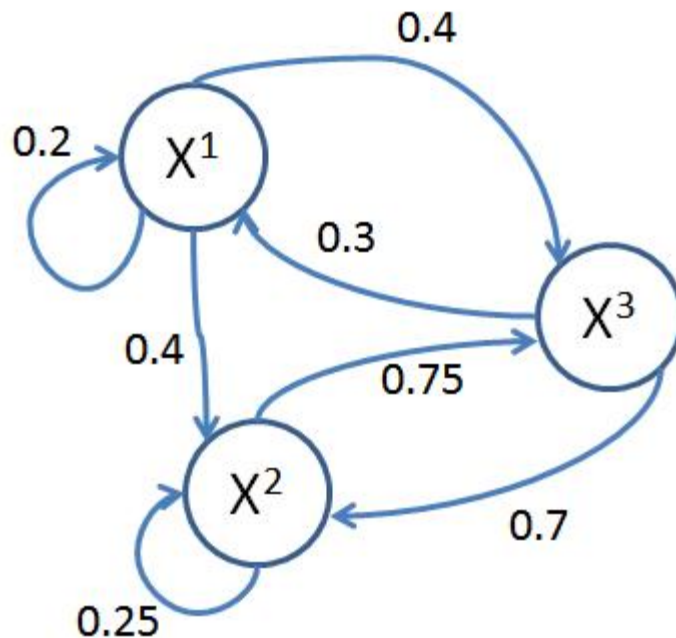
This is correct because it accounts for the samples that don't agree with the evidence and end up with the total number of samples. Then probability $P(e)$. Therefore, $M = P(e) * A$.

Total

1.00

Question 3

Stationary Distributions. Consider the simple Markov chain shown in the figure. The stationary distribution π for this chain must satisfy which of the following? (Select all that apply.)



Your Answer

- ☐ $\pi(x_3) = 0.4\pi(x_1) + 0.5\pi(x_2)$
- ☒ $\pi(x_1) + \pi(x_2) + \pi(x_3) = 1$
- ☐ $\pi(x_1) = 0.2\pi(x_1) + 0.4\pi(x_2) + 0.4\pi(x_3)$
- ☐ $\pi(x_1) = \pi(x_2) = \pi(x_3)$
- ☐ $\pi(x_3) = 0.3\pi(x_1) + 0.7\pi(x_2)$

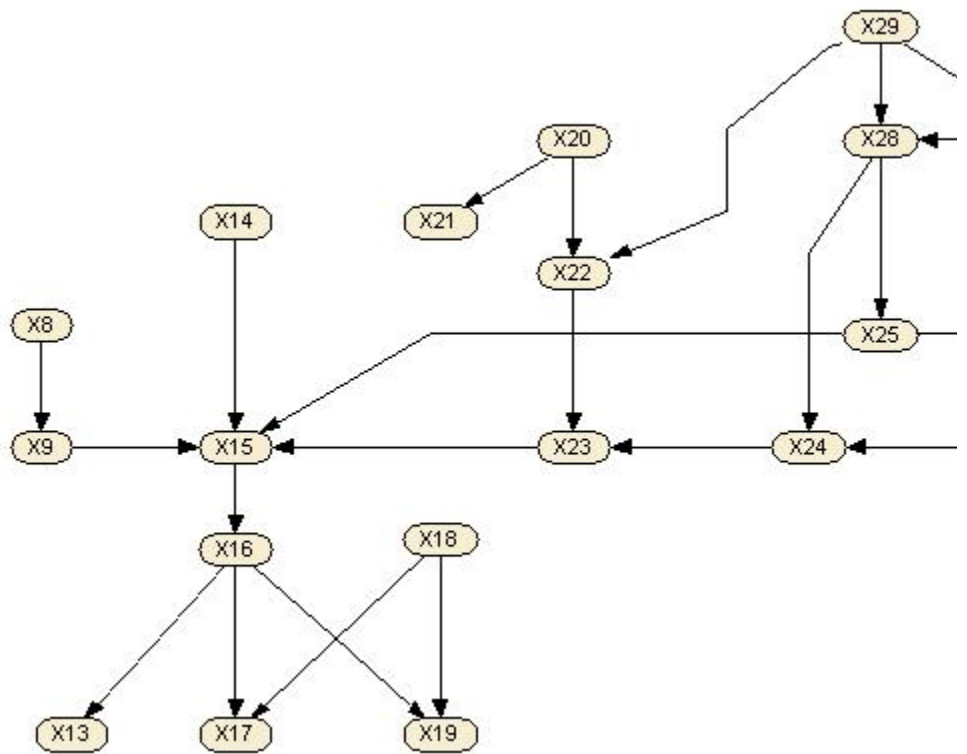
$$\pi(x_1) = 0.2\pi(x_1) + 0.3\pi(x_3)$$

Total



Question 4

***Gibbs Sampling in a Bayesian Network.** Suppose we have the Bayes below. If we are sampling the variable X_{23} as a substep of Gibbs sampling equation for the distribution we should use over the value x_{23}' ? By close computation such as summations are tractable and that we have access extra computation.



Your Answer

Score

•

$$\frac{P(x_{23}' | x_{22}, x_{24}) P(x_{15} | x_{23}', x_{14}, x_9, x_{25})}{\sum_{x_{23}} P(x_{23}'' | x_{22}, x_{24}) P(x_{15} | x_{23}'', x_{14}, x_9, x_{25})}$$



1.00

Total


1.00

$P(x_{23}' | x_{-23})$ is correct but not in closed form because we don't have get it, we have to expand it, and since all factors involving variables not

out (see equation 12.23 in Chapter 12.3.3), we get the correct answer. (


Question 5

Gibbs Sampling. Suppose we are running the Gibbs sampling algorithm on a Markov chain $X \rightarrow Y \rightarrow Z$. If the current sample is $\langle x_0, y_0, z_0 \rangle$ and we sample y as part of the Gibbs sampling process, with what probability will the next sample be $\langle x_0, y_1, z_0 \rangle$?

Your Answer	Score	Explanation
<input checked="" type="radio"/> $P(y_1 \mid x_0, z_0)$	 1.00	For Gibbs Sampling, we select one variable at a time to sample, given the current values of all other variables.
Total	1.00	

Question 6

Collecting Samples. Assume we have a Markov chain that we have run for a long time and now wish to collect samples and use them to estimate the probability that a coin is heads. Should we use every sample from the Markov chain after the burn-in?

Your Answer	Score	Explanation
<input checked="" type="radio"/> Yes, that would give a correct estimate of the probability. However, we cannot apply the Hoeffding bound to estimate the error in our estimate.	 1.00	This is correct because the collected samples are stationary (posterior) and the Hoeffding bound cannot be applied to non-stationary samples from the Markov chain.
Total	1.00	


Question 7

Markov Chain Mixing. Which of the following classes of chains would you expect to have the fastest mixing time in general?

Your Answer		Score	Expla
<input checked="" type="radio"/> Markov chains where state spaces are well connected and transitions between states have high probabilities.		1.00	This is able to you a
Total		1.00	

Question 8

Metropolis-Hastings Algorithm. Assume we have an $n \times n$ grid-structured $X_{i,j}$. Let $\mathbf{X}_i = \{X_{i,1}, \dots, X_{i,n}\}$ and $\mathbf{X}_{-i} = \mathcal{X} - \mathbf{X}_i$. Consider the Metropolis-Hastings algorithm: at each step, we take our current assignment inference to compute the conditional probability $P(\mathbf{X}_i \mid \mathbf{x}_{-i})$. We then sample from this distribution, and use that as our proposal. What is the correct acceptance probability?

Your Answer		Score	Explanation
<input checked="" type="radio"/> 1		1.00	This is (block) Gibbs sampling, where we sample simultaneously from their conditional distributions. Gibbs sampling is an instance of MH that has acceptance probability 1.
Total		1.00	