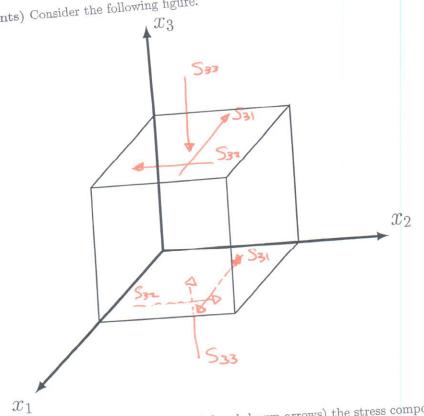
# Problem 1

(5 points) Consider the following figure:



On the figure, correctly indicate (with hand-drawn arrows) the stress components  $S_{33}$ ,  $S_{31}$ , and  $S_{32}$  on both sides of the cube where they act. Use a "compression positive" sign convention.

#### Problem 2

For the following matrix A,

$$\mathbf{A} = \begin{bmatrix} 1 & 2 \\ 5 & 4 \end{bmatrix}$$

perform the following calculations by hand:

- (i) (5 points) Compute the determinate of A.
- (ii) (5 points) Compute the eigenvalues of A.
- (iii) (5 points) Compute the eigenvectors of A, put them in unit-vector form.

(1) 
$$(1)(4) - (2)(5) = -6$$

$$\det\left(\begin{bmatrix}1-\lambda & 2\\ 5 & 4-\lambda\end{bmatrix}\right) \ge 0$$

$$(1-3)(4-3) - (2)(5) = 0$$
  
 $\lambda^2 - 53 - 6 = 0$ 

$$\begin{bmatrix} 1 - (-1) & 2 \\ 5 & 4 - (-1) \end{bmatrix}^{2} \begin{bmatrix} 2 & 2 \\ 5 & 5 \end{bmatrix} \longrightarrow \begin{bmatrix} 1 & 1 \\ 0 & 0 \end{bmatrix} \begin{cases} V_{1} + V_{2} = 0 \\ V_{2} = \text{free} \rightarrow 1 \end{cases}$$

$$V_1 + V_2 = 0$$

$$V_2 = \{cee \Rightarrow$$

$$\vec{3} = \begin{cases} -1 \\ \frac{1}{\sqrt{2}} \end{cases}$$

This page provided for additional calculations

For 
$$\lambda_2 = 6$$

$$\begin{bmatrix} 1 - (6) & 2 \\ 5 & 4 - (6) \end{bmatrix} = \begin{bmatrix} -5 & 2 \\ 5 & -2 \end{bmatrix} \rightarrow \begin{bmatrix} -5 & 2 \\ 0 & 0 \end{bmatrix}$$

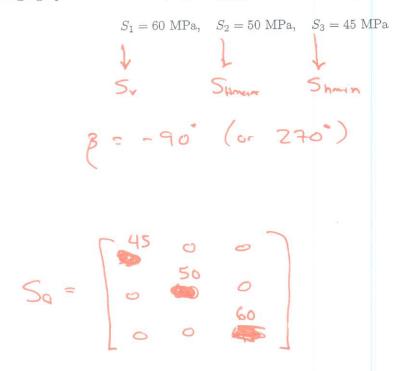
$$-5v_1 + 2v_2 = 0$$

$$v_2 = \begin{cases} ree \rightarrow 1 \\ v_1 = \end{cases}$$

$$v_1 = \begin{cases} 2 \\ 5 \end{cases}$$

### Problem 3

(20 points) Given the following principle stresses under normal faulting (using Anderson classification). What is the geographical stress tensor,  $S_G$ , if  $S_{Hmax}$  is oriented exactly east?



#### Name:

## Problem 4

Given the geographical stress,

$$\mathbf{S}_G = \begin{bmatrix} 47.5 & -12.5 & 0 \\ -12.5 & 47.5 & 0 \\ 0 & 0 & 40 \end{bmatrix} \text{ MPa}$$

- (i) (10 points) For a fault strike oriented east-west and a dip 60° from north, determine the normal and shear stresses acting on the fault plane.
- (ii) (5 points) If the fault where to slip, what type of fault slip would it be?
- (iii) (10 points) Faults typically slip when the ratio of shear to normal effective stress exceeds 0.6, i.e.  $\tau/\sigma_n^{eff} > 0.6$ . Using this criterion, calculate the critical injection pressure in petroleum engineering operations that one should not exceed to prevent fault slippage. You can assume that the fault is very near the injector and steady state conditions, such that the pore pressure is equal to the injection pressure.

(iii) 
$$\frac{\tau}{(t_n - P_p)} > 0.6 \Rightarrow \frac{\tau}{(t_n - P_p)} = M$$

$$P_{e} = \frac{\mu t_{n} - \tau}{\mu} = \frac{(0.6)(45.6) - 11.3}{0.6} = 26.8 \text{ m/s}$$

T = \( \tau\_{s}^2 + \tau\_{d}^2 = 11.3 \text{ m/g}