# Homework sheet 2 - Nash equilibrium in normal form games

1. Compute the Nash equilibrium (if they exist) in pure strategies for the following games:
2. For what values of does a Nash equilibrium exist in pure strategies for the following game:
3. Consider the following game:

* Suppose two vendors (of an identical product) must choose their location along a busy street. It is anticipated that their profit is directly related to their position on the street.
* If we allow their positions to be represented by a points on the line segment then we have:

and

By considering best responses of each player, identify the Nash equilibrium for the game.

1. Consider the following game:

Plot the expected utilities for each player against mixed strategies and use this to obtain the Nash Equilibria.

1. Assume a soccer player (player 1) is taking a penalty kick and has the option of shooting left or right: . A goalie (player 2) can either dive left or right: . The chances of a goal being scored are given below:
2. Assume the utility to player 1 if the probability of scoring and the utility to player 2 the probability of a goal not being scored. What is the Nash equilibrium for this game?
3. Assume that player 1 now has a further strategy available: to shoot in the middle: the probabilities of a goal being scored are now given:

Obtain the new Nash equilibrium for the game.

1. In the notes the following theorem is given:

Every normal form game with a ﬁnite number of pure strategies for each player, has at least one Nash equilibrium.

Prove the theorem for 2 player games with . I.e. prove the above result in the special case of games.