

## SBML Model Report

**Model name: “Vilar2002\_Oscillator”**



May 6, 2016

### 1 General Overview

This is a document in SBML Level 2 Version 3 format. This model was created by the following two authors: Nicolas Le Novre<sup>1</sup> and Bruce Shapiro<sup>2</sup> at June 30<sup>th</sup> 2005 at 10:20 a. m. and last time modified at June third 2013 at 1:58 p. m. Table 1 provides an overview of the quantities of all components of this model.

Table 1: Number of components in this model, which are described in the following sections.

Element	Quantity	Element	Quantity
compartment types	0	compartments	1
species types	0	species	10
events	0	constraints	0
reactions	16	function definitions	0
global parameters	0	unit definitions	1
rules	0	initial assignments	0

### Model Notes

**Minimal Model for Circadian Oscillations**  
**Minimal Model for Circadian Oscillations**

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**Citation**

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<sup>1</sup>EMBL-EBI, [lenov@ebi.ac.uk](mailto:lenov@ebi.ac.uk)

<sup>2</sup>Jet Propulsion Laboratory, [bshapiro@caltech.edu](mailto:bshapiro@caltech.edu)

Vilar JMG, Kueh HY, Barkai N, Leibler S, (2002). Mechanisms of noise resistance in genetic oscillators, PNAS, 99(9):5988-5992. <http://www.pnas.org/cgi/content/abstract/99/9/5988>

### Description

A minimal model of genomically based oscillation, based on two mutually interacting genes, an activator and a repressor. Postive feedback is provided by the activator protein, which binds to the promoters of both the activator and the repressor genes. Negative feedback is provided by the repressor protein which binds to the activator protein.

Rateconstant	Reaction
alphaA=50	DA->DA+MA
alphaAp=500	DAP->DAP+MA
alphaR=0.01	DR->DR+MR
alphaRp=50	DRp->DRp+MR
betaA=50	MA->A+MA
betaR=5	MR->MR+R
gammaA=1	A+DA->DAP
gammaC=2	A+R->C
gammaR=1	A+DR->DRp
deltaA=1	A->EmptySet
deltaA=1	C->R
deltaMA=10	MA->EmptySet
deltaMR=0.5	MR->EmptySet
deltaR=0.2	R->EmptySet
thetaA=50	DAP->A+DA
thetaR=100	DRp->A+DR

Variable	IC	ODE
A	0	$A'[t] = -(\delta A \cdot A[t]) - \gamma A \cdot A[t] \cdot DA[t] + \theta A \cdot DAP[t] - \gamma R \cdot A[t] \cdot DR[t] + \theta R \cdot DRp[t] + \beta A \cdot MA[t] - \gamma C \cdot A[t] \cdot R[t]$
C	0	$C'[t] = -(\delta A \cdot C[t]) + \gamma C \cdot A[t] \cdot R[t]$
DA	1	$DA'[t] = -(\gamma A \cdot A[t] \cdot DA[t]) + \theta A \cdot DAP[t]$

D <sub>Ap</sub>	0	$D_{Ap}'[t] = \gamma A[t] \cdot D_A[t] - \theta A \cdot D_{Ap}[t]$
D <sub>R</sub>	1	$D_R'[t] = -(\gamma R \cdot A[t] \cdot D_R[t]) + \theta R \cdot D_{Rp}[t]$
D <sub>Rp</sub>	0	$D_{Rp}'[t] = \gamma R \cdot A[t] \cdot D_R[t] - \theta R \cdot D_{Rp}[t]$
M <sub>A</sub>	0	$M_A'[t] = \alpha A \cdot D_A[t] + \alpha_{Ap} \cdot D_{Ap}[t] - \delta M_A \cdot M_A[t]$
M <sub>R</sub>	0	$M_R'[t] = \alpha R \cdot D_R[t] + \alpha_{Rp} \cdot D_{Rp}[t] - \delta M_R \cdot M_R[t]$
R	0	$R'[t] = \delta A \cdot C[t] + \beta R \cdot M_R[t] - \delta R \cdot R[t] - \gamma C \cdot A[t] \cdot R[t]$

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Generated by Cellerator Version 1.0 update 2.1127 using Mathematica 4.2 for Mac OS X (June 4, 2002), November 27, 2002 12:17:46, using (PowerMac,PowerPC,Mac OS X,MacOSX,Darwin)

author=B.E.Shapiro

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## 2 Unit Definitions

This is an overview of five unit definitions of which four are predefined by SBML and not mentioned in the model.

### 2.1 Unit `time`

Name `hour`

Definition 3600 s

### 2.2 Unit `substance`

Notes Mole is the predefined SBML unit for `substance`.

Definition `mol`

### 2.3 Unit `volume`

**Notes** Litre is the predefined SBML unit for `volume`.

**Definition** 1

### 2.4 Unit `area`

**Notes** Square metre is the predefined SBML unit for `area` since SBML Level 2 Version 1.

**Definition**  $\text{m}^2$

### 2.5 Unit `length`

**Notes** Metre is the predefined SBML unit for `length` since SBML Level 2 Version 1.

**Definition**  $\text{m}$

## 3 Compartment

This model contains one compartment.

Table 6: Properties of all compartments.

Id	Name	SBO	Spatial Dimensions	Size	Unit	Constant	Outside
deterministicOscillator			3	1	litre	<input checked="" type="checkbox"/>	

#### 3.1 Compartment `deterministicOscillator`

This is a three dimensional compartment with a constant size of one litre.

## 4 Species

This model contains ten species. The boundary condition of one of these species is set to `true` so that this species' amount cannot be changed by any reaction. Section 6 provides further details and the derived rates of change of each species.

Table 7: Properties of each species.

Id	Name	Compartment	Derived Unit	Constant	Boundary Condition
EmptySet		deterministicOscillator	mol	<input type="checkbox"/>	<input checked="" type="checkbox"/>
A		deterministicOscillator	mol	<input type="checkbox"/>	<input type="checkbox"/>
C		deterministicOscillator	mol	<input type="checkbox"/>	<input type="checkbox"/>
DA		deterministicOscillator	mol	<input type="checkbox"/>	<input type="checkbox"/>
DAp		deterministicOscillator	mol	<input type="checkbox"/>	<input type="checkbox"/>
DR		deterministicOscillator	mol	<input type="checkbox"/>	<input type="checkbox"/>
DRp		deterministicOscillator	mol	<input type="checkbox"/>	<input type="checkbox"/>
MA		deterministicOscillator	mol	<input type="checkbox"/>	<input type="checkbox"/>
MR		deterministicOscillator	mol	<input type="checkbox"/>	<input type="checkbox"/>
R		deterministicOscillator	mol	<input type="checkbox"/>	<input type="checkbox"/>

## 5 Reactions

This model contains 16 reactions. All reactions are listed in the following table and are subsequently described in detail. If a reaction is affected by a modifier, the identifier of this species is written above the reaction arrow.

Table 8: Overview of all reactions

Nº	Id	Name	Reaction Equation	SBO
1	Reaction1		$A + R \longrightarrow C$	
2	Reaction2		$A \longrightarrow \text{EmptySet}$	
3	Reaction3		$C \longrightarrow R$	
4	Reaction4		$R \longrightarrow \text{EmptySet}$	
5	Reaction5		$A + DA \longrightarrow DAp$	
6	Reaction6		$DAp \longrightarrow A + DA$	
7	Reaction7		$DA \longrightarrow DA + MA$	
8	Reaction8		$DAp \longrightarrow DAp + MA$	
9	Reaction9		$MA \longrightarrow \text{EmptySet}$	
10	Reaction10		$MA \longrightarrow A + MA$	
11	Reaction11		$A + DR \longrightarrow DRp$	
12	Reaction12		$DRp \longrightarrow A + DR$	
13	Reaction13		$DR \longrightarrow DR + MR$	
14	Reaction14		$DRp \longrightarrow DRp + MR$	
15	Reaction15		$MR \longrightarrow \text{EmptySet}$	
16	Reaction16		$MR \longrightarrow MR + R$	

## 5.1 Reaction Reaction1

This is an irreversible reaction of two reactants forming one product.

### Reaction equation



### Reactants

Table 9: Properties of each reactant.

Id	Name	SBO
A		
R		

### Product

Table 10: Properties of each product.

Id	Name	SBO
C		

### Kinetic Law

Derived unit contains undeclared units

$$v_1 = A \cdot R \cdot \text{gammaC} \quad (2)$$

Table 11: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
gammaC			2.0		<input checked="" type="checkbox"/>

## 5.2 Reaction Reaction2

This is an irreversible reaction of one reactant forming one product.

### Reaction equation



### Reactant

Table 12: Properties of each reactant.

Id	Name	SBO
A		

### Product

Table 13: Properties of each product.

Id	Name	SBO
EmptySet		

### Kinetic Law

Derived unit contains undeclared units

$$v_2 = A \cdot \text{deltaA} \quad (4)$$

Table 14: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
deltaA			1.0		<input checked="" type="checkbox"/>

## 5.3 Reaction `Reaction3`

This is an irreversible reaction of one reactant forming one product.

### Reaction equation



### Reactant



Table 15: Properties of each reactant.

Id	Name	SBO
C		

## Product

Table 16: Properties of each product.

Id	Name	SBO
R		

## Kinetic Law

Derived unit contains undeclared units

$$v_3 = C \cdot \text{deltaA} \quad (6)$$

Table 17: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
deltaA			1.0		<input checked="" type="checkbox"/>

## 5.4 Reaction `Reaction4`

This is an irreversible reaction of one reactant forming one product.

## Reaction equation



## Reactant

Table 18: Properties of each reactant.

Id	Name	SBO
R		

## Product

Table 19: Properties of each product.

Id	Name	SBO
	EmptySet	

### Kinetic Law

Derived unit contains undeclared units

$$v_4 = R \cdot \text{deltaR} \quad (8)$$

Table 20: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
	deltaR		0.2		<input checked="" type="checkbox"/>

### 5.5 Reaction `Reaction5`

This is an irreversible reaction of two reactants forming one product.

#### Reaction equation



#### Reactants

Table 21: Properties of each reactant.

Id	Name	SBO
	A	
	DA	

#### Product

Table 22: Properties of each product.

Id	Name	SBO
	DAp	

## Kinetic Law

Derived unit contains undeclared units

$$v_5 = A \cdot DA \cdot \text{gammaA} \quad (10)$$

Table 23: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
gammaA			1.0		<input checked="" type="checkbox"/>

## 5.6 Reaction [Reaction6](#)

This is an irreversible reaction of one reactant forming two products.

### Reaction equation



### Reactant

Table 24: Properties of each reactant.

Id	Name	SBO
DAp		

### Products

Table 25: Properties of each product.

Id	Name	SBO
A		
DA		

## Kinetic Law

Derived unit contains undeclared units

$$v_6 = DAp \cdot \text{thetaA} \quad (12)$$

Table 26: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
thetaA			50.0		<input checked="" type="checkbox"/>

## 5.7 Reaction Reaction7

This is an irreversible reaction of one reactant forming two products.

### Reaction equation



### Reactant

Table 27: Properties of each reactant.

Id	Name	SBO
	DA	

### Products

Table 28: Properties of each product.

Id	Name	SBO
	DA	
	MA	

### Kinetic Law

Derived unit contains undeclared units

$$v_7 = DA \cdot \text{alphaA} \quad (14)$$

Table 29: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
alphaA			50.0		<input checked="" type="checkbox"/>

## 5.8 Reaction Reaction8

This is an irreversible reaction of one reactant forming two products.

### Reaction equation



### Reactant

Table 30: Properties of each reactant.

Id	Name	SBO
DAp		

### Products

Table 31: Properties of each product.

Id	Name	SBO
DAp		
MA		

### Kinetic Law

Derived unit contains undeclared units

$$v_8 = \text{DAp} \cdot \text{alphaAp} \quad (16)$$

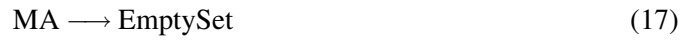
Table 32: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
alphaAp			500.0		<input checked="" type="checkbox"/>

## 5.9 Reaction Reaction9

This is an irreversible reaction of one reactant forming one product.

### Reaction equation



### Reactant

Table 33: Properties of each reactant.

Id	Name	SBO
	MA	

### Product

Table 34: Properties of each product.

Id	Name	SBO
	EmptySet	

### Kinetic Law

Derived unit contains undeclared units

$$v_9 = \text{MA} \cdot \text{deltaMA} \quad (18)$$

Table 35: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
	deltaMA		10.0		<input checked="" type="checkbox"/>

## 5.10 Reaction `Reaction10`

This is an irreversible reaction of one reactant forming two products.

### Reaction equation



### Reactant

Table 36: Properties of each reactant.

Id	Name	SBO
	MA	

## Products

Table 37: Properties of each product.

Id	Name	SBO
	A	
	MA	

## Kinetic Law

Derived unit contains undeclared units

$$v_{10} = \text{MA} \cdot \text{betaA} \quad (20)$$

Table 38: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
	betaA		50.0		<input checked="" type="checkbox"/>

## 5.11 Reaction `Reaction11`

This is an irreversible reaction of two reactants forming one product.

### Reaction equation



## Reactants

Table 39: Properties of each reactant.

Id	Name	SBO
	A	
	DR	

## Product

Table 40: Properties of each product.

Id	Name	SBO
DRp		

## Kinetic Law

Derived unit contains undeclared units

$$v_{11} = A \cdot DR \cdot \text{gammaR} \quad (22)$$

Table 41: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
gammaR			1.0		<input checked="" type="checkbox"/>

## 5.12 Reaction `Reaction12`

This is an irreversible reaction of one reactant forming two products.

### Reaction equation



## Reactant

Table 42: Properties of each reactant.

Id	Name	SBO
DRp		

## Products

Table 43: Properties of each product.

Id	Name	SBO
A		
DR		



Id	Name	SBO
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### Kinetic Law

Derived unit contains undeclared units

$$v_{12} = \text{DRp} \cdot \text{thetaR} \quad (24)$$

Table 44: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
thetaR			100.0		<input checked="" type="checkbox"/>

### 5.13 Reaction `Reaction13`

This is an irreversible reaction of one reactant forming two products.

#### Reaction equation



#### Reactant

Table 45: Properties of each reactant.

Id	Name	SBO
DR		

#### Products

Table 46: Properties of each product.

Id	Name	SBO
DR		
MR		

### Kinetic Law

Derived unit contains undeclared units

$$v_{13} = DR \cdot \text{alphaR} \quad (26)$$

Table 47: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
alphaR			0.01		<input checked="" type="checkbox"/>

#### 5.14 Reaction [Reaction14](#)

This is an irreversible reaction of one reactant forming two products.

##### Reaction equation



##### Reactant

Table 48: Properties of each reactant.

Id	Name	SBO
DRp		

##### Products

Table 49: Properties of each product.

Id	Name	SBO
DRp		
MR		

##### Kinetic Law

Derived unit contains undeclared units

$$v_{14} = DRp \cdot \text{alphaRp} \quad (28)$$

Table 50: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
alphaRp			50.0		<input checked="" type="checkbox"/>

### 5.15 Reaction [Reaction15](#)

This is an irreversible reaction of one reactant forming one product.

#### Reaction equation



#### Reactant

Table 51: Properties of each reactant.

Id	Name	SBO
MR		

#### Product

Table 52: Properties of each product.

Id	Name	SBO
EmptySet		

#### Kinetic Law

Derived unit contains undeclared units

$$v_{15} = \text{MR} \cdot \text{deltaMR} \quad (30)$$

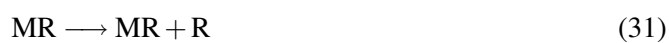
Table 53: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
deltaMR			0.5		<input checked="" type="checkbox"/>

### 5.16 Reaction [Reaction16](#)

This is an irreversible reaction of one reactant forming two products.

#### Reaction equation



## Reactant

Table 54: Properties of each reactant.

Id	Name	SBO
MR		

## Products

Table 55: Properties of each product.

Id	Name	SBO
MR		
R		

## Kinetic Law

Derived unit contains undeclared units

$$v_{16} = \text{MR} \cdot \text{betaR} \quad (32)$$

Table 56: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
betaR			5.0		<input checked="" type="checkbox"/>

## 6 Derived Rate Equations

When interpreted as an ordinary differential equation framework, this model implies the following set of equations for the rates of change of each species.

Identifiers for kinetic laws highlighted in gray cannot be verified to evaluate to units of SBML `substance` per time. As a result, some SBML interpreters may not be able to verify the consistency of the units on quantities in the model. Please check if

- parameters without an unit definition are involved or
- volume correction is necessary because the `hasOnlySubstanceUnits` flag may be set to `false` and `spacialDimensions > 0` for certain species.

## 6.1 Species EmptySet

Initial amount 0 mol

This species takes part in four reactions (as a product in [Reaction2](#), [Reaction4](#), [Reaction9](#), [Reaction15](#)), which do not influence its rate of change because this species is on the boundary of the reaction system:

$$\frac{d}{dt}\text{EmptySet} = 0 \quad (33)$$

## 6.2 Species A

Initial amount 0 mol

This species takes part in seven reactions (as a reactant in [Reaction1](#), [Reaction2](#), [Reaction5](#), [Reaction11](#) and as a product in [Reaction6](#), [Reaction10](#), [Reaction12](#)).

$$\frac{d}{dt}A = v_6 + v_{10} + v_{12} - v_1 - v_2 - v_5 - v_{11} \quad (34)$$

## 6.3 Species C

Initial amount 0 mol

This species takes part in two reactions (as a reactant in [Reaction3](#) and as a product in [Reaction1](#)).

$$\frac{d}{dt}C = v_1 - v_3 \quad (35)$$

## 6.4 Species DA

Initial amount 1 mol

This species takes part in four reactions (as a reactant in [Reaction5](#), [Reaction7](#) and as a product in [Reaction6](#), [Reaction7](#)).

$$\frac{d}{dt}DA = v_6 + v_7 - v_5 - v_7 \quad (36)$$

## 6.5 Species DAp

Initial amount 0 mol

This species takes part in four reactions (as a reactant in [Reaction6](#), [Reaction8](#) and as a product in [Reaction5](#), [Reaction8](#)).

$$\frac{d}{dt}DAp = v_5 + v_8 - v_6 - v_8 \quad (37)$$

## 6.6 Species DR

Initial amount 1 mol

This species takes part in four reactions (as a reactant in [Reaction11](#), [Reaction13](#) and as a product in [Reaction12](#), [Reaction13](#)).

$$\frac{d}{dt}DR = v_{12} + v_{13} - v_{11} - v_{13} \quad (38)$$

## 6.7 Species DRp

Initial amount 0 mol

This species takes part in four reactions (as a reactant in [Reaction12](#), [Reaction14](#) and as a product in [Reaction11](#), [Reaction14](#)).

$$\frac{d}{dt}DRp = v_{11} + v_{14} - v_{12} - v_{14} \quad (39)$$

## 6.8 Species MA

Initial amount 0 mol

This species takes part in five reactions (as a reactant in [Reaction9](#), [Reaction10](#) and as a product in [Reaction7](#), [Reaction8](#), [Reaction10](#)).

$$\frac{d}{dt}MA = v_7 + v_8 + v_{10} - v_9 - v_{10} \quad (40)$$

## 6.9 Species MR

Initial amount 0 mol

This species takes part in five reactions (as a reactant in [Reaction15](#), [Reaction16](#) and as a product in [Reaction13](#), [Reaction14](#), [Reaction16](#)).

$$\frac{d}{dt}MR = v_{13} + v_{14} + v_{16} - v_{15} - v_{16} \quad (41)$$

## 6.10 Species R

Initial amount 0 mol

This species takes part in four reactions (as a reactant in [Reaction1](#), [Reaction4](#) and as a product in [Reaction3](#), [Reaction16](#)).

$$\frac{d}{dt}R = v_3 + v_{16} - v_1 - v_4 \quad (42)$$

SBML<sup>2</sup>LaTeX was developed by Andreas Dräger<sup>a</sup>, Hannes Planatscher<sup>a</sup>, Dieudonné M Wouamba<sup>a</sup>, Adrian Schröder<sup>a</sup>, Michael Hucka<sup>b</sup>, Lukas Endler<sup>c</sup>, Martin Golebiewski<sup>d</sup> and Andreas Zell<sup>a</sup>. Please see <http://www.ra.cs.uni-tuebingen.de/software/SBML2LaTeX> for more information.

<sup>a</sup>Center for Bioinformatics Tübingen (ZBIT), Germany

<sup>b</sup>California Institute of Technology, Beckman Institute BNMC, Pasadena, United States

<sup>c</sup>European Bioinformatics Institute, Wellcome Trust Genome Campus, Hinxton, United Kingdom

<sup>d</sup>EML Research gGmbH, Heidelberg, Germany