

# Linear congruential generator

We have designed and implemented a new prime factorization algorithm. It is believed that the most challenging inputs to the algorithm are integers which are the product of  $K$  distinct primes. We would like to test the algorithm on a sequence of integers generated by a linear congruential generator. The question is how to choose the generator seed so that many challenging inputs are generated.

## The task

You are given parameters of a linear congruential generator. Your task is to compute the seed of the generator which will produce a sequence of  $N$  pseudorandom values containing as many as possible integers whose prime factorization consists of exactly  $K$  distinct primes.

## Input

The input is one line containing integers  $A, C, M, K, N$  separated by a space. Values  $A, C, M$  determine linear congruential generator given by formula  $x_{i+1} = Ax_i + C \pmod{M}$ . It is guaranteed that the generator has a period of length  $M$ . Value  $N$  is the number of inputs we are supposed to generate from a chosen seed to test the algorithm. The generated values are thus  $x_1, x_2, \dots, x_N$  where  $x_1$  equals the seed. Values of  $A, C$  and  $M$  are not greater than  $3 \times 10^8$ . Moreover,  $1 \leq K \leq 10$  and  $1 \leq N \leq M$ .

## Output

The output is one line containing two integers  $S$  and  $I$  separated by a space.  $S$  is the optimal seed,  $I$  is the number of the most challenging inputs that will be generated from  $S$ . If more seeds generate the same number of the most challenging inputs,  $S$  is that seed among them which is generated by the generator from the initial value  $x_1=0$  earlier than the other seeds.

## Example 1

### Input

```
5 11 8 1 4
```

### Output

```
0 3
```

The generator produces numbers 0, 3, 2, 5, 4, 7, 6, 1. Since  $K=1$ , the most challenging inputs are primes. If seed 0 is chosen, primes 2, 3 and 5 are included in the generated sequence of length  $N=4$ . This is the optimal setting as a sequence of length 4 cannot include all 4 primes produced by the generator.

## Example 2

### Input

```
5 3 16 2 7
```

### Output

```
8 3
```

The produced numbers are sequentially 0, 3, 2, 13, 4, 7, 6, 1, 8, 11, 10, 5, 12, 15, 14, 9. Since  $K=2$ , the most challenging inputs are those numbers in  $0, \dots, 15$  that are products of two distinct primes (6, 10, 14, 15). The optimal seed is thus 8.

## Example 3

### Input

```
17 9 32 2 10
```

### Output

```
13 5
```

## Public data

The public data set is intended for easier debugging and approximate program correctness checking. The public data set is stored also in the upload system and each time a student submits a solution it is run on the public dataset and the program output to stdout and stderr is available to him/her.

[Link to public data set](#)