

## SBML Model Report

### Model name: “Bindschadler2001\_coupled\_Ca\_oscillators”



May 6, 2016

## 1 General Overview

This is a document in SBML Level 2 Version 1 format. This model was created by Harish Dharuri<sup>1</sup> at May 31<sup>st</sup> 2006 at 8:28 a. m. and last time modified at May 24<sup>th</sup> 2014 at 4:17 p. m. Table 1 provides an overview of the quantities of all components of this model.

Table 1: Number of components in this model, which are described in the following sections.

Element	Quantity	Element	Quantity
compartment types	0	compartments	1
species types	0	species	4
events	0	constraints	0
reactions	11	function definitions	0
global parameters	16	unit definitions	1
rules	8	initial assignments	0

## Model Notes

The model reproduces the same amplitude antiphase calcium oscillations of coupled cells depicted in Figure 5B of the publication. This model was successfully tested on Jarnac and MathSBML. The values of „h1,, and „h2,, are not given in the publication, but the antiphase oscillations are reproduced over a narrow range of values of h1, h2,c1,c2,D and p. The values of D and p are given, while the other values were plugged in, in order to simulate the time profiles shown in the

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Figure. The time  $t=0$  in the figure may have been fixed after the system was allowed to settle, and hence does not correspond to the  $t=0$  of the simulation.

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To cite BioModels Database, please use: [Li C, Donizelli M, Rodriguez N, Dharuri H, Endler L, Chelliah V, Li L, He E, Henry A, Stefan MI, Snoep JL, Hucka M, Le Novre N, Laibe C \(2010\) BioModels Database: An enhanced, curated and annotated resource for published quantitative kinetic models. BMC Syst Biol., 4:92.](#)

## 2 Unit Definitions

This is an overview of five unit definitions of which four are predefined by SBML and not mentioned in the model.

### 2.1 Unit substance

**Name** micromole

**Definition**  $\mu\text{mol}$

### 2.2 Unit volume

**Notes** Litre is the predefined SBML unit for volume.

**Definition** l

### 2.3 Unit area

**Notes** Square metre is the predefined SBML unit for area since SBML Level 2 Version 1.

**Definition**  $\text{m}^2$

### 2.4 Unit length

**Notes** Metre is the predefined SBML unit for length since SBML Level 2 Version 1.

**Definition** m

## 2.5 Unit `time`

**Notes** Second is the predefined SBML unit for `time`.

**Definition** `s`

## 3 Compartment

This model contains one compartment.

Table 2: Properties of all compartments.

Id	Name	SBO	Spatial Dimensions	Size	Unit	Constant	Outside
<code>compartment</code>			3	1	litre	<input checked="" type="checkbox"/>	

### 3.1 Compartment `compartment`

This is a three dimensional compartment with a constant size of one litre.

## 4 Species

This model contains four species. Section 8 provides further details and the derived rates of change of each species.

Table 3: Properties of each species.

Id	Name	Compartment	Derived Unit	Constant	Boundary Condition
c1	Calcium ion Cell1	compartment	$\mu\text{mol} \cdot \text{l}^{-1}$	$\square$	$\square$
h1	Receptor fraction Cell1	compartment	$\mu\text{mol} \cdot \text{l}^{-1}$	$\square$	$\square$
c2	Calcium ion Cell2	compartment	$\mu\text{mol} \cdot \text{l}^{-1}$	$\square$	$\square$
h2	Receptor fraction Cell2	compartment	$\mu\text{mol} \cdot \text{l}^{-1}$	$\square$	$\square$

## 5 Parameters

This model contains 16 global parameters.

Table 4: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
Phi1_c1			0.0		<input type="checkbox"/>
r2			100.0		<input checked="" type="checkbox"/>
R1			6.0		<input checked="" type="checkbox"/>
Phi_minus1-_c1			0.0		<input type="checkbox"/>
k1			44.0		<input checked="" type="checkbox"/>
R3			50.0		<input checked="" type="checkbox"/>
Phi2_c1			0.0		<input type="checkbox"/>
k2			26.5		<input checked="" type="checkbox"/>
r4			20.0		<input checked="" type="checkbox"/>
Phi3_c1			0.0		<input type="checkbox"/>
k3			1.6		<input checked="" type="checkbox"/>
R5			1.6		<input checked="" type="checkbox"/>
Phi1_c2			0.0		<input type="checkbox"/>
Phi_minus1-_c2			0.0		<input type="checkbox"/>
Phi2_c2			0.0		<input type="checkbox"/>
Phi3_c2			0.0		<input type="checkbox"/>

## 6 Rules

This is an overview of eight rules.

### 6.1 Rule Phi1\_c1

Rule Phi1\_c1 is an assignment rule for parameter Phi1\_c1:

$$\text{Phi1\_c1} = \frac{r2 \cdot [c1]}{R1 + [c1]} \quad (1)$$

### 6.2 Rule Phi\_minus1\_c1

Rule Phi\_minus1\_c1 is an assignment rule for parameter Phi\_minus1\_c1:

$$\text{Phi\_minus1\_c1} = \frac{k1}{R3 + [c1]} \quad (2)$$

### 6.3 Rule $\text{Phi2\_c1}$

Rule  $\text{Phi2\_c1}$  is an assignment rule for parameter  $\text{Phi2\_c1}$ :

$$\text{Phi2\_c1} = \frac{k2 + r4 \cdot [c1]}{R3 + [c1]} \quad (3)$$

### 6.4 Rule $\text{Phi3\_c1}$

Rule  $\text{Phi3\_c1}$  is an assignment rule for parameter  $\text{Phi3\_c1}$ :

$$\text{Phi3\_c1} = \frac{k3}{R5 + [c1]} \quad (4)$$

### 6.5 Rule $\text{Phi1\_c2}$

Rule  $\text{Phi1\_c2}$  is an assignment rule for parameter  $\text{Phi1\_c2}$ :

$$\text{Phi1\_c2} = \frac{r2 \cdot [c2]}{R1 + [c2]} \quad (5)$$

### 6.6 Rule $\text{Phi\_minus1\_c2}$

Rule  $\text{Phi\_minus1\_c2}$  is an assignment rule for parameter  $\text{Phi\_minus1\_c2}$ :

$$\text{Phi\_minus1\_c2} = \frac{k1}{R3 + [c2]} \quad (6)$$

### 6.7 Rule $\text{Phi2\_c2}$

Rule  $\text{Phi2\_c2}$  is an assignment rule for parameter  $\text{Phi2\_c2}$ :

$$\text{Phi2\_c2} = \frac{k2 + r4 \cdot [c2]}{R3 + [c2]} \quad (7)$$

### 6.8 Rule $\text{Phi3\_c2}$

Rule  $\text{Phi3\_c2}$  is an assignment rule for parameter  $\text{Phi3\_c2}$ :

$$\text{Phi3\_c2} = \frac{k3}{R5 + [c2]} \quad (8)$$

## 7 Reactions

This model contains eleven reactions. All reactions are listed in the following table and are subsequently described in detail. If a reaction is affected by a modifier, the identifier of this species is written above the reaction arrow.

Table 5: Overview of all reactions

Nº	Id	Name	Reaction Equation	SBO
1	Jreceptor_Cell11	IP3R mediated Ca release Cell1	$\emptyset \xrightarrow{h1} c1$	
2	Jpump_Cell11	ATPase pump mediated Ca efflux Cell1	$c1 \longrightarrow \emptyset$	
3	Jleak_Cell11	IP3R independent Ca release Cell1	$\emptyset \longrightarrow c1$	
4	Inactivated_to- _S_Cell11	Inactivated to Shut state transition Cell1	$\emptyset \longrightarrow h1$	
5	Open_to- _Inactivated- _Cell11	Open to Inactivated state transition Cell1	$h1 \longrightarrow \emptyset$	
6	Jreceptor_Cell12	IP3R mediated Ca release Cell2	$\emptyset \xrightarrow{h2} c2$	
7	Jpump_Cell12	ATPase pump mediated Ca efflux Cell2	$c2 \longrightarrow \emptyset$	
8	Jleak_Cell12	IP3R independent Ca release Cell2	$\emptyset \longrightarrow c2$	
9	Inactivated_to- _S_Cell12	Inactivated to Shut state transition Cell2	$\emptyset \longrightarrow h2$	
10	Open_to- _Inactivated- _Cell12	Open to Inactivated state transition Cell2	$h2 \longrightarrow \emptyset$	
11	diffusion	Diffusion of Ca between cells	$c2 \longrightarrow c1$	

## 7.1 Reaction Jreceptor\_Cell1

This is an irreversible reaction of no reactant forming one product influenced by one modifier.

**Name** IP3R mediated Ca release Cell1

### Reaction equation



### Modifier

Table 6: Properties of each modifier.

Id	Name	SBO
h1	Receptor fraction Cell1	

### Product

Table 7: Properties of each product.

Id	Name	SBO
c1	Calcium ion Cell1	

### Kinetic Law

**Derived unit** contains undeclared units

$$v_1 = \text{vol}(\text{compartment}) \cdot k_f \cdot \left( \frac{p \cdot [h1] \cdot \text{Phi1\_c1}}{\text{Phi1\_c1} \cdot p + \text{Phi\_minus1\_c1}} \right)^4 \quad (10)$$

Table 8: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
kf			28.000		<input checked="" type="checkbox"/>
p			0.278		<input checked="" type="checkbox"/>

## 7.2 Reaction Jpump\_Cell1

This is an irreversible reaction of one reactant forming no product.



**Name** ATPase pump mediated Ca efflux Cell1

### Reaction equation



### Reactant

Table 9: Properties of each reactant.

Id	Name	SBO
c1	Calcium ion Cell1	

### Kinetic Law

**Derived unit** contains undeclared units

$$v_2 = \text{vol}(\text{compartment}) \cdot \frac{V_p \cdot [c1]^2}{K_p^2 + [c1]^2} \quad (12)$$

Table 10: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
Vp			1.20		<input checked="" type="checkbox"/>
Kp			0.18		<input checked="" type="checkbox"/>

## 7.3 Reaction Jleak\_Cell1

This is an irreversible reaction of no reactant forming one product.

**Name** IP3R independent Ca release Cell1

### Reaction equation



### Product

Table 11: Properties of each product.

Id	Name	SBO
c1	Calcium ion Cell1	

Id	Name	SBO
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### Kinetic Law

**Derived unit** contains undeclared units

$$v_3 = \text{vol}(\text{compartment}) \cdot \text{Jleak} \quad (14)$$

Table 12: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
Jleak			0.2		<input checked="" type="checkbox"/>

## 7.4 Reaction `Inactivated_to_S_Cell1`

This is an irreversible reaction of no reactant forming one product.

**Name** Inactivated to Shut state transition Cell1

### Reaction equation



### Product

Table 13: Properties of each product.

Id	Name	SBO
h1	Receptor fraction Cell1	

### Kinetic Law

**Derived unit** contains undeclared units

$$v_4 = \text{vol}(\text{compartment}) \cdot \text{Phi3\_c1} \cdot (1 - [\text{h1}]) \quad (16)$$

## 7.5 Reaction `Open_to_Inactivated_Cell1`

This is an irreversible reaction of one reactant forming no product.

**Name** Open to Inactivated state transition Cell1

### Reaction equation



### Reactant

Table 14: Properties of each reactant.

Id	Name	SBO
h1	Receptor fraction Cell1	

### Kinetic Law

**Derived unit** contains undeclared units

$$v_5 = \frac{\text{vol}(\text{compartment}) \cdot \text{Phi1\_c1} \cdot \text{Phi2\_c1} \cdot [h1] \cdot p}{\text{Phi1\_c1} \cdot p + \text{Phi\_minus1\_c1}} \quad (18)$$

Table 15: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
p			0.278		<input checked="" type="checkbox"/>

## 7.6 Reaction Jreceptor\_Cell12

This is an irreversible reaction of no reactant forming one product influenced by one modifier.

**Name** IP3R mediated Ca release Cell2

### Reaction equation



### Modifier

Table 16: Properties of each modifier.

Id	Name	SBO
h2	Receptor fraction Cell2	

## Product

Table 17: Properties of each product.

Id	Name	SBO
c2	Calcium ion Cell2	

## Kinetic Law

**Derived unit** contains undeclared units

$$v_6 = \text{vol}(\text{compartment}) \cdot k_f \cdot \left( \frac{p \cdot [h_2] \cdot \text{Phi1\_c2}}{\text{Phi1\_c2} \cdot p + \text{Phi\_minus1\_c2}} \right)^4 \quad (20)$$

Table 18: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
kf			28.000		<input checked="" type="checkbox"/>
p			0.278		<input checked="" type="checkbox"/>

## 7.7 Reaction J<sub>pump\_Cell2</sub>

This is an irreversible reaction of one reactant forming no product.

**Name** ATPase pump mediated Ca efflux Cell2

### Reaction equation



## Reactant

Table 19: Properties of each reactant.

Id	Name	SBO
c2	Calcium ion Cell2	

## Kinetic Law

**Derived unit** contains undeclared units

$$v_7 = \frac{\text{vol}(\text{compartment}) \cdot V_p \cdot [c2]^2}{K_p^2 + [c2]^2} \quad (22)$$

Table 20: Properties of each parameter.

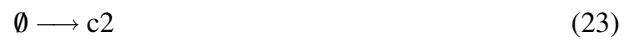
Id	Name	SBO	Value	Unit	Constant
Vp			1.20		<input checked="" type="checkbox"/>
Kp			0.18		<input checked="" type="checkbox"/>

## 7.8 Reaction Jleak\_Cell2

This is an irreversible reaction of no reactant forming one product.

**Name** IP3R independent Ca release Cell2

### Reaction equation



### Product

Table 21: Properties of each product.

Id	Name	SBO
c2	Calcium ion Cell2	

### Kinetic Law

**Derived unit** contains undeclared units

$$v_8 = \text{vol}(\text{compartment}) \cdot J_{\text{leak}} \quad (24)$$

Table 22: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
Jleak			0.2		<input checked="" type="checkbox"/>

## 7.9 Reaction Inactivated\_to\_S\_Cell2

This is an irreversible reaction of no reactant forming one product.

**Name** Inactivated to Shut state transition Cell2

### Reaction equation



### Product

Table 23: Properties of each product.

Id	Name	SBO
h2	Receptor fraction Cell2	

### Kinetic Law

**Derived unit** contains undeclared units

$$v_9 = \text{vol}(\text{compartment}) \cdot \text{Phi3\_c2} \cdot (1 - [h2]) \quad (26)$$

## 7.10 Reaction `Open_to_Inactivated_Cell2`

This is an irreversible reaction of one reactant forming no product.

**Name** Open to Inactivated state transition Cell2

### Reaction equation



### Reactant

Table 24: Properties of each reactant.

Id	Name	SBO
h2	Receptor fraction Cell2	

### Kinetic Law

**Derived unit** contains undeclared units

$$v_{10} = \frac{\text{vol}(\text{compartment}) \cdot \text{Phi1\_c2} \cdot \text{Phi2\_c2} \cdot [h2] \cdot p}{\text{Phi1\_c2} \cdot p + \text{Phi\_minus1\_c2}} \quad (28)$$

Table 25: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
p			0.278		<input checked="" type="checkbox"/>

### 7.11 Reaction diffusion

This is an irreversible reaction of one reactant forming one product.

**Name** Diffusion of Ca between cells

#### Reaction equation



#### Reactant

Table 26: Properties of each reactant.

Id	Name	SBO
c2	Calcium ion Cell2	

#### Product

Table 27: Properties of each product.

Id	Name	SBO
c1	Calcium ion Cell1	

#### Kinetic Law

**Derived unit** contains undeclared units

$$v_{11} = \text{vol}(\text{compartment}) \cdot D \cdot ([c2] - [c1]) \quad (30)$$

Table 28: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
D			0.01		<input checked="" type="checkbox"/>

## 8 Derived Rate Equations

When interpreted as an ordinary differential equation framework, this model implies the following set of equations for the rates of change of each species.

Identifiers for kinetic laws highlighted in gray cannot be verified to evaluate to units of SBML substance per time. As a result, some SBML interpreters may not be able to verify the consistency of the units on quantities in the model. Please check if

- parameters without an unit definition are involved or
- volume correction is necessary because the `hasOnlySubstanceUnits` flag may be set to `false` and `spacialDimensions` > 0 for certain species.

### 8.1 Species `c1`

**Name** Calcium ion Cell1

**Initial concentration**  $0.3 \mu\text{mol} \cdot \text{l}^{-1}$

This species takes part in four reactions (as a reactant in `Jpump_Cell1` and as a product in `Jreceptor_Cell1`, `Jleak_Cell1`, `diffusion`).

$$\frac{d}{dt}c1 = v_1 + v_3 + v_{11} - v_2 \quad (31)$$

### 8.2 Species `h1`

**Name** Receptor fraction Cell1

**Initial concentration**  $0.8 \mu\text{mol} \cdot \text{l}^{-1}$

This species takes part in three reactions (as a reactant in `Open_to_Inactivated_Cell1` and as a product in `Inactivated_to_S_Cell1` and as a modifier in `Jreceptor_Cell1`).

$$\frac{d}{dt}h1 = v_4 - v_5 \quad (32)$$

### 8.3 Species `c2`

**Name** Calcium ion Cell2

**Initial concentration**  $0.1 \mu\text{mol} \cdot \text{l}^{-1}$

This species takes part in four reactions (as a reactant in `Jpump_Cell2`, `diffusion` and as a product in `Jreceptor_Cell2`, `Jleak_Cell2`).

$$\frac{d}{dt}c2 = v_6 + v_8 - v_7 - v_{11} \quad (33)$$



## 8.4 Species `h2`

**Name** Receptor fraction Cell2

**Initial concentration**  $0.1 \mu\text{mol} \cdot \text{l}^{-1}$

This species takes part in three reactions (as a reactant in `Open_to_Inactivated_Cell2` and as a product in `Inactivated_to_S_Cell2` and as a modifier in `Jreceptor_Cell2`).

$$\frac{d}{dt}h2 = v_9 - v_{10} \quad (34)$$

SBML2<sup>AT</sup>EX was developed by Andreas Dräger<sup>a</sup>, Hannes Planatscher<sup>a</sup>, Dieudonné M Wouamba<sup>a</sup>, Adrian Schröder<sup>a</sup>, Michael Hucka<sup>b</sup>, Lukas Endler<sup>c</sup>, Martin Golebiewski<sup>d</sup> and Andreas Zell<sup>a</sup>. Please see <http://www.ra.cs.uni-tuebingen.de/software/SBML2LaTeX> for more information.

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