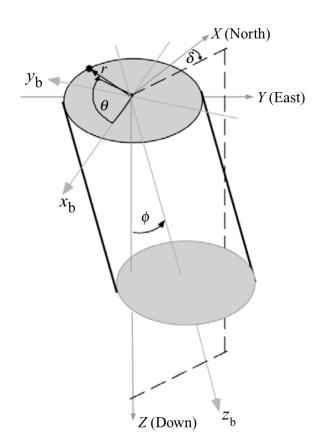
State of stress surrounding an arbitrarily deviated well





Stresses in the wellbore coordinate system

$$\mathbf{R}_{B} = \begin{bmatrix} \cos \delta \cos \phi & \sin \delta \cos \phi & -\sin \phi \\ -\sin \delta & \cos \delta & 0 \\ \cos \delta \sin \phi & \sin \delta \sin \phi & \cos \phi \end{bmatrix}$$

$$\mathbf{S}_B = \mathbf{R}_B \mathbf{S}_G \mathbf{R}_B^T$$

$$\mathbf{S}_B = \mathbf{R}_B(\mathbf{R}_G^T \mathbf{S} \mathbf{R}_G) \mathbf{R}_B^T$$



Stress at wellbore wall

$$\sigma_{zz} = \sigma_{33} - 2\nu(\sigma_{11} - \sigma_{22})\cos 2\theta - 4\nu\sigma_{12}\sin 2\theta$$

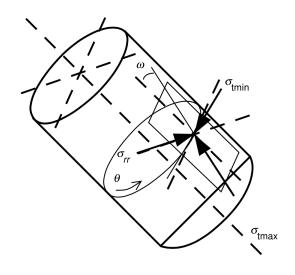
$$\sigma_{\theta\theta} = \sigma_{11} + \sigma_{22} - 2(\sigma_{11} - \sigma_{22})\cos 2\theta - 4\sigma_{12}\sin 2\theta - \Delta P$$

$$\tau_{\theta z} = 2(\sigma_{23}\cos \theta - \sigma_{13}\sin \theta)$$

$$\sigma_{rr} = \Delta P$$



Principal effective stresses around the wellbore



$$\sigma_{t \text{max}} = \frac{1}{2} \left(\sigma_{zz} + \sigma_{\theta\theta} + \sqrt{(\sigma_{zz} - \sigma_{\theta\theta})^2 + 4\tau_{\theta z}^2} \right)$$

$$\sigma_{t \text{min}} = \frac{1}{2} \left(\sigma_{zz} + \sigma_{\theta\theta} - \sqrt{(\sigma_{zz} - \sigma_{\theta\theta})^2 + 4\tau_{\theta z}^2} \right)$$

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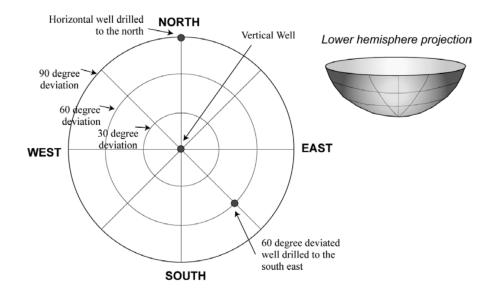
Example: Reverse faulting

$$\mathbf{S} = \begin{bmatrix} 30 & 0 & 0 \\ 0 & 25 & 0 \\ 0 & 0 & 20 \end{bmatrix} \qquad \begin{array}{l} \alpha = 90^{\circ} & \text{Azimuth of } S_{Hmax} \\ \beta = 0^{\circ} & S_{1} = S_{Hmax} \\ \gamma = 0^{\circ} & S_{2} = S_{hmin} \end{array}$$

Find the minimum and maximum tangential stress for an open hole well that is oriented 20° from North and deviated 20° from vertical at a depth of 2 km. Assume a hydrostatic pore pressure gradient and a Poisson ration of 0.2.



Lower hemisphere projection





Example

