```
# calculate after_position using the democratic combination of after_velocity and before_velocit
# The Oth elements of velocities, positions, and times are already filled in, so start with
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 after_position = before_position + delta_t * 0.5 * (after_velocity + before_velocity)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            # fundamental change for 2nd-order Runge-Kutta -- first estimate the mid_position!!
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            # calculate the acceleration -- using the estimated mid_position!
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  mid_position = before_position + 0.5 * delta_t * before_velocity
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  after_velocity = before_velocity + delta_t * mid_acceleration
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    mid_acceleration = acceleration_of_gravity(mid_position)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          # calculate after_velocity mid_acceleration
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         # assign the after values into their lists
                                         for i in range(1, simulation_time_steps):
                                                                                                                                                                                                                                                                     before_velocity = velocities[i - 1]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   after_time = before_time + delta_t
                                                                                                                                                                                                                                                                                                                                                             before_position = positions[i - 1]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            velocities[i] = after_velocity
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        positions[i] = after_position
                                                                                                                             # get all the before values
                                                                                                                                                                                                                                                                                                                                                                                                                                              before_time = times[i - 1]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         times[i] = after_time
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              # update time
                                                                                                                                                                                                                           # velocities
                                                                                                                                                                                                                                                                                                                   # positions
                                                                                                                                                                                                                                                                                                                                                                                                           # time
```