# **SBML Model Report**

# Model name: "Weimann2004\_CircadianOscillator"



May 5, 2016

# 1 General Overview

This is a document in SBML Level 2 Version 1 format. This model was created by Harish Dharuri $^1$  at April  $16^{th}$  2008 at 11:56 a. m. and last time modified at May  $16^{th}$  2012 at 10:04 a. m. Table 1 shows an overview of the quantities of all components of this model.

Table 1: Number of components in this model, which are described in the following sections.

Element	Quantity	Element	Quantity
compartment types	0	compartments	2
species types	0	species	7
events	0	constraints	0
reactions	17	function definitions	0
global parameters	27	unit definitions	6
rules	3	initial assignments	0

#### **Model Notes**

The model reproduces the time profile of the species as depicted in Fig 3A of the paper. Model successfully tested on MathSBML and Jarnac.

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# 2 Unit Definitions

This is an overview of nine unit definitions of which three are predefined by SBML and not mentioned in the model.

#### 2.1 Unit substance

Name nano mole

**Definition** nmol

#### 2.2 Unit time

Name hour

**Definition** 3600 s

# **2.3 Unit** nM

Name nM

**Definition**  $nmol \cdot l^{-1}$ 

# 2.4 Unit nM\_per\_hour

Name nM\_per\_hour

**Definition**  $nmol \cdot l^{-1} \cdot (3600 \text{ s})^{-1}$ 

#### 2.5 Unit time\_inverse

Name hr\_inv

 $\textbf{Definition} \ \left(3600 \ s\right)^{-1}$ 

#### 2.6 Unit nM\_inv\_hr\_inv

Name nM\_inv\_hr\_inv

**Definition**  $nmol^{-1} \cdot l \cdot (3600 \text{ s})^{-1}$ 

# 2.7 Unit volume

**Notes** Litre is the predefined SBML unit for volume.

**Definition** 1

#### 2.8 Unit area

**Notes** Square metre is the predefined SBML unit for area since SBML Level 2 Version 1.

**Definition** m<sup>2</sup>

# 2.9 Unit length

**Notes** Metre is the predefined SBML unit for length since SBML Level 2 Version 1.

**Definition** m

# 3 Compartments

This model contains two compartments.

Table 2: Properties of all compartments.

Id	Name	SBO	Spatial Dimensions	Size	Unit	Constant	Outside
Nucleus Cytoplasm	Nucleus Cytoplasm		3 3	1	litre litre	<b>1</b>	

# 3.1 Compartment Nucleus

This is a three dimensional compartment with a constant size of one litre.

Name Nucleus

# 3.2 Compartment Cytoplasm

This is a three dimensional compartment with a constant size of one litre.

Name Cytoplasm

# Produced by SBML2LATEX

# 4 Species

This model contains seven species. Section 8 provides further details and the derived rates of change of each species.

Table 3: Properties of each species.

Id	Name	Compartment	Derived Unit	Constant	Boundary Condi- tion
y1	Per2 or Cry mRNA	Cytoplasm	$nmol \cdot 1^{-1}$		
у2	PER2_CRY_complex_cytoplasm	Cytoplasm	$nmol \cdot l^{-1}$		
у3	PER2_CRY_complex_nucleus	Nucleus	$nmol \cdot l^{-1}$		
y4	Bmal1 mRNA	Cytoplasm	$nmol \cdot l^{-1}$		
у5	BMAL1_cytoplasm	Cytoplasm	$nmol \cdot l^{-1}$		
у6	BMAL1_nucleus	Nucleus	$nmol \cdot l^{-1}$	$\Box$	
y7	Active BMAL1	Nucleus	$nmol \cdot l^{-1}$	$\Box$	$\Box$

# **5 Parameters**

This model contains 27 global parameters.

Table 4: Properties of each parameter.

Id	Name	SBO	Value	Unit	Co	onstant
trans_per2-			0.000	nmol · 1 <sup>-1</sup>		$\Box$
_cry				$(3600 \text{ s})^{-1}$		
v1b			9.000	nmol $\cdot$ $1^{-1}$		
				$(3600 \text{ s})^{-1}$		
С			0.010	$nmol \cdot l^{-1}$		
k1b			1.000	$nmol \cdot l^{-1}$		
k1i			0.560	$nmol \cdot l^{-1}$		
$\mathtt{hill\_coeff}$			8.000	dimensionless		
$trans\_Bmal1$			0.000	nmol $\cdot$ $1^{-1}$	•	
				$(3600 \text{ s})^{-1}$		
v4b			3.600	nmol $\cdot$ $1^{-1}$	•	
				$(3600 \text{ s})^{-1}$		
r			3.000	dimensionless		
k4b			2.160	$nmol \cdot l^{-1}$		
y5_y6_y7			3.050	$nmol \cdot l^{-1}$		
k1d			0.120	$(3600 \text{ s})^{-1}$		
k2b			0.300	$nmol^{-1}$ · 1	•	
				$(3600 \text{ s})^{-1}$		
q			2.000	dimensionless		
k2d			0.050	$(3600 \text{ s})^{-1}$		
k2t			0.240	$(3600 \text{ s})^{-1}$		
k3t			0.020	$(3600 \text{ s})^{-1}$		
k3d			0.120	$(3600 \text{ s})^{-1}$		
k4d			0.750	$(3600 \text{ s})^{-1}$		
k5b			0.240	$(3600 \text{ s})^{-1}$		
k5d			0.060	$(3600 \text{ s})^{-1}$		
k5t			0.450	$(3600 \text{ s})^{-1}$		
k6t			0.060	$(3600 \text{ s})^{-1}$		$\overline{\mathbf{Z}}$
k6d			0.120	$(3600 \text{ s})^{-1}$		$\overline{\mathbf{Z}}$
k6a			0.090	$(3600 \text{ s})^{-1}$		$\mathbf{Z}$
k7a			0.003	$(3600 \text{ s})^{-1}$		$ \mathbf{Z} $
k7d			0.090	$(3600 \text{ s})^{-1}$		

# 6 Rules

This is an overview of three rules.

# **6.1 Rule** trans\_per2\_cry

Rule trans\_per2\_cry is an assignment rule for parameter trans\_per2\_cry:

$$trans\_per2\_cry = \frac{v1b \cdot ([y7] + c)}{k1b \cdot \left(1 + \left(\frac{[y3]}{k1i}\right)^{hill\_coeff}\right) + [y7] + c}$$
 (1)

#### 6.2 Rule trans\_Bmal1

Rule trans\_Bmal1 is an assignment rule for parameter trans\_Bmal1:

$$trans\_Bmal1 = \frac{v4b \cdot [y3]^r}{k4b^r + [y3]^r} \tag{2}$$

Derived unit  $10^{-9} \text{ mol} \cdot l^{-1} \cdot (3600 \text{ s})^{-1}$ 

# **6.3 Rule** y5\_y6\_y7

Rule y5\_y6\_y7 is an assignment rule for parameter y5\_y6\_y7:

$$y5_y6_y7 = [y5] + [y6] + [y7]$$
 (3)

**Derived unit**  $nmol \cdot l^{-1}$ 

# 7 Reactions

This model contains 17 reactions. All reactions are listed in the following table and are subsequently described in detail. If a reaction is affected by a modifier, the identifier of this species is written above the reaction arrow.

Table 5: Overview of all reactions

N⁰	Id	Name	Reaction Equation	SBO
1	per2_cry- _transcription	per2_cry_transcription	$\emptyset \longrightarrow y1$	
2	per2_cry_mRNA- _degradation	per2_cry_mRNA_degradation	$y1 \longrightarrow \emptyset$	
3	per2_cry- _complex- _formation	per2_cry_complex_formation	$\emptyset \xrightarrow{y1} y2$	
4	<pre>cytoplasmicper2_crycomplexdegradation</pre>	cytoplasmic_per2_cry_complex_degradation	$y2 \longrightarrow \emptyset$	
5	per2_cry- _nuclear_import	per2_cry_nuclear_import	$y2 \longrightarrow y3$	
6	per2_cry- _nuclear_export	per2_cry_nuclear_export	$y3 \longrightarrow y2$	
7	nuclear_per2- _cry_complex- _degradation	nuclear_per2_cry_complex_degradation	y3	
8	Bmal1- _transcription	Bmal1_transcription	$\emptyset \longrightarrow y4$	
9	Bmal1_mRNA- _degradation	Bmal1_mRNA_degradation	y4	

N⁰	Id	Name	Reaction Equation	SBO
10	BMAL1- _translation	BMAL1_translation	$\emptyset \xrightarrow{y4} y5$	
11	cytoplasmic- _BMAL1- _degradation	cytoplasmic_BMAL1_degradation	$y5 \longrightarrow \emptyset$	
12	BMAL1_nuclear- _import	BMAL1_nuclear_import	$y5 \longrightarrow y6$	
13	BMAL1_nuclear- _export	BMAL1_nuclear_export	$y6 \longrightarrow y5$	
14	nuclear_BMAL1- _degradation	nuclear_BMAL1_degradation	$y6 \longrightarrow \emptyset$	
15	BMAL1activation	BMAL1_activation	$y6 \longrightarrow y7$	
16	BMAL1- _deactivation	BMAL1_deactivation	$y7 \longrightarrow y6$	
17	Active_BMAL1- _degradation	Active_BMAL1_degradation	y7	

# **7.1 Reaction** per2\_cry\_transcription

This is an irreversible reaction of no reactant forming one product.

Name per2\_cry\_transcription

# **Reaction equation**

$$\emptyset \longrightarrow y1$$
 (4)

#### **Product**

Table 6: Properties of each product.

	*	
Id	Name	SBO
y1	Per2 or Cry mRNA	

#### **Kinetic Law**

**Derived unit**  $nmol \cdot (3600 \text{ s})^{-1}$ 

$$v_1 = \text{vol}\left(\text{Cytoplasm}\right) \cdot \text{trans\_per2\_cry}$$
 (5)

# 7.2 Reaction per2\_cry\_mRNA\_degradation

This is an irreversible reaction of one reactant forming no product.

Name per2\_cry\_mRNA\_degradation

# **Reaction equation**

$$y1 \longrightarrow \emptyset$$
 (6)

#### Reactant

Table 7: Properties of each reactant.

Id	Name	SBO
у1	Per2 or Cry mRNA	

#### **Kinetic Law**

$$v_2 = \text{vol}\left(\text{Cytoplasm}\right) \cdot \text{k1d} \cdot [\text{y1}] \tag{7}$$

# 7.3 Reaction per2\_cry\_complex\_formation

This is an irreversible reaction of no reactant forming one product influenced by one modifier.

Name per2\_cry\_complex\_formation

#### **Reaction equation**

$$\emptyset \xrightarrow{y1} y2 \tag{8}$$

#### Modifier

Table 8: Properties of each modifier.

Id	Name	SBO
y1	Per2 or Cry mRNA	

#### **Product**

Table 9: Properties of each product.

Id	Name	SBO
у2	PER2_CRY_complex_cytoplasm	

#### **Kinetic Law**

**Derived unit**  $9.99999999999998 \cdot 10^{-10} \text{ mol} \cdot (3600 \text{ s})^{-1}$ 

$$v_3 = \text{vol}\left(\text{Cytoplasm}\right) \cdot \text{k2b} \cdot [\text{y1}]^q$$
 (9)

# **7.4 Reaction** cytoplasmic\_per2\_cry\_complex\_degradation

This is an irreversible reaction of one reactant forming no product.

Name cytoplasmic\_per2\_cry\_complex\_degradation

# **Reaction equation**

$$y2 \longrightarrow \emptyset$$
 (10)

#### Reactant

Table 10: Properties of each reactant.

	<u>.</u>	
Id	Name	SBO
y2	PER2_CRY_complex_cytoplasm	

**Derived unit**  $(3600 \text{ s})^{-1} \cdot \text{nmol}$ 

$$v_4 = \text{vol}\left(\text{Cytoplasm}\right) \cdot \text{k2d} \cdot [\text{y2}]$$
 (11)

# 7.5 Reaction per2\_cry\_nuclear\_import

This is an irreversible reaction of one reactant forming one product.

Name per2\_cry\_nuclear\_import

#### **Reaction equation**

$$y2 \longrightarrow y3$$
 (12)

#### Reactant

Table 11: Properties of each reactant.

Id	Name	SBO
у2	PER2_CRY_complex_cytoplasm	

#### **Product**

Table 12: Properties of each product.

Id	Name	SBO
уЗ	PER2_CRY_complex_nucleus	

#### **Kinetic Law**

$$v_5 = \text{vol}(\text{Cytoplasm}) \cdot \text{k2t} \cdot [\text{y2}]$$
 (13)

# 7.6 Reaction per2\_cry\_nuclear\_export

This is an irreversible reaction of one reactant forming one product.

Name per2\_cry\_nuclear\_export

# **Reaction equation**

$$y3 \longrightarrow y2$$
 (14)

#### Reactant

Table 13: Properties of each reactant.

Id	Name	SBO
у3	PER2_CRY_complex_nucleus	

#### **Product**

Table 14: Properties of each product.

Id	Name	SBO
у2	PER2_CRY_complex_cytoplasm	

# **Kinetic Law**

**Derived unit**  $(3600 \text{ s})^{-1} \cdot \text{nmol}$ 

$$v_6 = \text{vol}\left(\text{Nucleus}\right) \cdot \text{k3t} \cdot [\text{y3}] \tag{15}$$

# 7.7 Reaction nuclear\_per2\_cry\_complex\_degradation

This is an irreversible reaction of one reactant forming no product.

Name nuclear\_per2\_cry\_complex\_degradation

# **Reaction equation**

$$y3 \longrightarrow \emptyset$$
 (16)

#### Reactant

Table 15: Properties of each reactant

Table 13. I Toperties of Cach reactant.		
Id	Name	SBO
у3	PER2_CRY_complex_nucleus	

**Derived unit**  $(3600 \text{ s})^{-1} \cdot \text{nmol}$ 

$$v_7 = \text{vol}(\text{Nucleus}) \cdot \text{k3d} \cdot [\text{y3}] \tag{17}$$

# 7.8 Reaction Bmal1\_transcription

This is an irreversible reaction of no reactant forming one product.

Name Bmal1\_transcription

#### **Reaction equation**

$$\emptyset \longrightarrow y4$$
 (18)

#### **Product**

Table 16: Properties of each product.

Id	Name	SBO
y4	Bmal1 mRNA	

#### **Kinetic Law**

**Derived unit**  $nmol \cdot (3600 \text{ s})^{-1}$ 

$$v_8 = \text{vol}\left(\text{Cytoplasm}\right) \cdot \text{trans\_Bmal1}$$
 (19)

# 7.9 Reaction Bmal1\_mRNA\_degradation

This is an irreversible reaction of one reactant forming no product.

Name Bmal1\_mRNA\_degradation

# **Reaction equation**

$$y4 \longrightarrow \emptyset$$
 (20)

#### Reactant

Table 17: Properties of each reactant.

Id	Name	SBO
y4	Bmal1 mRNA	

#### **Kinetic Law**

**Derived unit**  $(3600 \text{ s})^{-1} \cdot \text{nmol}$ 

$$v_9 = \text{vol}\left(\text{Cytoplasm}\right) \cdot \text{k4d} \cdot [\text{y4}]$$
 (21)

# 7.10 Reaction BMAL1\_translation

This is an irreversible reaction of no reactant forming one product influenced by one modifier.

Name BMAL1\_translation

# **Reaction equation**

$$\emptyset \xrightarrow{y4} y5 \tag{22}$$

# **Modifier**

Table 18: Properties of each modifier.

Id	Name	SBO
y4	Bmal1 mRNA	

# **Product**

Table 19: Properties of each product.

Id	Name	SBO
у5	BMAL1_cytoplasm	

#### **Kinetic Law**

$$v_{10} = \text{vol}\left(\text{Cytoplasm}\right) \cdot \text{k5b} \cdot [\text{y4}] \tag{23}$$

# **7.11 Reaction** cytoplasmic\_BMAL1\_degradation

This is an irreversible reaction of one reactant forming no product.

Name cytoplasmic\_BMAL1\_degradation

# **Reaction equation**

$$y5 \longrightarrow \emptyset$$
 (24)

#### Reactant

Table 20: Properties of each reactant.

Id	Name	SBO
у5	BMAL1_cytoplasm	

#### **Kinetic Law**

**Derived unit**  $(3600 \text{ s})^{-1} \cdot \text{nmol}$ 

$$v_{11} = \text{vol}\left(\text{Cytoplasm}\right) \cdot \text{k5d} \cdot [\text{y5}]$$
 (25)

# 7.12 Reaction BMAL1\_nuclear\_import

This is an irreversible reaction of one reactant forming one product.

Name BMAL1\_nuclear\_import

# **Reaction equation**

$$y5 \longrightarrow y6$$
 (26)

#### Reactant

Table 21: Properties of each reactant.

Id	Name	SBO
у5	BMAL1_cytoplasm	

#### **Product**

Table 22: Properties of each product.

Id	Name	SBO
у6	BMAL1_nucleus	

**Derived unit**  $(3600 \text{ s})^{-1} \cdot \text{nmol}$ 

$$v_{12} = vol(Cytoplasm) \cdot k5t \cdot [y5]$$
 (27)

# 7.13 Reaction BMAL1\_nuclear\_export

This is an irreversible reaction of one reactant forming one product.

Name BMAL1\_nuclear\_export

#### **Reaction equation**

$$y6 \longrightarrow y5$$
 (28)

#### Reactant

Table 23: Properties of each reactant.

Id	Name	SBO
у6	BMAL1_nucleus	

#### **Product**

Table 24: Properties of each product.

Id	Name	SBO
у5	BMAL1_cytoplasm	

#### **Kinetic Law**

$$v_{13} = \text{vol}(\text{Nucleus}) \cdot \text{k6t} \cdot [\text{y6}] \tag{29}$$

# 7.14 Reaction nuclear\_BMAL1\_degradation

This is an irreversible reaction of one reactant forming no product.

Name nuclear\_BMAL1\_degradation

# **Reaction equation**

$$y6 \longrightarrow \emptyset$$
 (30)

#### Reactant

Table 25: Properties of each reactant.

Id	Name	SBO
у6	BMAL1_nucleus	

#### **Kinetic Law**

**Derived unit**  $(3600 \text{ s})^{-1} \cdot \text{nmol}$ 

$$v_{14} = \text{vol}(\text{Nucleus}) \cdot \text{k6d} \cdot [\text{y6}] \tag{31}$$

# 7.15 Reaction BMAL1\_activation

This is an irreversible reaction of one reactant forming one product.

Name BMAL1\_activation

# **Reaction equation**

$$y6 \longrightarrow y7$$
 (32)

#### Reactant

Table 26: Properties of each reactant.

Id	Name	SBO
у6	BMAL1_nucleus	

#### **Product**

Table 27: Properties of each product.

Id	Name	SBO
у7	Active BMAL1	

**Derived unit**  $(3600 \text{ s})^{-1} \cdot \text{nmol}$ 

$$v_{15} = \text{vol}(\text{Nucleus}) \cdot \text{k6a} \cdot [\text{y6}] \tag{33}$$

#### 7.16 Reaction BMAL1\_deactivation

This is an irreversible reaction of one reactant forming one product.

Name BMAL1\_deactivation

# **Reaction equation**

$$y7 \longrightarrow y6$$
 (34)

#### Reactant

Table 28: Properties of each reactant.

Id	Name	SBO
у7	Active BMAL1	

#### **Product**

Table 29: Properties of each product.

Id	Name	SBO
у6	BMAL1_nucleus	

#### **Kinetic Law**

$$v_{16} = \text{vol}\left(\text{Nucleus}\right) \cdot \text{k7a} \cdot [\text{y7}] \tag{35}$$

# 7.17 Reaction Active\_BMAL1\_degradation

This is an irreversible reaction of one reactant forming no product.

Name Active\_BMAL1\_degradation

#### **Reaction equation**

$$y7 \longrightarrow \emptyset$$
 (36)

#### Reactant

Table 30: Properties of each reactant.

Id	Name	SBO
у7	Active BMAL1	

#### **Kinetic Law**

**Derived unit**  $(3600 \text{ s})^{-1} \cdot \text{nmol}$ 

$$v_{17} = \text{vol}(\text{Nucleus}) \cdot \text{k7d} \cdot [\text{y7}] \tag{37}$$

# 8 Derived Rate Equations

When interpreted as an ordinary differential equation framework, this model implies the following set of equations for the rates of change of each species.

# 8.1 Species y1

Name Per2 or Cry mRNA

Initial concentration  $0.2 \text{ nmol} \cdot 1^{-1}$ 

This species takes part in three reactions (as a reactant in per2\_cry\_mRNA\_degradation and as a product in per2\_cry\_transcription and as a modifier in per2\_cry\_complex\_formation).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathbf{y}\mathbf{1} = v_1 - v_2 \tag{38}$$

# 8.2 Species y2

Name PER2\_CRY\_complex\_cytoplasm

Initial concentration  $0 \text{ nmol} \cdot l^{-1}$ 

This species takes part in four reactions (as a reactant in cytoplasmic\_per2\_cry\_complex\_degradation, per2\_cry\_nuclear\_import and as a product in per2\_cry\_complex\_formation, per2\_cry\_nuclear\_export).

$$\frac{\mathrm{d}}{\mathrm{d}t}y2 = v_3 + v_6 - v_4 - v_5 \tag{39}$$

#### 8.3 Species y3

Name PER2\_CRY\_complex\_nucleus

Initial concentration  $1.1 \text{ nmol} \cdot l^{-1}$ 

This species takes part in three reactions (as a reactant in per2\_cry\_nuclear\_export, nuclear\_per2\_cry\_complex\_degradation and as a product in per2\_cry\_nuclear\_import).

$$\frac{d}{dt}y3 = v_5 - v_6 - v_7 \tag{40}$$

#### 8.4 Species y4

Name Bmall mRNA

Initial concentration 0.8 nmol·l<sup>-1</sup>

This species takes part in three reactions (as a reactant in Bmall\_mRNA\_degradation and as a product in Bmall\_transcription and as a modifier in BMALl\_translation).

$$\frac{\mathrm{d}}{\mathrm{d}t}y4 = v_8 - v_9 \tag{41}$$

#### 8.5 Species y5

Name BMAL1\_cytoplasm

Initial concentration  $1 \text{ nmol} \cdot l^{-1}$ 

This species takes part in four reactions (as a reactant in cytoplasmic\_BMAL1\_degradation, BMAL1\_nuclear\_import and as a product in BMAL1\_translation, BMAL1\_nuclear\_export).

$$\frac{\mathrm{d}}{\mathrm{d}t}y5 = v_{10} + v_{13} - v_{11} - v_{12} \tag{42}$$

# 8.6 Species y6

Name BMAL1\_nucleus

Initial concentration  $1 \text{ nmol} \cdot l^{-1}$ 

This species takes part in five reactions (as a reactant in BMAL1\_nuclear\_export, nuclear\_BMAL1\_degradation, BMAL1\_activation and as a product in BMAL1\_nuclear\_import, BMAL1\_deactivation).

$$\frac{\mathrm{d}}{\mathrm{d}t}y6 = v_{12} + v_{16} - v_{13} - v_{14} - v_{15} \tag{43}$$

#### 8.7 Species y7

Name Active BMAL1

Initial concentration 1.05 nmol·l<sup>-1</sup>

This species takes part in three reactions (as a reactant in BMAL1\_deactivation, Active-\_BMAL1\_degradation and as a product in BMAL1\_activation).

$$\frac{\mathrm{d}}{\mathrm{d}t}y7 = v_{15} - v_{16} - v_{17} \tag{44}$$

 $\mathfrak{BML2}^{d}$  was developed by Andreas Dräger<sup>a</sup>, Hannes Planatscher<sup>a</sup>, Dieudonné M Wouamba<sup>a</sup>, Adrian Schröder<sup>a</sup>, Michael Hucka<sup>b</sup>, Lukas Endler<sup>c</sup>, Martin Golebiewski<sup>d</sup> and Andreas Zell<sup>a</sup>. Please see http://www.ra.cs.uni-tuebingen.de/software/SBML2LaTeX for more information.

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