

## SBML Model Report

**Model name:**  
**“Swat2004\_Mammalian\_G1\_S\_Transition”**



May 6, 2016

### 1 General Overview

This is a document in SBML Level 2 Version 4 format. This model was created by Lukas Endler<sup>1</sup> at August 17<sup>th</sup> 2009 at 2:15 p.m. and last time modified at August ninth 2012 at 4:28 p.m. Table 1 shows an overview of the quantities of all components of this model.

Table 1: Number of components in this model, which are described in the following sections.

| Element           | Quantity | Element              | Quantity |
|-------------------|----------|----------------------|----------|
| compartment types | 0        | compartments         | 1        |
| species types     | 0        | species              | 9        |
| events            | 0        | constraints          | 0        |
| reactions         | 22       | function definitions | 0        |
| global parameters | 40       | unit definitions     | 3        |
| rules             | 0        | initial assignments  | 0        |

### Model Notes

This is the extended model described the article:

**Bifurcation analysis of the regulatory modules of the mammalian G1/S transition.**

Swat M, Kel A, Herzel H. *Bioinformatics* 2004 Jul 10;20(10):1506-11. PMID: [15231543](#) , doi: [10.1093/bioinformatics/bth110](#)

#### Abstract:

MOTIVATION: Mathematical models of the cell cycle can contribute to an understanding of

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its basic mechanisms. Modern simulation tools make the analysis of key components and their interactions very effective. This paper focuses on the role of small modules and feedbacks in the gene-protein network governing the G1/S transition in mammalian cells. Mutations in this network may lead to uncontrolled cell proliferation. Bifurcation analysis helps to identify the key components of this extremely complex interaction network.

**RESULTS:** We identify various positive and negative feedback loops in the network controlling the G1/S transition. It is shown that the positive feedback regulation of E2F1 and a double activator-inhibitor module can lead to bistability. Extensions of the core module preserve the essential features such as bistability. The complete model exhibits a transcritical bifurcation in addition to bistability. We relate these bifurcations to the cell cycle checkpoint and the G1/S phase transition point. Thus, core modules can explain major features of the complex G1/S network and have a robust decision taking function.

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To cite BioModels Database, please use [Le Novre N., Bornstein B., Broicher A., Courtot M., Donizelli M., Dharuri H., Li L., Sauro H., Schilstra M., Shapiro B., Snoep J.L., Hucka M. \(2006\) BioModels Database: A Free, Centralized Database of Curated, Published, Quantitative Kinetic Models of Biochemical and Cellular Systems Nucleic Acids Res., 34: D689-D691.](#)

## 2 Unit Definitions

This is an overview of five unit definitions of which two are predefined by SBML and not mentioned in the model.

### 2.1 Unit `time`

**Name** norm. time

**Definition** dimensionless

### 2.2 Unit `volume`

**Name** norm. volume

**Definition** dimensionless

### 2.3 Unit `substance`

**Name** norm substance

**Definition** dimensionless

### 2.4 Unit `area`

**Notes** Square metre is the predefined SBML unit for area since SBML Level 2 Version 1.

**Definition** m<sup>2</sup>

### 2.5 Unit `length`

**Notes** Metre is the predefined SBML unit for length since SBML Level 2 Version 1.

**Definition** m

## 3 Compartment

This model contains one compartment.

Table 2: Properties of all compartments.

| Id   | Name | SBO | Spatial<br>Dimensions | Size | Unit          | Constant                            | Outside |
|------|------|-----|-----------------------|------|---------------|-------------------------------------|---------|
| cell | cell |     | 3                     | 1    | dimensionless | <input checked="" type="checkbox"/> |         |

### 3.1 Compartment `cell`

This is a three dimensional compartment with a constant size of one dimensionless.

**Name** cell

## 4 Species

This model contains nine species. Section 7 provides further details and the derived rates of change of each species.

Table 3: Properties of each species.

| Id    | Name           | Compartment | Derived Unit                                 | Constant | Boundary Condition |
|-------|----------------|-------------|--|----------|--------------------|
| pRB   | pRB            | cell        | dimensionless<br>dimensionless <sup>-1</sup> | ·<br>⊖   | ⊖                  |
| pRBp  | pRBp           | cell        | dimensionless<br>dimensionless <sup>-1</sup> | ·<br>⊖   | ⊖                  |
| E2F1  | E2F1           | cell        | dimensionless<br>dimensionless <sup>-1</sup> | ·<br>⊖   | ⊖                  |
| CycDi | CycD/cdk4,6(i) | cell        | dimensionless<br>dimensionless <sup>-1</sup> | ·<br>⊖   | ⊖                  |
| CycDa | CycD/cdk4,6(a) | cell        | dimensionless<br>dimensionless <sup>-1</sup> | ·<br>⊖   | ⊖                  |
| AP1   | AP1            | cell        | dimensionless<br>dimensionless <sup>-1</sup> | ·<br>⊖   | ⊖                  |
| pRBpp | pRBpp          | cell        | dimensionless<br>dimensionless <sup>-1</sup> | ·<br>⊖   | ⊖                  |
| CycEi | CycE/cdk2(i)   | cell        | dimensionless<br>dimensionless <sup>-1</sup> | ·<br>⊖   | ⊖                  |
| CycEa | CycEa/cdk2(a)  | cell        | dimensionless<br>dimensionless <sup>-1</sup> | ·<br>⊖   | ⊖                  |

## 5 Parameters

This model contains 40 global parameters.

Table 4: Properties of each parameter.

| Id        | Name      | SBO | Value | Unit | Constant |
|-----------|-----------|-----|-------|------|----------|
| k1        | k1        |     | 1.000 |      | ✓        |
| Km1       | Km1       |     | 0.500 |      | ✓        |
| J11       | J11       |     | 0.500 |      | ✓        |
| J61       | J61       |     | 5.000 |      | ✓        |
| k16       | k16       |     | 0.400 |      | ✓        |
| k61       | k61       |     | 0.300 |      | ✓        |
| phi_pRB   | phi_pRB   |     | 0.005 |      | ✓        |
| kp        | kp        |     | 0.050 |      | ✓        |
| k2        | k2        |     | 1.600 |      | ✓        |
| a         | a         |     | 0.040 |      | ✓        |
| Km2       | Km2       |     | 4.000 |      | ✓        |
| J12       | J12       |     | 5.000 |      | ✓        |
| J62       | J62       |     | 8.000 |      | ✓        |
| phi_E2F1  | phi_E2F1  |     | 0.100 |      | ✓        |
| k3        | k3        |     | 0.050 |      | ✓        |
| k23       | k23       |     | 0.300 |      | ✓        |
| J13       | J13       |     | 0.002 |      | ✓        |
| J63       | J63       |     | 2.000 |      | ✓        |
| k34       | k34       |     | 0.040 |      | ✓        |
| Km4       | Km4       |     | 0.300 |      | ✓        |
| phi_CycDi | phi_CycDi |     | 0.023 |      | ✓        |
| k43       | k43       |     | 0.010 |      | ✓        |
| phi_CycDa | phi_CycDa |     | 0.030 |      | ✓        |
| Fm        | Fm        |     | 0.005 |      | ✓        |
| k25       | k25       |     | 0.900 |      | ✓        |
| J15       | J15       |     | 0.001 |      | ✓        |
| J65       | J65       |     | 6.000 |      | ✓        |
| phi_AP1   | phi_AP1   |     | 0.010 |      | ✓        |
| k67       | k67       |     | 0.700 |      | ✓        |
| k76       | k76       |     | 0.100 |      | ✓        |
| phi_pRBpp | phi_pRBpp |     | 0.040 |      | ✓        |
| phi_pRBp  | phi_pRBp  |     | 0.060 |      | ✓        |
| k28       | k28       |     | 0.060 |      | ✓        |
| J18       | J18       |     | 0.600 |      | ✓        |
| J68       | J68       |     | 7.000 |      | ✓        |
| k89       | k89       |     | 0.070 |      | ✓        |
| Km9       | Km9       |     | 0.005 |      | ✓        |

| Id        | Name      | SBO | Value | Unit | Constant                            |
|-----------|-----------|-----|-------|------|-------------------------------------|
| k98       | k98       |     | 0.010 |      | <input checked="" type="checkbox"/> |
| phi_CycEi | phi_CycEi |     | 0.060 |      | <input checked="" type="checkbox"/> |
| phi_CycEa | phi_CycEa |     | 0.050 |      | <input checked="" type="checkbox"/> |

## 6 Reactions

This model contains 22 reactions. All reactions are listed in the following table and are subsequently described in detail. If a reaction is affected by a modifier, the identifier of this species is written above the reaction arrow.

Table 5: Overview of all reactions

| Nº | Id                      | Name                   | Reaction Equation  | SBO |
|----|-------------------------|------------------------|--|-----|
| 1  | pRB_synthesis           | pRB synthesis          | $\emptyset \xrightarrow{\text{pRB, pRBp, E2F1}} \text{pRB}$        |     |
| 2  | pRB-_phosphorylation    | pRB phosphorylation    | $\text{pRB} \xrightarrow{\text{pRB, CycDa}} \text{pRBp}$           |     |
| 3  | pRBp-_dephosphorylation | pRBp dephosphorylation | $\text{pRBp} \longrightarrow \text{pRB}$                           |     |
| 4  | pRB_degradation         | pRB degradation        | $\text{pRB} \longrightarrow \emptyset$                             |     |
| 5  | E2F1_synthesis          | E2F1 synthesis         | $\emptyset \xrightarrow{\text{E2F1, pRB, pRBp}} \text{E2F1}$       |     |
| 6  | E2F1-_degradation       | E2F1 degradation       | $\text{E2F1} \longrightarrow \emptyset$                            |     |
| 7  | CycD_synthesis          | CycD synthesis         | $\emptyset \xrightarrow{\text{E2F1, pRB, pRBp, AP1}} \text{CycDi}$ |     |
| 8  | CycD_inhibition         | CycD inhibition        | $\text{CycDa} \longrightarrow \text{CycDi}$                        |     |
| 9  | CycD_activation         | CycD activation        | $\text{CycDi} \xrightarrow{\text{CycDi, CycDa}} \text{CycDa}$      |     |
| 10 | CycD-_degradation       | CycD degradation       | $\text{CycDi} \longrightarrow \emptyset$                           |     |
| 11 | CycD-_degradation2      | CycD degradation2      | $\text{CycDa} \longrightarrow \emptyset$                           |     |
| 12 | AP1_synthesis           | AP1 synthesis          | $\emptyset \xrightarrow{\text{E2F1, pRB, pRBp}} \text{AP1}$        |     |
| 13 | Ap1_degradation         | Ap1 degradation        | $\text{AP1} \longrightarrow \emptyset$                             |     |
| 14 | pRBp-_phosphorylation   | pRBp phosphorylation   | $\text{pRBp} \xrightarrow{\text{pRBp, CycEa}} \text{pRBpp}$        |     |

| Nº | Id                           | Name                    | Reaction Equation   | SBO |
|----|------------------------------|-------------------------|---|-----|
| 15 | pRBpp-<br>_dephosphorylation | pRBpp dephosphorylation | $\text{pRBpp} \longrightarrow \text{pRBp}$                    |     |
| 16 | pRBpp-<br>_degradation       | pRBpp degradation       | $\text{pRBpp} \longrightarrow \emptyset$                      |     |
| 17 | pRBp-<br>_degradation        | pRBp degradation        | $\text{pRBp} \longrightarrow \emptyset$                       |     |
| 18 | CycE.synthesis               | CycE synthesis          | $\emptyset \xrightarrow{\text{E2F1, pRB, pRBp}} \text{CycEi}$ |     |
| 19 | CycE.activation              | CycE activation         | $\text{CycEi} \xrightarrow{\text{CycEi, CycEa}} \text{CycEa}$ |     |
| 20 | CycE.inhibition              | CycE inhibition         | $\text{CycEa} \longrightarrow \text{CycEi}$                   |     |
| 21 | CycE-<br>_degradation        | CycE degradation        | $\text{CycEi} \longrightarrow \emptyset$                      |     |
| 22 | CycE-<br>_degradation2       | CycE degradation2       | $\text{CycEa} \longrightarrow \emptyset$                      |     |

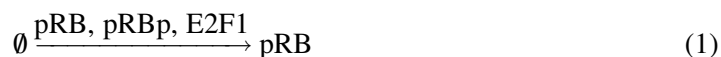


## 6.1 Reaction pRB\_synthesis

This is an irreversible reaction of no reactant forming one product influenced by three modifiers.

**Name** pRB synthesis

### Reaction equation



### Modifiers

Table 6: Properties of each modifier.

| Id   | Name | SBO |
|------|------|-----|
| pRB  | pRB  |     |
| pRBp | pRBp |     |
| E2F1 | E2F1 |     |

### Product

Table 7: Properties of each product.

| Id  | Name | SBO |
|-----|------|-----|
| pRB | pRB  |     |

### Kinetic Law

**Derived unit** contains undeclared units

$$v_1 = \text{vol}(\text{cell}) \cdot k_1 \cdot \frac{[\text{E2F1}]}{K_{m1} + [\text{E2F1}]} \cdot \frac{J_{11}}{J_{11} + [\text{pRB}]} \cdot \frac{J_{61}}{J_{61} + [\text{pRBp}]} \quad (2)$$

## 6.2 Reaction pRB\_phosphorylation

This is an irreversible reaction of one reactant forming one product influenced by two modifiers.

**Name** pRB phosphorylation

### Reaction equation



**Reactant**

Table 8: Properties of each reactant.

| Id  | Name | SBO |
|-----|------|-----|
| pRB | pRB  |     |

## Modifiers

Table 9: Properties of each modifier.

| Id    | Name           | SBO |
|-------|----------------|-----|
| pRB   | pRB            |     |
| CycDa | CycD/cdk4,6(a) |     |

## Product

Table 10: Properties of each product.

| Id   | Name | SBO |
|------|------|-----|
| pRBp | pRBp |     |

## Kinetic Law

**Derived unit** contains undeclared units

$$v_2 = \text{vol}(\text{cell}) \cdot k_{16} \cdot [\text{pRB}] \cdot [\text{CycDa}] \quad (4)$$

### 6.3 Reaction pRBp\_dephosphorylation

This is an irreversible reaction of one reactant forming one product.

**Name** pRBp dephosphorylation

#### Reaction equation



## Reactant

Table 11: Properties of each reactant.

| Id   | Name | SBO |
|------|------|-----|
| pRBp | pRBp |     |

## Product

Table 12: Properties of each product.

| Id  | Name | SBO |
|-----|------|-----|
| pRB | pRB  |     |

## Kinetic Law

**Derived unit** contains undeclared units

$$v_3 = \text{vol}(\text{cell}) \cdot k_{61} \cdot [\text{pRBp}] \quad (6)$$

### 6.4 Reaction pRB\_degradation

This is an irreversible reaction of one reactant forming no product.

**Name** pRB degradation

## Reaction equation



## Reactant

Table 13: Properties of each reactant.

| Id  | Name | SBO |
|-----|------|-----|
| pRB | pRB  |     |

## Kinetic Law

**Derived unit** contains undeclared units

$$v_4 = \text{vol}(\text{cell}) \cdot \text{phi\_pRB} \cdot [\text{pRB}] \quad (8)$$

### 6.5 Reaction E2F1\_synthesis

This is an irreversible reaction of no reactant forming one product influenced by three modifiers.

**Name** E2F1 synthesis

### Reaction equation



### Modifiers

Table 14: Properties of each modifier.

| Id   | Name | SBO |
|------|------|-----|
| E2F1 | E2F1 |     |
| pRB  | pRB  |     |
| pRBp | pRBp |     |

### Product

Table 15: Properties of each product.

| Id   | Name | SBO |
|------|------|-----|
| E2F1 | E2F1 |     |

### Kinetic Law

**Derived unit** contains undeclared units

$$v_5 = \text{vol}(\text{cell}) \cdot \left( k_p + \frac{k_2 \cdot (a^2 + [\text{E2F1}]^2)}{K m_2^2 + [\text{E2F1}]^2} \cdot \frac{J_{12}}{J_{12} + [\text{pRB}]} \cdot \frac{J_{62}}{J_{62} + [\text{pRBp}]} \right) \quad (10)$$

## 6.6 Reaction E2F1\_degradation

This is an irreversible reaction of one reactant forming no product.

**Name** E2F1 degradation

### Reaction equation



### Reactant

Table 16: Properties of each reactant.

| Id   | Name | SBO |
|------|------|-----|
| E2F1 | E2F1 |     |

### Kinetic Law

**Derived unit** contains undeclared units

$$v_6 = \text{vol}(\text{cell}) \cdot \text{phi\_E2F1} \cdot [\text{E2F1}] \quad (12)$$

## 6.7 Reaction CycD\_synthesis

This is an irreversible reaction of no reactant forming one product influenced by four modifiers.

**Name** CycD synthesis

### Reaction equation



### Modifiers

Table 17: Properties of each modifier.

| Id   | Name | SBO |
|------|------|-----|
| E2F1 | E2F1 |     |
| pRB  | pRB  |     |
| pRBp | pRBp |     |
| AP1  | AP1  |     |

### Product

Table 18: Properties of each product.

| Id    | Name           | SBO |
|-------|----------------|-----|
| CycDi | CycD/cdk4,6(i) |     |

### Kinetic Law

**Derived unit** contains undeclared units

$$v_7 = \text{vol}(\text{cell}) \cdot \left( k_3 \cdot [\text{AP1}] + k_{23} \cdot [\text{E2F1}] \cdot \frac{J_{13}}{J_{13} + [\text{pRB}]} \cdot \frac{J_{63}}{J_{63} + [\text{pRBp}]} \right) \quad (14)$$

## 6.8 Reaction `CycD_inibition`

This is an irreversible reaction of one reactant forming one product.

**Name** CycD inibition

### Reaction equation



### Reactant

Table 19: Properties of each reactant.

| Id    | Name           | SBO |
|-------|----------------|-----|
| CycDa | CycD/cdk4,6(a) |     |

### Product

Table 20: Properties of each product.

| Id    | Name           | SBO |
|-------|----------------|-----|
| CycDi | CycD/cdk4,6(i) |     |

### Kinetic Law

**Derived unit** contains undeclared units

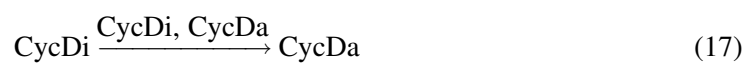
$$v_8 = \text{vol}(\text{cell}) \cdot k_{43} \cdot [\text{CycDa}] \quad (16)$$

## 6.9 Reaction `CycD_activation`

This is an irreversible reaction of one reactant forming one product influenced by two modifiers.

**Name** CycD activation

### Reaction equation



**Reactant**



Table 21: Properties of each reactant.

| Id    | Name           | SBO |
|-------|----------------|-----|
| CycDi | CycD/cdk4,6(i) |     |

## Modifiers

Table 22: Properties of each modifier.

| Id    | Name           | SBO |
|-------|----------------|-----|
| CycDi | CycD/cdk4,6(i) |     |
| CycDa | CycD/cdk4,6(a) |     |

## Product

Table 23: Properties of each product.

| Id    | Name           | SBO |
|-------|----------------|-----|
| CycDa | CycD/cdk4,6(a) |     |

## Kinetic Law

**Derived unit** contains undeclared units

$$v_9 = \text{vol}(\text{cell}) \cdot k_{34} \cdot [\text{CycDi}] \cdot \frac{[\text{CycDa}]}{K_{m4} + [\text{CycDa}]} \quad (18)$$

### 6.10 Reaction CycD\_degradation

This is an irreversible reaction of one reactant forming no product.

**Name** CycD degradation

#### Reaction equation



## Reactant

Table 24: Properties of each reactant.

| Id    | Name           | SBO |
|-------|----------------|-----|
| CycDi | CycD/cdk4,6(i) |     |

#### Kinetic Law

**Derived unit** contains undeclared units

$$v_{10} = \text{vol}(\text{cell}) \cdot \text{phi\_CycDi} \cdot [\text{CycDi}] \quad (20)$$

#### 6.11 Reaction CycD\_degradation2

This is an irreversible reaction of one reactant forming no product.

**Name** CycD degradation2

#### Reaction equation



#### Reactant

Table 25: Properties of each reactant.

| Id    | Name           | SBO |
|-------|----------------|-----|
| CycDa | CycD/cdk4,6(a) |     |

#### Kinetic Law

**Derived unit** contains undeclared units

$$v_{11} = \text{vol}(\text{cell}) \cdot \text{phi\_CycDa} \cdot [\text{CycDa}] \quad (22)$$

#### 6.12 Reaction AP1\_synthesis

This is an irreversible reaction of no reactant forming one product influenced by three modifiers.

**Name** AP1 synthesis

#### Reaction equation



## Modifiers

Table 26: Properties of each modifier.

| Id   | Name | SBO |
|------|------|-----|
| E2F1 | E2F1 |     |
| pRB  | pRB  |     |
| pRBp | pRBp |     |

## Product

Table 27: Properties of each product.

| Id  | Name | SBO |
|-----|------|-----|
| AP1 | AP1  |     |

## Kinetic Law

**Derived unit** contains undeclared units

$$v_{12} = \text{vol}(\text{cell}) \cdot \left( F_m + k_{25} \cdot [\text{E2F1}] \cdot \frac{J_{15}}{J_{15} + [\text{pRB}]} \cdot \frac{J_{65}}{J_{65} + [\text{pRBp}]} \right) \quad (24)$$

### 6.13 Reaction Ap1\_degradation

This is an irreversible reaction of one reactant forming no product.

**Name** Ap1 degradation

#### Reaction equation



## Reactant

Table 28: Properties of each reactant.

| Id  | Name | SBO |
|-----|------|-----|
| AP1 | AP1  |     |

## Kinetic Law

**Derived unit** contains undeclared units

$$v_{13} = \text{vol}(\text{cell}) \cdot \text{phi\_AP1} \cdot [\text{AP1}] \quad (26)$$

## 6.14 Reaction pRBp\_phosphorylation

This is an irreversible reaction of one reactant forming one product influenced by two modifiers.

**Name** pRBp phosphorylation

### Reaction equation



### Reactant

Table 29: Properties of each reactant.

| Id   | Name | SBO |
|------|------|-----|
| pRBp | pRBp |     |

### Modifiers

Table 30: Properties of each modifier.

| Id    | Name          | SBO |
|-------|---------------|-----|
| pRBp  | pRBp          |     |
| CycEa | CycEa/cdk2(a) |     |

### Product

Table 31: Properties of each product.

| Id    | Name  | SBO |
|-------|-------|-----|
| pRBpp | pRBpp |     |

## Kinetic Law

**Derived unit** contains undeclared units

$$v_{14} = \text{vol}(\text{cell}) \cdot k_{67} \cdot [\text{pRBp}] \cdot [\text{CycEa}] \quad (28)$$

### 6.15 Reaction pRBpp\_dephosphorylation

This is an irreversible reaction of one reactant forming one product.

**Name** pRBpp dephosphorylation

#### Reaction equation



#### Reactant

Table 32: Properties of each reactant.

| Id    | Name  | SBO |
|-------|-------|-----|
| pRBpp | pRBpp |     |

#### Product

Table 33: Properties of each product.

| Id   | Name | SBO |
|------|------|-----|
| pRBp | pRBp |     |

#### Kinetic Law

**Derived unit** contains undeclared units

$$v_{15} = \text{vol}(\text{cell}) \cdot k_{76} \cdot [\text{pRBpp}] \quad (30)$$

### 6.16 Reaction pRBpp\_degradation

This is an irreversible reaction of one reactant forming no product.

**Name** pRBpp degradation

#### Reaction equation



#### Reactant

Table 34: Properties of each reactant.

| Id    | Name  | SBO |
|-------|-------|-----|
| pRBpp | pRBpp |     |

### Kinetic Law

**Derived unit** contains undeclared units

$$v_{16} = \text{vol}(\text{cell}) \cdot \text{phi\_pRBpp} \cdot [\text{pRBpp}] \quad (32)$$

### 6.17 Reaction pRBp\_degradation

This is an irreversible reaction of one reactant forming no product.

**Name** pRBp degradation

### Reaction equation



### Reactant

Table 35: Properties of each reactant.

| Id   | Name | SBO |
|------|------|-----|
| pRBp | pRBp |     |

### Kinetic Law

**Derived unit** contains undeclared units

$$v_{17} = \text{vol}(\text{cell}) \cdot \text{phi\_pRBp} \cdot [\text{pRBp}] \quad (34)$$

### 6.18 Reaction CycE\_synthesis

This is an irreversible reaction of no reactant forming one product influenced by three modifiers.

**Name** CycE synthesis

### Reaction equation



## Modifiers

Table 36: Properties of each modifier.

| Id   | Name | SBO |
|------|------|-----|
| E2F1 | E2F1 |     |
| pRB  | pRB  |     |
| pRBp | pRBp |     |

## Product

Table 37: Properties of each product.

| Id    | Name         | SBO |
|-------|--------------|-----|
| CycEi | CycE/cdk2(i) |     |

## Kinetic Law

**Derived unit** contains undeclared units

$$v_{18} = \text{vol}(\text{cell}) \cdot k_{28} \cdot [\text{E2F1}] \cdot \frac{J_{18}}{J_{18} + [\text{pRB}]} \cdot \frac{J_{68}}{J_{68} + [\text{pRBp}]} \quad (36)$$

### 6.19 Reaction CycE\_activation

This is an irreversible reaction of one reactant forming one product influenced by two modifiers.

**Name** CycE activation

#### Reaction equation



## Reactant

Table 38: Properties of each reactant.

| Id    | Name         | SBO |
|-------|--------------|-----|
| CycEi | CycE/cdk2(i) |     |

## Modifiers

Table 39: Properties of each modifier.

| Id    | Name          | SBO |
|-------|---------------|-----|
| CycEi | CycE/cdk2(i)  |     |
| CycEa | CycEa/cdk2(a) |     |

## Product

Table 40: Properties of each product.

| Id    | Name          | SBO |
|-------|---------------|-----|
| CycEa | CycEa/cdk2(a) |     |

## Kinetic Law

**Derived unit** contains undeclared units

$$v_{19} = \frac{\text{vol}(\text{cell}) \cdot k_{89} \cdot [\text{CycEi}] \cdot [\text{CycEa}]}{K_{m9} + [\text{CycEa}]} \quad (38)$$

## 6.20 Reaction CycE\_inhibition

This is an irreversible reaction of one reactant forming one product.

**Name** CycE inibition

## Reaction equation



## Reactant

Table 41: Properties of each reactant.

| Id    | Name          | SBO |
|-------|---------------|-----|
| CycEa | CycEa/cdk2(a) |     |

## Product



Table 42: Properties of each product.

| Id    | Name         | SBO |
|-------|--------------|-----|
| CycEi | CycE/cdk2(i) |     |

### Kinetic Law

**Derived unit** contains undeclared units

$$v_{20} = \text{vol}(\text{cell}) \cdot k_{98} \cdot [\text{CycEa}] \quad (40)$$

### 6.21 Reaction CycE\_degradation

This is an irreversible reaction of one reactant forming no product.

**Name** CycE degradation

### Reaction equation



### Reactant

Table 43: Properties of each reactant.

| Id    | Name         | SBO |
|-------|--------------|-----|
| CycEi | CycE/cdk2(i) |     |

### Kinetic Law

**Derived unit** contains undeclared units

$$v_{21} = \text{vol}(\text{cell}) \cdot \text{phi\_CycEi} \cdot [\text{CycEi}] \quad (42)$$

### 6.22 Reaction CycE\_degradation2

This is an irreversible reaction of one reactant forming no product.

**Name** CycE degradation2

### Reaction equation



**Reactant**

Table 44: Properties of each reactant.

| Id    | Name          | SBO |
|-------|---------------|-----|
| CycEa | CycEa/cdk2(a) |     |

## Kinetic Law

**Derived unit** contains undeclared units

$$v_{22} = \text{vol}(\text{cell}) \cdot \text{phi\_CycEa} \cdot [\text{CycEa}] \quad (44)$$

## 7 Derived Rate Equations

When interpreted as an ordinary differential equation framework, this model implies the following set of equations for the rates of change of each species.

Identifiers for kinetic laws highlighted in gray cannot be verified to evaluate to units of SBML substance per time. As a result, some SBML interpreters may not be able to verify the consistency of the units on quantities in the model. Please check if

- parameters without an unit definition are involved or
- volume correction is necessary because the `hasOnlySubstanceUnits` flag may be set to `false` and `spacialDimensions` > 0 for certain species.

### 7.1 Species pRB

**Name** pRB

**Notes** retinoblastoma tumor suppressor protein

**Initial concentration** 0.1 dimensionless · dimensionless<sup>-1</sup>

This species takes part in ten reactions (as a reactant in [pRB\\_phosphorylation](#), [pRB\\_degradation](#) and as a product in [pRB\\_synthesis](#), [pRBp\\_dephosphorylation](#) and as a modifier in [pRB\\_synthesis](#), [pRB\\_phosphorylation](#), [E2F1\\_synthesis](#), [CycD\\_synthesis](#), [AP1\\_synthesis](#), [CycE\\_synthesis](#)).

$$\frac{d}{dt} \text{pRB} = v_1 + v_3 - v_2 - v_4 \quad (45)$$

### 7.2 Species pRBp

**Name** pRBp

**Notes** monophosphorlyated pRB

**Initial concentration** 0.1 dimensionless · dimensionless<sup>-1</sup>

This species takes part in eleven reactions (as a reactant in [pRBp\\_dephosphorylation](#), [pRBp\\_phosphorylation](#), [pRBp\\_degradation](#) and as a product in [pRB\\_phosphorylation](#), [pRBpp\\_dephosphorylation](#) and as a modifier in [pRB\\_synthesis](#), [E2F1\\_synthesis](#), [CycD\\_synthesis](#), [AP1\\_synthesis](#), [pRBp\\_phosphorylation](#), [CycE\\_synthesis](#)).

$$\frac{d}{dt} \text{pRBp} = v_2 + v_{15} - v_3 - v_{14} - v_{17} \quad (46)$$

### 7.3 Species E2F1

**Name** E2F1

**Notes** dimers of E2F1-6 and DP1,2

**Initial concentration** 0.1 dimensionless · dimensionless<sup>-1</sup>

This species takes part in seven reactions (as a reactant in [E2F1\\_degradation](#) and as a product in [E2F1\\_synthesis](#) and as a modifier in [pRB\\_synthesis](#), [E2F1\\_synthesis](#), [CycD\\_synthesis](#), [AP1\\_synthesis](#), [CycE\\_synthesis](#)).

$$\frac{d}{dt} \text{E2F1} = v_5 - v_6 \quad (47)$$

### 7.4 Species CycDi

**Name** CycD/cdk4,6(i)

**Initial concentration** 0.1 dimensionless · dimensionless<sup>-1</sup>

This species takes part in five reactions (as a reactant in [CycD\\_activation](#), [CycD\\_degradation](#) and as a product in [CycD\\_synthesis](#), [CycD\\_inhibition](#) and as a modifier in [CycD\\_activation](#)).

$$\frac{d}{dt} \text{CycDi} = v_7 + v_8 - v_9 - v_{10} \quad (48)$$

### 7.5 Species CycDa

**Name** CycD/cdk4,6(a)

**Initial concentration** 0.1 dimensionless · dimensionless<sup>-1</sup>

This species takes part in five reactions (as a reactant in [CycD\\_inhibition](#), [CycD\\_degradation2](#) and as a product in [CycD\\_activation](#) and as a modifier in [pRB\\_phosphorylation](#), [CycD\\_activation](#)).

$$\frac{d}{dt} \text{CycDa} = v_9 - v_8 - v_{11} \quad (49)$$

## 7.6 Species AP1

**Name** AP1

**Notes** c-Jun/Fos dimers

**Initial concentration**  $0.1 \text{ dimensionless} \cdot \text{dimensionless}^{-1}$

This species takes part in three reactions (as a reactant in [Ap1\\_degradation](#) and as a product in [AP1\\_synthesis](#) and as a modifier in [CycD\\_synthesis](#)).

$$\frac{d}{dt} \text{AP1} = v_{12} - v_{13} \quad (50)$$

## 7.7 Species pRBpp

**Name** pRBpp

**Notes** diphosphorylated form of pRB

**Initial concentration**  $0.1 \text{ dimensionless} \cdot \text{dimensionless}^{-1}$

This species takes part in three reactions (as a reactant in [pRBpp\\_dephosphorylation](#), [pRBpp\\_degradation](#) and as a product in [pRBp\\_phosphorylation](#)).

$$\frac{d}{dt} \text{pRBpp} = v_{14} - v_{15} - v_{16} \quad (51)$$

## 7.8 Species CycEi

**Name** CycE/cdk2(i)

**Initial concentration**  $0.1 \text{ dimensionless} \cdot \text{dimensionless}^{-1}$

This species takes part in five reactions (as a reactant in [CycE\\_activation](#), [CycE\\_degradation](#) and as a product in [CycE\\_synthesis](#), [CycE\\_inhibition](#) and as a modifier in [CycE\\_activation](#)).

$$\frac{d}{dt} \text{CycEi} = v_{18} + v_{20} - v_{19} - v_{21} \quad (52)$$

## 7.9 Species CycEa

**Name** CycEa/cdk2(a)

**Initial concentration**  $0.1 \text{ dimensionless} \cdot \text{dimensionless}^{-1}$

This species takes part in five reactions (as a reactant in [CycE\\_inhibition](#), [CycE\\_degradation2](#) and as a product in [CycE\\_activation](#) and as a modifier in [pRBp\\_phosphorylation](#), [CycE\\_activation](#)).

$$\frac{d}{dt} \text{CycEa} = v_{19} - v_{20} - v_{22} \quad (53)$$

SBML<sup>2</sup>TeX was developed by Andreas Dräger<sup>a</sup>, Hannes Planatscher<sup>a</sup>, Dieudonné M Wouamba<sup>a</sup>, Adrian Schröder<sup>a</sup>, Michael Hucka<sup>b</sup>, Lukas Endler<sup>c</sup>, Martin Golebiewski<sup>d</sup> and Andreas Zell<sup>a</sup>. Please see <http://www.ra.cs.uni-tuebingen.de/software/SBML2LaTeX> for more information.

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