## **SBML Model Report**

# Model name: "Chickarmane2006 - Stem cell switch reversible"



May 6, 2016

#### 1 General Overview

This is a document in SBML Level 2 Version 3 format. This model was created by the following four authors: Lukas Endler<sup>1</sup>, Vijayalakshmi Chelliah<sup>2</sup>, Carsten Peterson<sup>3</sup> and Vijay Chickarmane<sup>4</sup> at November 25<sup>th</sup> 2008 at 5:19 p. m. and last time modified at June fifth 2013 at 4:59 p. m. Table 1 gives an overview of the quantities of all components of this model.

Table 1: Number of components in this model, which are described in the following sections.

Element	Quantity	Element	Quantity
compartment types	0	compartments	1
species types	0	species	12
events	0	constraints	0
reactions	10	function definitions	0
global parameters	32	unit definitions	3
rules	0	initial assignments	0

#### **Model Notes**

Chickarmane2006 - Stem cell switch reversible

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Kinetic modeling approach of the transcriptional dynamics of the embryonic stem cell switch. This model is described in the article: Transcriptional dynamics of the embryonic stem cell switch. Chickarmane V, Troein C, Nuber UA, Sauro HM, Peterson CPLoS Computational Biology. 2006; 2(9):e123

Abstract:

Recent ChIP experiments of human and mouse embryonic stem cells have elucidated the architecture of the transcriptional regulatory circuitry responsible for cell determination, which involves the transcription factors OCT4, SOX2, and NANOG. In addition to regulating each other through feedback loops, these genes also regulate downstream target genes involved in the maintenance and differentiation of embryonic stem cells. A search for the OCT4-SOX2-NANOG network motif in other species reveals that it is unique to mammals. With a kinetic modeling approach, we ascribe function to the observed OCT4-SOX2-NANOG network by making plausible assumptions about the interactions between the transcription factors at the gene promoter binding sites and RNA polymerase (RNAP), at each of the three genes as well as at the target genes. We identify a bistable switch in the network, which arises due to several positive feedback loops, and is switched on/off by input environmental signals. The switch stabilizes the expression levels of the three genes, and through their regulatory roles on the downstream target genes, leads to a binary decision: when OCT4, SOX2, and NANOG are expressed and the switch is on, the self-renewal genes are on and the differentiation genes are off. The opposite holds when the switch is off. The model is extremely robust to parameter changes. In addition to providing a self-consistent picture of the transcriptional circuit, the model generates several predictions. Increasing the binding strength of NANOG to OCT4 and SOX2, or increasing its basal transcriptional rate, leads to an irreversible bistable switch: the switch remains on even when the activating signal is removed. Hence, the stem cell can be manipulated to be selfrenewing without the requirement of input signals. We also suggest tests that could discriminate between a variety of feedforward regulation architectures of the target genes by OCT4, SOX2, and NANOG.

This model is hosted on BioModels Database and identified by: MODEL7957907314.

To cite BioModels Database, please use: BioModels Database: An enhanced, curated and annotated resource for published quantitative kinetic models.

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#### 2 Unit Definitions

This is an overview of five unit definitions of which two are predefined by SBML and not mentioned in the model.

#### 2.1 Unit substance

Name arb\_substance

**Definition** dimensionless

#### 2.2 Unit volume

Name arb\_volume

**Definition** 1

#### 2.3 Unit time

Name arb\_time

**Definition** dimensionless

#### 2.4 Unit area

Notes Square metre is the predefined SBML unit for area since SBML Level 2 Version 1.

**Definition**  $m^2$ 

#### 2.5 Unit length

**Notes** Metre is the predefined SBML unit for length since SBML Level 2 Version 1.

**Definition** m

### 3 Compartment

This model contains one compartment.

Table 2: Properties of all compartments.

Id	Name	SBO	Spatial Dimensions	Size	Unit	Constant	Outside
compartment			3	1	litre	Ø	

#### 3.1 Compartment compartment

This is a three dimensional compartment with a constant size of one litre.

# 4 Species

This model contains twelve species. The boundary condition of seven of these species is set to true so that these species' amount cannot be changed by any reaction. Section 7 provides further details and the derived rates of change of each species.

Table 3: Properties of each species.

Id	Name	Compartment	Derived Unit	Constant	Boundary Condi- tion
OCT4_Gene		compartment	dimensionless $\cdot 1^{-1}$		$\overline{Z}$
${\tt NANOG\_Gene}$		compartment	dimensionless $\cdot 1^{-1}$		
$SOX2\_Gene$		compartment	dimensionless $\cdot 1^{-1}$	$\Box$	
targetGene		compartment	dimensionless $\cdot 1^{-1}$		
degradation		compartment	dimensionless $\cdot 1^{-1}$		
p53		compartment	dimensionless $\cdot 1^{-1}$		
A		compartment	dimensionless $\cdot 1^{-1}$		
OCT4		compartment	dimensionless $\cdot 1^{-1}$		
SOX2		compartment	dimensionless $\cdot 1^{-1}$		
NANOG		compartment	dimensionless $\cdot 1^{-1}$		
OCT4_SOX2		compartment	dimensionless $\cdot 1^{-1}$	$\Box$	
Protein		compartment	dimensionless $\cdot 1^{-1}$	$\Box$	

# **5 Parameters**

This model contains 32 global parameters.

Table 4: Properties of each parameter.

Id	Name	SBO Value Uni	t Constant
eta1	eta1	$10^{-4}$	
a1	a1	1.000	$\overline{\mathbf{Z}}$
a2	a2	0.010	$ \checkmark $
a3	a3	0.200	$\square$
f	f	1000.000	$\square$
b1	b1	0.001	$\square$
b2	b2	0.001	$ \checkmark $
b3	b3	$7 \cdot 10^{-4}$	$\mathbf{Z}$
gamma1	gamma1	1.000	$\square$
eta5	eta5	$10^{-4}$	$\square$
e1	e1	0.005	$\square$
e2	e2	0.100	$\square$
f2	f2	$9.95 \cdot 10^{-4}$	
f1	f1	0.001	$\mathbf{Z}$
f3	f3	0.010	$\square$
gamma2	gamma2	1.000	$\square$
k1c	k1c	0.050	
k2c	k2c	0.001	$\square$
k3c	k3c	5.000	$\square$
eta3	eta3	$10^{-4}$	$\mathbf{Z}$
c1	c1	1.000	$\square$
c2	c2	0.010	$\square$
c3	c3	0.200	$\mathbf{Z}$
d1	d1	0.001	$\square$
d2	d2	0.001	$\square$
d3	d3	$7 \cdot 10^{-4}$	$\square$
gamma3	gamma3	1.000	$\mathbf{Z}$
g1	g1	0.100	$\overline{\mathbf{Z}}$
eta7	eta7	$10^{-4}$	$\overline{\mathbf{Z}}$
h1	h1	0.002	$\mathbf{Z}$
h2	h2	0.050	$\mathbf{Z}$
gamma4	gamma4	0.010	$\mathbf{Z}$

# Produced by SBML2ATEX

# 6 Reactions

This model contains ten reactions. All reactions are listed in the following table and are subsequently described in detail. If a reaction is affected by a modifier, the identifier of this species is written above the reaction arrow.

Table 5: Overview of all reactions

N⁰	Id	Name	Reaction Equation SB	Ю
1	J0		OCT4_Gene A, OCT4_SOX2, NANOG OCT4	
2	J1		OCT4 —→ degradation	
3	J2		$NANOG\_Gene \xrightarrow{OCT4\_SOX2, p53} NANOG$	
4	J3		NANOG degradation	
5	J4		$OCT4 + SOX2 \longrightarrow OCT4\_SOX2$	
6	J5		OCT4_SOX2 —→ degradation	
7	J6		$SOX2\_Gene \xrightarrow{A, OCT4\_SOX2, NANOG} SOX2$	
8	J7		$SOX2 \longrightarrow degradation$	
9	Ј8		targetGene $\xrightarrow{\text{OCT4\_SOX2}}$ NANOG Protein	
10	J9		Protein → degradation	

#### **6.1 Reaction** J0

This is an irreversible reaction of one reactant forming one product influenced by three modifiers.

#### **Reaction equation**

OCT4\_Gene 
$$\xrightarrow{A, \text{ OCT4\_SOX2}, \text{ NANOG}} \text{ OCT4}$$
 (1)

#### Reactant

Table 6: Properties of each reactant.

Id	Name	SBO
OCT4_Gene		

#### **Modifiers**

Table 7: Properties of each modifier.

Id	Name	SBO
A		
$0CT4\_SOX2$		
NANOG		

#### **Product**

Table 8: Properties of each product.

Id	Name	SBO
OCT4		

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_1 = \frac{\text{eta1} + \text{a1} \cdot [\text{A}] + \text{a2} \cdot [\text{OCT4\_SOX2}] + \text{a3} \cdot [\text{OCT4\_SOX2}] \cdot [\text{NANOG}]}{1 + \frac{\text{eta1}}{\text{f}} + \text{b1} \cdot [\text{A}] + \text{b2} \cdot [\text{OCT4\_SOX2}] + \text{b3} \cdot [\text{OCT4\_SOX2}] \cdot [\text{NANOG}]}$$
(2)

#### **6.2 Reaction** J1

This is an irreversible reaction of one reactant forming one product.

#### **Reaction equation**

$$OCT4 \longrightarrow degradation$$
 (3)

#### Reactant

Table 9: Properties of each reactant.

Id	Name	SBO
OCT4		

#### **Product**

Table 10: Properties of each product.

Id	Name	SBO
degradation		

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_2 = \text{gamma1} \cdot [\text{OCT4}] \tag{4}$$

#### **6.3 Reaction** J2

This is an irreversible reaction of one reactant forming one product influenced by two modifiers.

#### **Reaction equation**

$$NANOG\_Gene \xrightarrow{OCT4\_SOX2, p53} NANOG$$
 (5)

#### Reactant

Table 11: Properties of each reactant.

Id	Name	SBO
NANOG_Gene		

#### **Modifiers**

Table 12: Properties of each modifier.

Id	Name	SBO
OCT4_SOX2		
p53		

#### **Product**

Table 13: Properties of each product.

Id	Name	SBO
NANOG		

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_{3} = \frac{\text{eta5} + \text{e1} \cdot [\text{OCT4\_SOX2}] + \text{e2} \cdot [\text{OCT4\_SOX2}] \cdot [\text{NANOG}]}{1 + \frac{\text{eta5}}{\text{f}} + \text{f2} \cdot [\text{OCT4\_SOX2}] + \text{f1} \cdot [\text{OCT4\_SOX2}] \cdot [\text{NANOG}] + \text{f3} \cdot [\text{p53}]}$$
(6)

#### **6.4 Reaction** J3

This is an irreversible reaction of one reactant forming one product.

#### **Reaction equation**

$$NANOG \longrightarrow degradation \tag{7}$$

#### Reactant

Table 14: Properties of each reactant.

Id	Name	SBO
NANOG		

#### **Product**

Table 15: Properties of each product.

Id	Name	SBO
degradation		

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_4 = \text{gamma2} \cdot [\text{NANOG}]$$
 (8)

#### 6.5 Reaction J4

This is an irreversible reaction of two reactants forming one product.

#### **Reaction equation**

$$OCT4 + SOX2 \longrightarrow OCT4\_SOX2 \tag{9}$$

#### **Reactants**

Table 16: Properties of each reactant.

Id	Name	SBO
OCT4		
SOX2		

#### **Product**

Table 17: Properties of each product.

Id	Name	SBO
OCT4_SOX2		

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_5 = \text{k1c} \cdot [\text{OCT4}] \cdot [\text{SOX2}] - \text{k2c} \cdot [\text{OCT4\_SOX2}]$$
 (10)

#### 6.6 Reaction J5

This is an irreversible reaction of one reactant forming one product.

#### **Reaction equation**

$$OCT4\_SOX2 \longrightarrow degradation$$
 (11)

#### Reactant

Table 18: Properties of each reactant.

Id	Name	SBO
OCT4_SOX2		

#### **Product**

Table 19: Properties of each product.

Id	Name	SBO
degradation		

#### **Kinetic Law**

Derived unit contains undeclared units

$$v_6 = k3c \cdot [OCT4\_SOX2] \tag{12}$$

#### **6.7 Reaction** J6

This is an irreversible reaction of one reactant forming one product influenced by three modifiers.

#### **Reaction equation**

$$SOX2\_Gene \xrightarrow{A, OCT4\_SOX2, NANOG} SOX2$$
 (13)

#### Reactant

Table 20: Properties of each reactant.

Id	Name	SBO
SOX2_Gene		

#### **Modifiers**

Table 21: Properties of each modifier.

Id	 Name	SBO
Δ		

Id	Name	SBO
OCT4_SOX2		
NANOG		

#### **Product**

Table 22: Properties of each product.

Id	Name	SBO
SOX2		

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_7 = \frac{\text{eta3} + \text{c1} \cdot [\text{A}] + \text{c2} \cdot [\text{OCT4\_SOX2}] + \text{c3} \cdot [\text{OCT4\_SOX2}] \cdot [\text{NANOG}]}{1 + \frac{\text{eta3}}{\text{f}} + \text{d1} \cdot [\text{A}] + \text{d2} \cdot [\text{OCT4\_SOX2}] + \text{d3} \cdot [\text{OCT4\_SOX2}] \cdot [\text{NANOG}]}$$
(14)

#### **6.8 Reaction** J7

This is an irreversible reaction of one reactant forming one product.

#### **Reaction equation**

$$SOX2 \longrightarrow degradation$$
 (15)

#### Reactant

Table 23: Properties of each reactant.

Id	Name	SBO
SOX2		

#### **Product**

Table 24: Properties of each product.

Id	Name	SBO
degradation		

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_8 = \text{gamma3} \cdot [\text{SOX2}] \tag{16}$$

#### 6.9 Reaction J8

This is an irreversible reaction of one reactant forming one product influenced by two modifiers.

#### **Reaction equation**

#### Reactant

Table 25: Properties of each reactant.

Id	Name	SBO
targetGene		

#### **Modifiers**

Table 26: Properties of each modifier.

Id	Name	SBO
OCT4_SOX2		
NANOG		

#### **Product**

Table 27: Properties of each product.

Id	Name	SBO
Protein		

#### **Kinetic Law**

Derived unit contains undeclared units

$$v_9 = \frac{g1 \cdot [\text{OCT4\_SOX2}] + \text{eta7}}{1 + \frac{\text{eta7}}{\text{f}} + \text{h1} \cdot [\text{OCT4\_SOX2}] + \text{h2} \cdot [\text{OCT4\_SOX2}] \cdot [\text{NANOG}]}$$
(18)

#### 6.10 Reaction J9

This is an irreversible reaction of one reactant forming one product.

#### **Reaction equation**

Protein 
$$\longrightarrow$$
 degradation (19)

#### Reactant

Table 28: Properties of each reactant.

Id	Name	SBO
Protein		

#### **Product**

Table 29: Properties of each product.

Id	Name	SBO
degradation		

#### **Kinetic Law**

Derived unit contains undeclared units

$$v_{10} = \text{gamma4} \cdot [\text{Protein}]$$
 (20)

# 7 Derived Rate Equations

When interpreted as an ordinary differential equation framework, this model implies the following set of equations for the rates of change of each species.

Identifiers for kinetic laws highlighted in gray cannot be verified to evaluate to units of SBML substance per time. As a result, some SBML interpreters may not be able to verify the consistency of the units on quantities in the model. Please check if

- parameters without an unit definition are involved or
- volume correction is necessary because the hasOnlySubstanceUnits flag may be set to false and spacialDimensions> 0 for certain species.

#### 7.1 Species OCT4\_Gene

#### **Initial amount** 0 dimensionless

This species takes part in one reaction (as a reactant in J0), which does not influence its rate of change because this species is on the boundary of the reaction system:

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{OCT4}_{-}\mathrm{Gene} = 0 \tag{21}$$

#### 7.2 Species NANOG\_Gene

#### **Initial amount** 0 dimensionless

This species takes part in one reaction (as a reactant in J2), which does not influence its rate of change because this species is on the boundary of the reaction system:

$$\frac{d}{dt}NANOG\_Gene = 0$$
 (22)

#### 7.3 Species SOX2\_Gene

#### **Initial amount** 0 dimensionless

This species takes part in one reaction (as a reactant in J6), which does not influence its rate of change because this species is on the boundary of the reaction system:

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{SOX2}_{-}\mathrm{Gene} = 0 \tag{23}$$

#### 7.4 Species targetGene

#### **Initial amount** 0.01 dimensionless

This species takes part in one reaction (as a reactant in J8), which does not influence its rate of change because this species is on the boundary of the reaction system:

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{targetGene} = 0 \tag{24}$$

#### 7.5 Species degradation

#### **Initial amount** 0 dimensionless

This species takes part in five reactions (as a product in J1, J3, J5, J7, J9), which do not influence its rate of change because this species is on the boundary of the reaction system:

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{degradation} = 0 \tag{25}$$

#### 7.6 Species p53

#### **Initial amount** 0 dimensionless

This species takes part in one reaction (as a modifier in J2), which does not influence its rate of change because this species is on the boundary of the reaction system:

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathbf{p}53 = 0\tag{26}$$

#### 7.7 Species A

#### **Initial amount** 10 dimensionless

This species takes part in two reactions (as a modifier in J0, J6), which do not influence its rate of change because this species is on the boundary of the reaction system:

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathbf{A} = 0\tag{27}$$

#### 7.8 Species OCT4

#### **Initial amount** 0.01 dimensionless

This species takes part in three reactions (as a reactant in J1, J4 and as a product in J0).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{OCT4} = |v_1| - |v_2| - |v_5| \tag{28}$$

#### 7.9 Species SOX2

#### **Initial amount** 0.01 dimensionless

This species takes part in three reactions (as a reactant in J4, J7 and as a product in J6).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{SOX2} = |v_7| - |v_5| - |v_8| \tag{29}$$

#### 7.10 Species NANOG

#### **Initial amount** 0.01 dimensionless

This species takes part in five reactions (as a reactant in J3 and as a product in J2 and as a modifier in J0, J6, J8).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{NANOG} = v_3 - v_4 \tag{30}$$

#### 7.11 Species OCT4\_SOX2

#### **Initial amount** 0.1 dimensionless

This species takes part in six reactions (as a reactant in J5 and as a product in J4 and as a modifier in J0, J2, J6, J8).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{OCT4\_SOX2} = v_5 - v_6 \tag{31}$$

#### 7.12 Species Protein

#### **Initial amount** 0 dimensionless

This species takes part in two reactions (as a reactant in J9 and as a product in J8).

$$\frac{\mathrm{d}}{\mathrm{d}t} \text{Protein} = |v_9| - |v_{10}| \tag{32}$$

 $\mathfrak{BML2}^{d}$  was developed by Andreas Dräger<sup>a</sup>, Hannes Planatscher<sup>a</sup>, Dieudonné M Wouamba<sup>a</sup>, Adrian Schröder<sup>a</sup>, Michael Hucka<sup>b</sup>, Lukas Endler<sup>c</sup>, Martin Golebiewski<sup>d</sup> and Andreas Zell<sup>a</sup>. Please see http://www.ra.cs.uni-tuebingen.de/software/SBML2LaTeX for more information.

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