

input : vectors with $L(t_i)$, t_i and $V_0(t_i)$, arranged by their appearance time t_i , N grid points x_k

output: $\tau_{num}(x_k)$ as a vector of size N

$\tau_n(x_k) \leftarrow$ array length N of empty dynamic arrays length n ;

$k \leftarrow 1$;

for $i \leftarrow 1$ **to** *length of* $t_i - 1$ **do**

if $L(t_{i+1}) \geq L(t_i)$ **then**

repeat

$\tau_{n+1}(x_k) \leftarrow$ output of interpolating $L(t), V_0(t)$ at t_i, t_{i+1} ;

$k \leftarrow k + 1$;

until $x_k > L(t_i)$;

end

if $L(t_{i+1}) < L(t_i)$ **then**

repeat

$\tau_{n+1}(x_k) \leftarrow$ output of interpolating $L(t), V_0(t)$ at t_i, t_{i+1} ;

$k := k - 1$;

until $x_k < L(t_i)$;

end

end

for $i \leftarrow 1$ **to** N **do**

$\tau_{num}(x_k) \leftarrow \tau_1(x_k)$;

for $j \leftarrow 2$ **to** *length of* $\tau_n(x_k)$ **do**

if j *even* **then**

$\tau_{num}(x_k) \leftarrow \tau_{num}(x_k) + \tau_j(x_k)$;

else

$\tau_{num}(x_k) \leftarrow \tau_{num}(x_k) - \tau_j(x_k)$;

end

end