# Rebuttal to "Comments on 'Control Cloud Data Access Privilege and Anonymity With Fully Anonymous Attribute-Based Encryption"

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Abstract—Ma et al. recently submitted a comment correspondence which points out a flaw in our paper (a sequel of our earlier paper published in the *Proceedings of IEEE INFOCOM*). The flaw led to the leakage of the system-wide master key; therefore, we improved our own scheme by addressing it.

# I. SUMMARY OF THE UNCOVERED FLAW

Our key generation (Section V.B in [1] and IV.B in [2]) let all attribute authorities (*i.e.*, key generators) jointly and securely distribute  $D = g^{\sum v_k + \sum d_k}$  to all users where any individual  $v_k, d_k$  is kept secret to anyone else but the k-th authority  $\mathcal{A}_k$ .  $g^{\sum v_k}$  works as a system-wide master key which can be composed if and only if all authorities participate in the computation, and it is not supposed to be known to anyone (even the authorities).

However, when  $H(att(i))^{r_i}g^{\sum d_k}$  is delivered to the key requester, the authority in charge of the attribute i directly sent out  $H(att(i))^{r_i}$ , and all single  $x_kg^{d_k}$ 's where  $\prod x_k=1$ . This enabled all key requesters to calculate  $g^{\sum d_k}=\prod (x_kg^{d_k})$ , and this can recover  $g^{\sum v_k}$  from  $D=g^{\sum v_k+\sum d_k}$ , which allowed attackers to bypass our privilege control by directly using the calculated system-wide master key.<sup>1</sup>

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<sup>1</sup>The system-wise master key is not supposed to be known to any user or any authority in the system. This component will exist in valid private key if and only if all authorities jointly generated the private key. All authorities independently perform their key generation tasks, and our scheme does not need a central coordinator for the key generation.

Besides, since  $x_k$  is always reused, any valid key requester is able to infer all individual  $x_k g^{d_k}$  as well.

### II. ADDRESSING THE FLAW

It is easy to fix this flaw. All we need to do is to prevent authorities from sending all single  $x_k g^{d_k}$ 's to key requesters. In order to do so, we let each authority  $\mathcal{A}_k$  privately send  $H(att(i))^{r_i} \cdot x_k \cdot g^{d_k}$  as a whole to the key requester (*i.e.* kept secret to other authorities) if  $\mathcal{A}_k$  is in charge of any attribute of this requester, and he sends only  $x_k \cdot g^{d_k}$  if none of the attributes of this requester are under his control.

By doing so, at least one  $x_k \cdot g^{d_k}$  remains hidden to the key requesters because authorities do not generate keys for attributes not belonging to the user at all. Then, there must be one authority who sends out  $H(att(i))^{r_i} \cdot x_k \cdot g^{d_k}$  instead of  $x_k \cdot g^{d_k}$ , and key requesters are not able to derive  $g^{\sum d_k}$  or  $g^{\sum v_k}$ .

Also, in order to avoid leakage of individual  $x_k g^{dk}$ 's, we simply let all authorities share fresh  $x_k$ 's for every different attribute. This does not affect the asymptotic complexity of the key generation algorithm since the original complexity is  $O(N|\mathbb{A}|)$  where N is the number of authorities and  $|\mathbb{A}|$  is the number of attributes in the requested keys for each authority. The extra computation overhead is not noticeable either since it is merely  $(N-1)|\mathbb{A}|$  random numbers generation,  $2(N-1)|\mathbb{A}|$  multiplications and  $|\mathbb{A}|$  exponentiations. The extra communication overhead due to this fix is noticeable since the authority needs to send a large integer (128-256B) to N-1 authorities, and it also receives integers from N-1 authorities. This is comparable to the original overhead of the key generation algorithm which requires communication of multiple large integers. However, the increment is at most twice of the original communication overhead.

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#### REFERENCES

- T. Jung, X. Li, Z. Wan, and M. Wan, "Control cloud data access privilege and anonymity with fully anonymous attribute-based encryption," *IEEE Trans. Inf. Forensics Security*, vol. 10, no. 1, pp. 190–199, Jan. 2014.
- [2] T. Jung, X.-Y. Li, Z. Wan, and M. Wan, "Privacy preserving cloud data access with multi-authorities," in *Proc. IEEE INFOCOM*, Apr. 2013, pp. 2625–2633.