# **SBML Model Report**

# Model name: "Hoefnagel2002\_PyruvateBranches"



May 6, 2016

#### 1 General Overview

This is a document in SBML Level 2 Version 4 format. This model was created by the following two authors: Nicolas Le Novre<sup>1</sup> and Maria Schilstra<sup>2</sup> at March sixth 2005 at 8:03 p. m. and last time modified at April eighth 2016 at 2:25 p. m. Table 1 provides an overview of the quantities of all components of this model.

Table 1: Number of components in this model, which are described in the following sections.

Element	Quantity	Element	Quantity
compartment types	0	compartments	1
species types	0	species	19
events	0	constraints	0
reactions	14	function definitions	0
global parameters	0	unit definitions	2
rules	0	initial assignments	0

#### **Model Notes**

This a model from the article:

Metabolic engineering of lactic acid bacteria, the combined approach: kinetic modelling, metabolic control and experimental analysis.

<sup>&</sup>lt;sup>1</sup>EMBL-EBI, lenov@ebi.ac.uk

<sup>&</sup>lt;sup>2</sup>SBML Team - Science and Technology Research Institute - University of Hertfordshire, m.j.1.schilstra@ herts.ac.uk

Hoefnagel MH, Starrenburg MJ, Martens DE, Hugenholtz J, Kleerebezem M, Van Swam II, Bongers R, Westerhoff HV, Snoep JL Microbiology 2002 Apr; 148(4):1003-13 11932446, Abstract:

Everyone who has ever tried to radically change metabolic fluxes knows that it is often harder to determine which enzymes have to be modified than it is to actually implement these changes. In the more traditional genetic engineering approaches bottle-necks are pinpointed using qualitative, intuitive approaches, but the alleviation of suspected rate-limiting steps has not often been successful. Here the authors demonstrate that a model of pyruvate distribution in Lactococcus lactis based on enzyme kinetics in combination with metabolic control analysis clearly indicates the key control points in the flux to acetoin and diacetyl, important flavour compounds. The model presented here (available at http://jjj.biochem.sun.ac.za/wcfs.html) showed that the enzymes with the greatest effect on this flux resided outside the acetolactate synthase branch itself. Experiments confirmed the predictions of the model, i.e. knocking out lactate dehydrogenase and overexpressing NADH oxidase increased the flux through the acetolactate synthase branch from 0 to 75% of measured product formation rates.

The paper does not have any figure to be put as a curation figure in the BioModels database. The model does reproduce the fluxes and control-coefficients given in Figure 2 and Table 4. To reproduce the results, the model was changed from the description in the article according to the model on JWS: the parameter Kmpyr was changed to 2.5 from 25. The equillibrium constant for PTA reaction (R4) was changed from 0.0281 to 0.0065. The Km for oxygen in the NOX reaction (R13) was changed from 0.01 to 0.2. Slight deviations between the values in the article and the model results may stem from different algorithms used for finding the steady state.

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To cite BioModels Database, please use: Li C, Donizelli M, Rodriguez N, Dharuri H, Endler L, Chelliah V, Li L, He E, Henry A, Stefan MI, Snoep JL, Hucka M, Le Novre N, Laibe C (2010) BioModels Database: An enhanced, curated and annotated resource for published quantitative kinetic models. BMC Syst Biol., 4:92.

#### 2 Unit Definitions

This is an overview of five unit definitions of which three are predefined by SBML and not mentioned in the model.

#### 2.1 Unit substance

Name millimole (default)

**Definition** mmol

#### 2.2 Unit time

Name minute (default)

#### **Definition** 60 s

#### 2.3 Unit volume

**Notes** Litre is the predefined SBML unit for volume.

#### **Definition** 1

#### 2.4 Unit area

Notes Square metre is the predefined SBML unit for area since SBML Level 2 Version 1.

**Definition**  $m^2$ 

# 2.5 Unit length

**Notes** Metre is the predefined SBML unit for length since SBML Level 2 Version 1.

**Definition** m

# 3 Compartment

This model contains one compartment.

Table 2: Properties of all compartments.

Id	Name	SBO	Spatial Dimensions	Size	Unit	Constant	Outside
compartment			3	1	litre	Ø	

# 3.1 Compartment compartment

This is a three dimensional compartment with a constant size of one litre.

# 4 Species

This model contains 19 species. The boundary condition of eight of these species is set to true so that these species' amount cannot be changed by any reaction. Section 6 provides further details and the derived rates of change of each species.

Table 3: Properties of each species.

Id	Name	Compartment	Derived Unit	Constant	Boundary
					Condi-
					tion
ADP		compartment	mmol		
NAD		compartment	mmol		
ATP		compartment	mmol		
NADH		compartment	mmol		
pyruvate		compartment	mmol		
lactate		compartment	mmol		
CoA		compartment	mmol		
halfglucose		compartment	mmol		
AcCoA		compartment	mmol		
AcP		compartment	mmol		
Ac		compartment	mmol		
AcO		compartment	mmol		
EtOH		compartment	mmol		
AcLac		compartment	mmol		$\Box$
AcetoinIn		compartment	mmol		
AcetoinOut		compartment	mmol		
Butanediol		compartment	mmol		$\overline{\mathbf{Z}}$
02		compartment	mmol	$\Box$	$\overline{\mathbf{Z}}$
P04		compartment	$\text{mmol} \cdot l^{-1}$		$\overline{\mathbf{Z}}$

# **5 Reactions**

This model contains 14 reactions. All reactions are listed in the following table and are subsequently described in detail. If a reaction is affected by a modifier, the identifier of this species is written above the reaction arrow.

Table 4: Overview of all reactions

N⁰	Id	Name	Reaction Equation SBO			
1	R1		$ADP + NAD + halfglucose \longrightarrow ATP + NADH +$			
			pyruvate			
2	R2		$NADH + pyruvate \longrightarrow NAD + lactate$			
3	R3		$NAD + pyruvate + CoA \longrightarrow NADH + AcCoA$			
4	R4		$AcCoA + PO4 \longrightarrow CoA + AcP$			
5	R5		$ADP + AcP \longrightarrow ATP + Ac$			
6	R6		$NADH + AcCoA \longrightarrow NAD + CoA + AcO$			
7	R7		$NADH + AcO \longrightarrow NAD + EtOH$			
8	R8		2 pyruvate → AcLac			
9	R9		AcLac → AcetoinIn			
10	R10		AcetoinIn → AcetoinOut			
11	R11		$NADH + AcetoinIn \longrightarrow NAD + Butanediol$			
12	R12		$ATP \longrightarrow ADP$			
13	R13		$NADH + O2 \longrightarrow NAD$			
14	R14		AcLac → AcetoinIn			

#### 5.1 Reaction R1

This is an irreversible reaction of three reactants forming three products.

# **Reaction equation**

$$ADP + NAD + halfglucose \longrightarrow ATP + NADH + pyruvate$$
 (1)

#### **Reactants**

Table 5: Properties of each reactant.

Id	Name	SBO
ADP		
NAD		
halfglucose		

#### **Products**

Table 6: Properties of each product.

Id	Name	SBO
ATP		
NADH		
pyruvate		

#### **Kinetic Law**

$$v_{1} = \frac{2 \cdot V_{-1} \cdot \frac{\text{halfglucose}}{2 \cdot \text{Kglc}_{-1}} \cdot \frac{\text{NAD}}{\text{Knad}_{-1}} \cdot \frac{\text{ADP}}{\text{Kadp}_{-1}}}{\left(1 + \frac{\text{halfglucose}}{2 \cdot \text{Kglc}_{-1}} + \frac{\text{pyruvate}}{\text{Kpyr}_{-1}}\right) \cdot \left(1 + \frac{\text{NAD}}{\text{Knad}_{-1}} + \frac{\text{NADH}}{\text{Knadh}_{-1}}\right) \cdot \left(1 + \frac{\text{ADP}}{\text{Kadp}_{-1}} + \frac{\text{ATP}}{\text{Katp}_{-1}}\right)}$$
(2)

Table 7: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
$V_{-}1$			2397.000		
$\tt Kglc_1$			0.100		
${\tt Knad\_1}$			0.141		
${\tt Kadp\_1}$			0.047		
$\mathtt{Kpyr}_{\mathtt{-}}\mathtt{1}$			2.500		$   \overline{\mathscr{A}} $

Id	Name	SBO	Value	Unit	Constant
Knadh_1			0.090		$ \mathbf{Z} $
$\mathtt{Katp}_{-}\mathtt{1}$			0.019		

# 5.2 Reaction R2

This is an irreversible reaction of two reactants forming two products.

# **Reaction equation**

$$NADH + pyruvate \longrightarrow NAD + lactate$$
 (3)

#### **Reactants**

Table 8: Properties of each reactant.

Id	Name	SBO
NADH		
pyruvate		

#### **Products**

Table 9: Properties of each product.

Id	Name	SBO
NAD		
lactate		

#### **Kinetic Law**

$$v_{2} = \frac{V_{-}2 \cdot \frac{\text{pyruvate} \cdot \text{NADH} - \frac{\text{lactate} \cdot \text{NAD}}{\text{Keg}, 2}}{\text{Kpyr}_{-}2 \cdot \text{Knadh}_{-}2}}{\left(1 + \frac{\text{pyruvate}}{\text{Kpyr}_{-}2} + \frac{\text{lactate}}{\text{Klac}_{-}2}\right) \cdot \left(1 + \frac{\text{NADH}}{\text{Knadh}_{-}2} + \frac{\text{NAD}}{\text{Knad}_{-}2}\right)}$$
(4)

Table 10: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
	Ivallic	300	varuc	- Cilit	Constant
$V_{-}2$			5118.00		

Id	Name	SBO	Value	Unit	Constant
Keq_2			21120.69		
${\tt Kpyr\_2}$			1.50		$\overline{\mathbf{Z}}$
$Knadh_2$			0.08		
${\tt Klac\_2}$			100.00		$ \overline{\checkmark} $
${\tt Knad\_2}$			2.40		$\overline{\mathbf{Z}}$

#### 5.3 Reaction R3

This is an irreversible reaction of three reactants forming two products.

#### **Reaction equation**

$$NAD + pyruvate + CoA \longrightarrow NADH + AcCoA$$
 (5)

#### **Reactants**

Table 11: Properties of each reactant.

Id	Name	SBO
NAD		
pyruvate CoA		

## **Products**

Table 12: Properties of each product.

Id	Name	SBO
NADH		
AcCoA		

#### **Kinetic Law**

$$v_{3} = \frac{V_{.3} \cdot \frac{\text{pyruvate}}{\text{Kpyr}.3} \cdot \frac{\text{NAD}}{\text{Knad}.3} \cdot \frac{\text{CoA}}{\text{Kcoa}.3} \cdot \frac{\text{NAD}}{\text{NAD} + \text{Ki}.3 \cdot \text{NADH}}}{\left(1 + \frac{\text{pyruvate}}{\text{Kpyr}.3}\right) \cdot \left(1 + \frac{\text{NAD}}{\text{Knad}.3} + \frac{\text{NADH}}{\text{Knadh}.3}\right) \cdot \left(1 + \frac{\text{CoA}}{\text{Kcoa}.3} + \frac{\text{AcCoA}}{\text{Kaccoa}.3}\right)}$$
(6)

Table 13: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
V_3			259.000		Ø
Kpyr_3			1.000		$\mathbf{Z}$
${\tt Knad\_3}$			0.400		$\mathbf{Z}$
Kcoa_3			0.014		$\mathbf{Z}$
Ki_3			46.416		
$Knadh_3$			0.100		
Kaccoa_3			0.008		<u></u>

#### 5.4 Reaction R4

This is an irreversible reaction of two reactants forming two products.

# **Reaction equation**

$$AcCoA + PO4 \longrightarrow CoA + AcP$$
 (7)

#### **Reactants**

Table 14: Properties of each reactant.

Id	Name	SBO
AcCoA		
P04		

#### **Products**

Table 15: Properties of each product.

Id	Name	SBO
CoA		
AcP		

#### **Kinetic Law**

$$\nu_{4} = \frac{V_{\_}4 \cdot \frac{\text{AcCoA} \cdot [\text{PO4}] - \frac{\text{AcP} \cdot \text{CoA}}{\text{Keq.4}}}{\text{Kiaccoa.4} \cdot \text{Kpi.4}}}{1 + \frac{\text{AcCoA}}{\text{Kiaccoa.4}} + \frac{[\text{PO4}]}{\text{Kipi.4}} + \frac{\text{AcP}}{\text{Kiacp.4}} + \frac{\text{CoA}}{\text{Kicoa.4}} + \frac{\text{AcCoA} \cdot [\text{PO4}]}{\text{Kiaccoa.4} \cdot \text{Kpi.4}} + \frac{\text{AcP} \cdot \text{CoA}}{\text{Kacp.4} \cdot \text{Kicoa.4}}}$$

$$(8)$$

Table 16: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
V_4			42.000		✓
${\tt Keq\_4}$			0.007		$ \overline{\checkmark}$
Kiaccoa_4			0.200		$ \overline{\checkmark}$
Kpi_4			2.600		$\mathbf{Z}$
Kipi_4			2.600		
${\tt Kiacp\_4}$			0.200		$ \mathbf{Z} $
Kicoa_4			0.029		$ \mathbf{Z} $
Kacp_4			0.700		$\square$

#### 5.5 Reaction R5

This is an irreversible reaction of two reactants forming two products.

# **Reaction equation**

$$ADP + AcP \longrightarrow ATP + Ac \tag{9}$$

#### **Reactants**

Table 17: Properties of each reactant.

Id	Name	SBO
ADP		
AcP		

#### **Products**

Table 18: Properties of each product.

Id	Name	SBO
ATP		
Ac		

#### **Kinetic Law**

$$v_{5} = \frac{V_{-5} \cdot \frac{\text{AcP} \cdot \text{ADP} - \frac{\text{Ac} \cdot \text{ATP}}{\text{Keq.5}}}{\text{Kadp.5} \cdot \text{Kacp.5}}}{\left(1 + \frac{\text{AcP}}{\text{Kacp.5}} + \frac{\text{Ac}}{\text{Kac}}\right) \cdot \left(1 + \frac{\text{ADP}}{\text{Kadp.5}} + \frac{\text{ATP}}{\text{Katp.5}}\right)}$$
(10)

Table 19: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
V_5			2700.000		lacksquare
Keq_5			174.217		
$Kadp_{-}5$			0.500		
${\tt Kacp\_5}$			0.160		
Kac_5			7.000		
Katp_5			0.070		$\square$

#### 5.6 Reaction R6

This is an irreversible reaction of two reactants forming three products.

# **Reaction equation**

$$NADH + AcCoA \longrightarrow NAD + CoA + AcO$$
 (11)

#### **Reactants**

Table 20: Properties of each reactant.

Id	Name	SBO
NADH		
AcCoA		

# **Products**

Table 21: Properties of each product.

Id	Name	SBO
NAD		
CoA		
AcO		

Derived unit contains undeclared units

$$v_{6} = \frac{V_{-}6 \cdot \frac{\text{AcCoA} \cdot \text{NADH} - \frac{\text{CoA} \cdot \text{NAD-AcO}}{\text{Keq.6}}}{\text{Kaccoa\_6} \cdot \text{Knadh\_6}}}{\left(1 + \frac{\text{NAD}}{\text{Knad\_6}} + \frac{\text{NADH}}{\text{Knadh\_6}}\right) \cdot \left(1 + \frac{\text{AcCoA}}{\text{Kaccoa\_6}} + \frac{\text{CoA}}{\text{Kcoa\_6}}\right) \cdot \left(1 + \frac{\text{AcO}}{\text{Kaco\_6}}\right)}$$
(12)

Table 22: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
V_6			97.000		Ø
$\mathrm{Keq}_{-}6$			1.000		$\overline{\mathbf{Z}}$
Kaccoa_6			0.007		$\square$
${\tt Knadh\_6}$			0.025		$\square$
${\tt Knad\_6}$			0.080		
Kcoa_6			0.008		$\square$
Kaco_6			10.000		

#### 5.7 Reaction R7

This is an irreversible reaction of two reactants forming two products.

# **Reaction equation**

$$NADH + AcO \longrightarrow NAD + EtOH$$
 (13)

## Reactants

Table 23: Properties of each reactant.

Id	Name	SBO
NADH		
AcO		

#### **Products**

Table 24: Properties of each product.

Id	Name	SBO
NAD		
E±0H		

Id	Name	SBO

**Derived unit** contains undeclared units

$$v_7 = \frac{V_{-7} \cdot \frac{\text{AcO·NADH} - \frac{\text{EtOH·NAD}}{\text{Keq.7}}}{\text{Kaco.7·Knadh.7}}}{\left(1 + \frac{\text{NAD}}{\text{Knad.7}} + \frac{\text{NADH}}{\text{Knadh.7}}\right) \cdot \left(1 + \frac{\text{AcO}}{\text{Kaco.7}} + \frac{\text{EtOH}}{\text{Ketoh.7}}\right)}$$
(14)

Table 25: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
V_7			162.00		$\overline{Z}$
${\tt Keq\_7}$			12354.90		
${\tt Kaco7}$			0.03		
${\tt Knadh}_{-}{\tt 7}$			0.05		
${\tt Knad}_{\tt -}{\tt 7}$			0.08		
${\tt Ketoh\_7}$			1.00		

## 5.8 Reaction R8

This is an irreversible reaction of one reactant forming one product.

# **Reaction equation**

$$2 pyruvate \longrightarrow AcLac$$
 (15)

#### Reactant

Table 26: Properties of each reactant.

Id	Name	SBO
pyruvate		

## **Product**

Table 27: Properties of each product.

Id	Name	SBO
AcLac		

Id	Name	SBO

**Derived unit** contains undeclared units

$$v_{8} = \frac{V_{-8} \cdot \frac{\text{pyruvate}}{\text{Kpyr}_{-8}} \cdot \left(1 - \frac{\text{AcLac}}{\text{pyruvate} \cdot \text{Keq}_{-8}}\right) \cdot \left(\frac{\text{pyruvate}}{\text{Kpyr}_{-8}} + \frac{\text{AcLac}}{\text{Kaclac}_{-8}}\right)^{n_{-8} - 1}}{1 + \left(\frac{\text{pyruvate}}{\text{Kpyr}_{-8}} + \frac{\text{AcLac}}{\text{Kaclac}_{-8}}\right)^{n_{-8}}}$$
(16)

Table 28: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
V_8			600.000		
Kpyr_8			50.000		$\overline{\mathbf{Z}}$
Keq_8			$9\cdot 10^{12}$		$\overline{\mathbf{Z}}$
Kaclac_8			100.000		$\overline{\mathbf{Z}}$
n8			2.400		$\overline{\checkmark}$

#### 5.9 Reaction R9

This is an irreversible reaction of one reactant forming one product.

# **Reaction equation**

$$AcLac \longrightarrow AcetoinIn \tag{17}$$

#### Reactant

Table 29: Properties of each reactant.

Id	Name	SBO
AcLac		

#### **Product**

Table 30: Properties of each product.

Id	Name	SBO
AcetoinIn		

	Id	Name	SBO
--	----	------	-----

**Derived unit** contains undeclared units

$$v_9 = \frac{V_-9 \cdot \frac{\text{AcLac}}{\text{Kaclac}_-9}}{1 + \frac{\text{AcLac}}{\text{Kaclac}_-9} + \frac{\text{AcetoinIn}}{\text{Kacet}_-9}}$$
(18)

Table 31: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
V_9		106.0	$\blacksquare$
Kaclac_9		10.0	
Kacet_9		100.0	$\square$

# 5.10 Reaction R10

This is an irreversible reaction of one reactant forming one product.

# **Reaction equation**

$$AcetoinIn \longrightarrow AcetoinOut$$
 (19)

# Reactant

Table 32: Properties of each reactant.

Id	Name	SBO
AcetoinIn		

#### **Product**

Table 33: Properties of each product.

Id	Name	SBO
AcetoinOut		

**Derived unit** contains undeclared units

$$v_{10} = \frac{V_{-10} \cdot \frac{\text{AcetoinIn}}{\text{Kacet}_{-10}}}{1 + \frac{\text{AcetoinIn}}{\text{Kacet}_{-10}}}$$
(20)

Table 34: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
V_10		200.0	
Kacet_10		5.0	

# 5.11 Reaction R11

This is an irreversible reaction of two reactants forming two products.

# **Reaction equation**

$$NADH + AcetoinIn \longrightarrow NAD + Butanediol$$
 (21)

## **Reactants**

Table 35: Properties of each reactant.

Id	Name	SBO
NADH		
AcetoinIn		

#### **Products**

Table 36: Properties of each product.

Id	Name	SBO
NAD		
Butanediol		

# **Kinetic Law**

$$v_{11} = \frac{V_{-}11 \cdot \frac{\text{AcetoinIn} \cdot \text{NADH} - \frac{\text{Butanediol} \cdot \text{NAD}}{\text{Keq.}11}}{\left(1 + \frac{\text{AcetoinIn}}{\text{Kacet.}11} + \frac{\text{Butanediol}}{\text{Kbut.}11}\right) \cdot \left(1 + \frac{\text{NADH}}{\text{Knadh.}11} + \frac{\text{NAD}}{\text{Knad}.}\right)}$$
(22)

Table 37: Properties of each parameter.

Twell by the period of twell parameter.			
Id	Name	SBO Value Unit	Constant
V_11		105.00	
$\mathrm{Keq}_{-}11$		1400.00	
Kacet_11		0.06	$ ot \hspace{-1em} \checkmark$
${\tt Knadh\_11}$		0.02	$ ot \hspace{-1em} \checkmark$
${ t Kbut}_{-}11$		2.60	$\square$
Knad_11		0.16	

#### 5.12 Reaction R12

This is an irreversible reaction of one reactant forming one product.

# **Reaction equation**

$$ATP \longrightarrow ADP$$
 (23)

#### Reactant

Table 38: Properties of each reactant.

Id	Name	SBO
ATP		

#### **Product**

Table 39: Properties of each product.

Id	Name	SBO
ADP		

#### **Kinetic Law**

$$v_{12} = \frac{V_{-}12 \cdot \left(\frac{ATP}{ADP \cdot Katp_{-}12}\right)^{n_{-}12}}{1 + \left(\frac{ATP}{ADP \cdot Katp_{-}12}\right)^{n_{-}12}}$$
(24)

Table 40: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
V_12			900.000		
$\mathtt{Katp}_{\mathtt{-}}12$			6.196		
$n_{-}12$			2.580		

#### 5.13 Reaction R13

This is an irreversible reaction of two reactants forming one product.

#### **Reaction equation**

$$NADH + O2 \longrightarrow NAD \tag{25}$$

#### **Reactants**

Table 41: Properties of each reactant.

Id	Name	SBO
NADH		
02		

#### **Product**

Table 42: Properties of each product.

Id	Name	SBO
NAD		

#### **Kinetic Law**

$$v_{13} = \frac{V_{-}13 \cdot \frac{\text{NADH-O2}}{\text{Knadh.13-Ko.13}}}{\left(1 + \frac{\text{NADH}}{\text{Knadh.13}} + \frac{\text{NAD}}{\text{Knad.13}}\right) \cdot \left(1 + \frac{\text{O2}}{\text{Ko.13}}\right)}$$
(26)

Table 43: Properties of each parameter.

Id	Name	SBO Value	Unit	Constant
V_13		118.000	ı	lacksquare
$Knadh_13$		0.041		
Ko_13		0.200		
Knad_13		1.000		

# 5.14 Reaction R14

This is an irreversible reaction of one reactant forming one product.

# **Reaction equation**

$$AcLac \longrightarrow AcetoinIn \tag{27}$$

# Reactant

Table 44: Properties of each reactant.

Id	Name	SBO
AcLac		

#### **Product**

Table 45: Properties of each product.

Id	Name	SBO
AcetoinIn		

# **Kinetic Law**

$$v_{14} = k_{-}14 \cdot AcLac \tag{28}$$

Table 46: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
k_14			$3 \cdot 10^{-4}$		

# **6 Derived Rate Equations**

When interpreted as an ordinary differential equation framework, this model implies the following set of equations for the rates of change of each species.

Identifiers for kinetic laws highlighted in gray cannot be verified to evaluate to units of SBML substance per time. As a result, some SBML interpreters may not be able to verify the consistency of the units on quantities in the model. Please check if

- · parameters without an unit definition are involved or
- volume correction is necessary because the hasOnlySubstanceUnits flag may be set to false and spacialDimensions > 0 for certain species.

#### 6.1 Species ADP

#### Initial amount 4.9 mmol

This species takes part in three reactions (as a reactant in R1, R5 and as a product in R12).

$$\frac{d}{dt}ADP = |v_{12}| - |v_1| - |v_5| \tag{29}$$

#### 6.2 Species NAD

#### Initial amount 6.33 mmol

This species takes part in seven reactions (as a reactant in R1, R3 and as a product in R2, R6, R7, R11, R13).

$$\frac{d}{dt}NAD = v_2 + v_6 + v_7 + v_{11} + v_{13} - v_1 - v_3$$
(30)

#### 6.3 Species ATP

#### Initial amount 0.1 mmol

This species takes part in three reactions (as a reactant in R12 and as a product in R1, R5).

$$\frac{d}{dt}ATP = |v_1| + |v_5| - |v_{12}| \tag{31}$$

#### **6.4 Species NADH**

#### **Initial amount** 3.67 mmol

This species takes part in seven reactions (as a reactant in R2, R6, R7, R11, R13 and as a product in R1, R3).

$$\frac{d}{dt}NADH = |v_1| + |v_3| - |v_2| - |v_6| - |v_7| - |v_{11}| - |v_{13}|$$
(32)

# 6.5 Species pyruvate

#### **Initial amount** 1 mmol

This species takes part in four reactions (as a reactant in R2, R3, R8 and as a product in R1).

$$\frac{\mathrm{d}}{\mathrm{d}t} \text{pyruvate} = |v_1| - |v_2| - |v_3| - 2|v_8| \tag{33}$$

# 6.6 Species lactate

#### Initial amount 0.1 mmol

This species takes part in one reaction (as a product in R2), which does not influence its rate of change because this species is on the boundary of the reaction system:

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{lactate} = 0 \tag{34}$$

#### 6.7 Species CoA

#### Initial amount 1 mmol

This species takes part in three reactions (as a reactant in R3 and as a product in R4, R6).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{CoA} = |v_4| + |v_6| - |v_3| \tag{35}$$

# 6.8 Species halfglucose

#### Initial amount 30 mmol

This species takes part in one reaction (as a reactant in R1), which does not influence its rate of change because this species is on the boundary of the reaction system:

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{halfglucose} = 0 \tag{36}$$

# 6.9 Species AcCoA

#### Initial amount 0 mmol

This species takes part in three reactions (as a reactant in R4, R6 and as a product in R3).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{AcCoA} = |v_3| - |v_4| - |v_6| \tag{37}$$

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#### 6.10 Species AcP

#### **Initial amount** 0 mmol

This species takes part in two reactions (as a reactant in R5 and as a product in R4).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{AcP} = |v_4| - |v_5| \tag{38}$$

# 6.11 Species Ac

#### **Initial amount** 1 mmol

This species takes part in one reaction (as a product in R5), which does not influence its rate of change because this species is on the boundary of the reaction system:

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{Ac} = 0\tag{39}$$

#### 6.12 Species Ac0

#### Initial amount 0 mmol

This species takes part in two reactions (as a reactant in R7 and as a product in R6).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{AcO} = |v_6| - |v_7| \tag{40}$$

#### 6.13 Species EtOH

#### Initial amount 1 mmol

This species takes part in one reaction (as a product in R7), which does not influence its rate of change because this species is on the boundary of the reaction system:

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{EtOH} = 0\tag{41}$$

# 6.14 Species AcLac

#### Initial amount 0 mmol

This species takes part in three reactions (as a reactant in R9, R14 and as a product in R8).

$$\frac{\mathrm{d}}{\mathrm{d}t} \mathrm{AcLac} = |v_8| - |v_9| - |v_{14}| \tag{42}$$

# 6.15 Species AcetoinIn

#### **Initial amount** 0 mmol

This species takes part in four reactions (as a reactant in R10, R11 and as a product in R9, R14).

$$\frac{d}{dt}AcetoinIn = v_9 + v_{14} - v_{10} - v_{11}$$
 (43)

# 6.16 Species AcetoinOut

#### **Initial amount** 0 mmol

This species takes part in one reaction (as a product in R10), which does not influence its rate of change because this species is on the boundary of the reaction system:

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{AcetoinOut} = 0 \tag{44}$$

#### 6.17 Species Butanediol

#### Initial amount 0.01 mmol

This species takes part in one reaction (as a product in R11), which does not influence its rate of change because this species is on the boundary of the reaction system:

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{Butanediol} = 0 \tag{45}$$

# **6.18 Species** 02

#### **Initial amount** 0.2 mmol

This species takes part in one reaction (as a reactant in R13), which does not influence its rate of change because this species is on the boundary of the reaction system:

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{O}2 = 0\tag{46}$$

#### **6.19 Species** P04

# Initial amount 10 mmol

This species takes part in one reaction (as a reactant in R4), which does not influence its rate of change because this constant species is on the boundary of the reaction system:

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{PO4} = 0\tag{47}$$

SML2ATEX was developed by Andreas Dräger<sup>a</sup>, Hannes Planatscher<sup>a</sup>, Dieudonné M Wouamba<sup>a</sup>, Adrian Schröder<sup>a</sup>, Michael Hucka<sup>b</sup>, Lukas Endler<sup>c</sup>, Martin Golebiewski<sup>d</sup> and Andreas Zell<sup>a</sup>. Please see http://www.ra.cs.uni-tuebingen.de/software/SBML2LaTeX for more information.

<sup>&</sup>lt;sup>a</sup>Center for Bioinformatics Tübingen (ZBIT), Germany

<sup>&</sup>lt;sup>b</sup>California Institute of Technology, Beckman Institute BNMC, Pasadena, United States

 $<sup>^</sup>c\mathrm{European}$  Bioinformatics Institute, Wellcome Trust Genome Campus, Hinxton, United Kingdom

<sup>&</sup>lt;sup>d</sup>EML Research gGmbH, Heidelberg, Germany