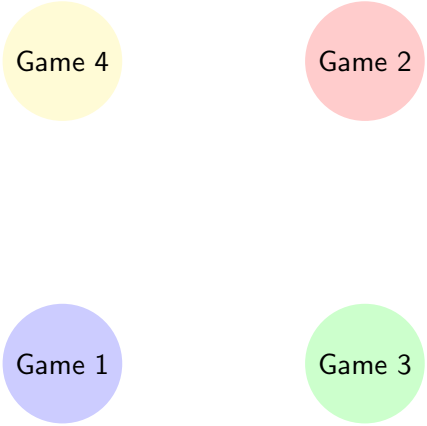


Stochastic Games

Game Theory

Vincent Knight

- ▶ X a set of states with a stage game defined for each state;
- ▶ A set of strategies $S_i(x)$ for each player for each state $x \in X$;
- ▶ A set of rewards dependant on the state and the actions of the other players: $u_i(x, s_1, s_2)$;
- ▶ A set of probabilities of transitioning to a future state:
 $\pi(x'|x, s_1, s_2)$;
- ▶ Each stage game is played at a set of discrete times t .

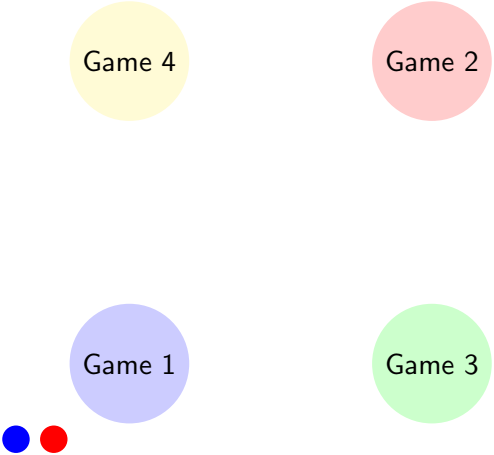


Game 4

Game 2

Game 1

Game 3



Game 4

Game 2

Game 1

Game 3

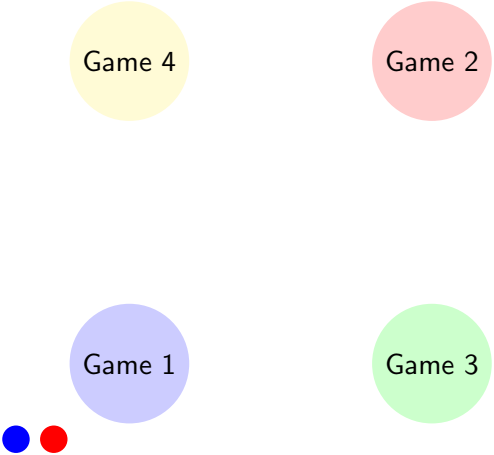
Game 4

Game 2

Game 1

Game 3



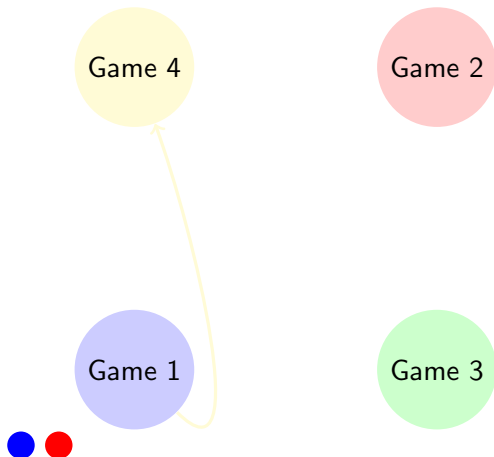


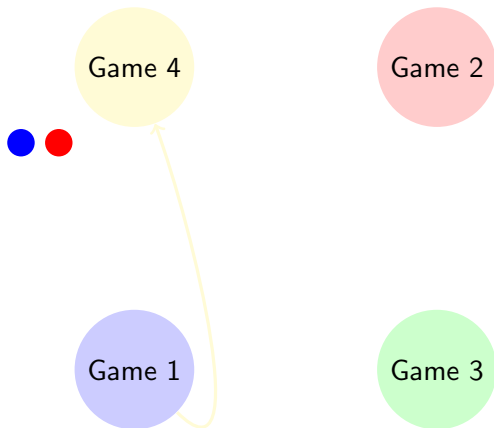
Game 4

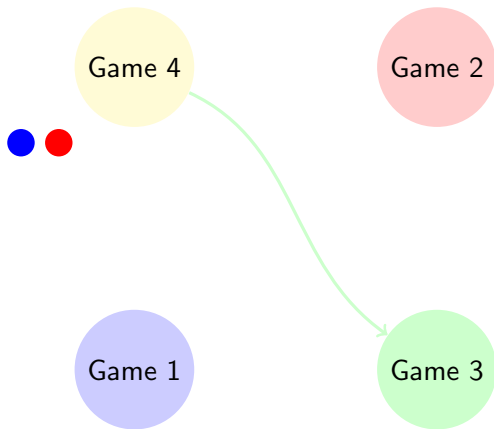
Game 2

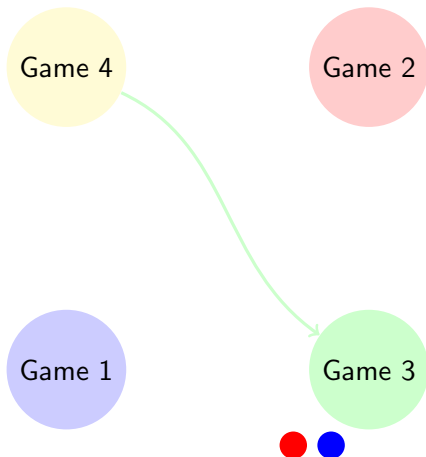
Game 1

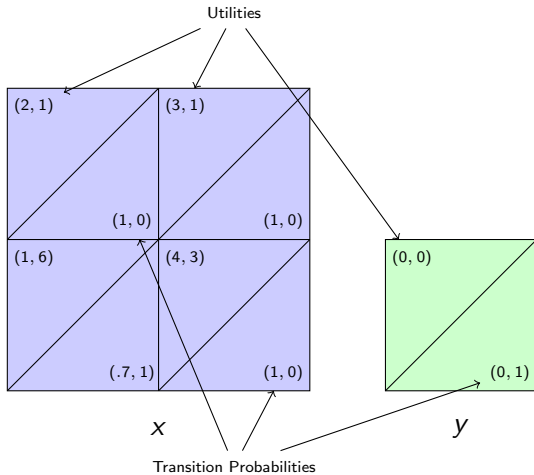
Game 3











$$U_i(r,s) = \left(u_i(x,r,s) + \delta \sum_{x' \in X} \pi(x'|x,r,s) U_i^*(x') \right)$$

$$U_i(r, s) = \left(u_i(x, r, s) + \delta \sum_{x' \in X} \pi(x'|x, r, s) U_i^*(x') \right)$$

Thus a Nash equilibrium satisfies:

$$U_1^*(x) = \max_{r \in S_1(x)} (u_i(x, r, s^*) + \delta \sum_{x' \in X} \pi(x'|x, r, s^*) U_1^*(x'))$$

$$U_2^*(x) = \max_{s \in S_2(x)} (u_i(x, r^*, s) + \delta \sum_{x' \in X} \pi(x'|x, r^*, s) U_1^*(x'))$$