

## SBML Model Report

**Model name:**  
**“Zhu2007\_TF\_modulated\_by\_Calcium”**



May 6, 2016

### 1 General Overview

This is a document in SBML Level 2 Version 4 format. This model was created by Harish Dharuri<sup>1</sup> at December 21<sup>st</sup> 2007 at 9:55 a.m. and last time modified at May 27<sup>th</sup> 2014 at 10:02 p.m. Table 1 provides an overview of the quantities of all components of this model.

Table 1: Number of components in this model, which are described in the following sections.

Element	Quantity	Element	Quantity
compartment types	0	compartments	2
species types	0	species	3
events	0	constraints	0
reactions	9	function definitions	0
global parameters	7	unit definitions	2
rules	2	initial assignments	0

### Model Notes

This a model from the article:

**A theoretical study on activation of transcription factor modulated by intracellular Ca<sup>2+</sup> oscillations.**

Zhu CL, Zheng Y, Jia Y *Biophys. Chem.*[2007 Aug;129(1):49-55 [17560007](#),

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**Abstract:**

This work presents both deterministic and stochastic models of genetic expression modulated by intracellular calcium ( $\text{Ca}^{2+}$ ) oscillations, based on macroscopic differential equations and chemical Langevin equations, respectively. In deterministic case, the oscillations of intracellular  $\text{Ca}^{2+}$  decrease the effective  $\text{Ca}^{2+}$  threshold for the activation of transcriptional activator (TF-A). The average activation of TF-A increases with the increase of the average amplitude of intracellular  $\text{Ca}^{2+}$  oscillations, but decreases with the increase of the period of intracellular  $\text{Ca}^{2+}$  oscillations, which are qualitatively consistent with the experimental results on the gene expression in lymphocytes. In stochastic case, it is found that a large internal fluctuation of the biochemical reaction can enhance gene expression efficiency specifically at a low level of external stimulations or at a small rate of TF-A dimer phosphorylation activated by  $\text{Ca}^{2+}$ , which reduces the threshold of the average intracellular  $\text{Ca}^{2+}$  concentration for gene expression.

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To cite BioModels Database, please use [Le Novre N., Bornstein B., Broicher A., Courtot M., Donizelli M., Dharuri H., Li L., Sauro H., Schilstra M., Shapiro B., Snoep J.L., Hucka M.\(2006\) BioModels Database: A Free, Centralized Database of Curated, Published, Quantitative Kinetic Models of Biochemical and Cellular Systems Nucleic Acids Res., 34: D689-D691.](#)

## 2 Unit Definitions

This is an overview of five unit definitions of which three are predefined by SBML and not mentioned in the model.

### 2.1 Unit `substance`

**Name** micro mole

**Definition**  $\mu\text{mol}$

### 2.2 Unit `time`

**Name** minutes

**Definition** 60 s

### 2.3 Unit `volume`

**Notes** Litre is the predefined SBML unit for volume.

**Definition** 1

## 2.4 Unit `area`

**Notes** Square metre is the predefined SBML unit for `area` since SBML Level 2 Version 1.

**Definition**  $\text{m}^2$

## 2.5 Unit `length`

**Notes** Metre is the predefined SBML unit for `length` since SBML Level 2 Version 1.

**Definition**  $\text{m}$

# 3 Compartments

This model contains two compartments.

Table 2: Properties of all compartments.

Id	Name	SBO	Spatial Dimensions	Size	Unit	Constant	Outside
<code>cytoplasm</code>	<code>cytoplasm</code>		3	1	litre	<input checked="" type="checkbox"/>	
<code>store</code>	<code>store</code>		3	1	litre	<input checked="" type="checkbox"/>	

### 3.1 Compartment `cytoplasm`

This is a three dimensional compartment with a constant size of one litre.

**Name** `cytoplasm`

### 3.2 Compartment `store`

This is a three dimensional compartment with a constant size of one litre.

**Name** `store`

## 4 Species

This model contains three species. Section 8 provides further details and the derived rates of change of each species.

Table 3: Properties of each species.

Id	Name	Compartment	Derived Unit	Constant	Boundary Condition
X	TF_A	cytoplasm	$\mu\text{mol} \cdot \text{l}^{-1}$	$\square$	$\square$
Y	Calcium in store	store	$\mu\text{mol} \cdot \text{l}^{-1}$	$\square$	$\square$
Z	Calcium in cytoplasm	cytoplasm	$\mu\text{mol} \cdot \text{l}^{-1}$	$\square$	$\square$

## 5 Parameters

This model contains seven global parameters.

Table 4: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
kf	kf		0.0		<input type="checkbox"/>
Kd	Kd		0.0		<input type="checkbox"/>
kf0			6.0		<input checked="" type="checkbox"/>
gamma			9.0		<input checked="" type="checkbox"/>
Ka	Ka		0.5		<input checked="" type="checkbox"/>
Kb	Kb		0.5		<input checked="" type="checkbox"/>
Kd0			10.0		<input checked="" type="checkbox"/>

## 6 Rules

This is an overview of two rules.

### 6.1 Rule $_{kf}$

Rule  $_{kf}$  is an assignment rule for parameter  $_{kf}$ :

$$kf = kf0 \cdot \left( 1 + \frac{\text{gamma} \cdot [Z]^4}{Ka^4 + [Z]^4} \right) \quad (1)$$

### 6.2 Rule $_{Kd}$

Rule  $_{Kd}$  is an assignment rule for parameter  $_{Kd}$ :

$$Kd = \frac{Kd0}{1 + \frac{[Z]^4}{Kb^4}} \quad (2)$$

## 7 Reactions

This model contains nine reactions. All reactions are listed in the following table and are subsequently described in detail. If a reaction is affected by a modifier, the identifier of this species is written above the reaction arrow.

Table 5: Overview of all reactions

Nº	Id	Name	Reaction Equation	SBO
1	TF_synthesis	TF Synthesis	$\emptyset \rightleftharpoons X$	
2	TF_degradation	TF degradation	$X \rightleftharpoons \emptyset$	
3	TF_synthesis-_basal	TF_synthesis_basal	$\emptyset \rightleftharpoons X$	
4	Calcium_Influx	Calcium_Influx	$\emptyset \rightleftharpoons Z$	
5	Calcium_Influx-_stimulation	Calcium Influx by stimulation	$\emptyset \rightleftharpoons Z$	
6	Calcium_into-_store	Calcium Influx	$Z \rightleftharpoons Y$	
7	Calcium_into-_cytoplasm	Calcium influx to cytoplasm	$Y \rightleftharpoons Z$	
8	Leakage	Calcium Leakage	$Y \rightleftharpoons Z$	
9	Leakage_from-_cytoplasm	Leakage from cytoplasm	$Z \rightleftharpoons \emptyset$	

## 7.1 Reaction TF\_synthesis

This is a reversible reaction of no reactant forming one product.

**Name** TF Synthesis

### Reaction equation



### Product

Table 6: Properties of each product.

Id	Name	SBO
X	TF_A	

### Kinetic Law

**Derived unit** contains undeclared units

$$v_1 = \frac{k_f \cdot [X]^2}{[X]^2 + K_d} \quad (4)$$

## 7.2 Reaction TF\_degradation

This is a reversible reaction of one reactant forming no product.

**Name** TF degradation

### Reaction equation



### Reactant

Table 7: Properties of each reactant.

Id	Name	SBO
X	TF_A	

### Kinetic Law

**Derived unit** contains undeclared units

$$v_2 = k_d \cdot [X] \quad (6)$$

Table 8: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
kd			1.0		<input checked="" type="checkbox"/>

### 7.3 Reaction `TF_synthesis_basal`

This is a reversible reaction of no reactant forming one product.

**Name** `TF_synthesis_basal`

#### Reaction equation



#### Product

Table 9: Properties of each product.

Id	Name	SBO
X	TF_A	

#### Kinetic Law

**Derived unit** not available

$$v_3 = R_{bas} \quad (8)$$

Table 10: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
Rbas	Rbas		0.1		<input checked="" type="checkbox"/>

### 7.4 Reaction `Calcium_Influx`

This is a reversible reaction of no reactant forming one product.

**Name** `Calcium_Influx`



### Reaction equation



### Product

Table 11: Properties of each product.

Id	Name	SBO
Z	Calcium in cytoplasm	

### Kinetic Law

**Derived unit** not available

$$v_4 = v_0 \quad (10)$$

Table 12: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
v0			1.0		<input checked="" type="checkbox"/>

## 7.5 Reaction `Calcium_Influx_stimulation`

This is a reversible reaction of no reactant forming one product.

**Name** Calcium Influx by stimulation

### Reaction equation



### Product

Table 13: Properties of each product.

Id	Name	SBO
Z	Calcium in cytoplasm	

### Kinetic Law

**Derived unit** not available

$$v_5 = v_1 \cdot \text{beta} \quad (12)$$

Table 14: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
v1			5.7		<input checked="" type="checkbox"/>
beta			0.3		<input checked="" type="checkbox"/>

## 7.6 Reaction Calcium\_into\_store

This is a reversible reaction of one reactant forming one product.

**Name** Calcium Influx

### Reaction equation



### Reactant

Table 15: Properties of each reactant.

Id	Name	SBO
Z	Calcium in cytoplasm	

### Product

Table 16: Properties of each product.

Id	Name	SBO
Y	Calcium in store	

### Kinetic Law

**Derived unit** contains undeclared units

$$v_6 = \frac{V_{m2} \cdot [Z]^n}{K_2^n + [Z]^n} \quad (14)$$

Table 17: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
Vm2			30.0		<input checked="" type="checkbox"/>
K2			0.5		<input checked="" type="checkbox"/>
n			2.0		<input checked="" type="checkbox"/>

## 7.7 Reaction Calcium\_into\_cytoplasm

This is a reversible reaction of one reactant forming one product.

**Name** Calcium influx to cytoplasm

### Reaction equation



### Reactant

Table 18: Properties of each reactant.

Id	Name	SBO
Y	Calcium in store	

### Product

Table 19: Properties of each product.

Id	Name	SBO
Z	Calcium in cytoplasm	

### Kinetic Law

**Derived unit** contains undeclared units

$$v_7 = \frac{\frac{V_{m3} \cdot [Y]^m}{K_r^m + [Y]^m} \cdot [Z]^p}{K_A^p + [Z]^p} \quad (16)$$

Table 20: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
V <sub>m3</sub>			325.00		<input checked="" type="checkbox"/>
K <sub>r</sub>			1.70		<input checked="" type="checkbox"/>
K <sub>A</sub>			0.46		<input checked="" type="checkbox"/>
m			2.00		<input checked="" type="checkbox"/>
p			4.00		<input checked="" type="checkbox"/>

## 7.8 Reaction Leakage

This is a reversible reaction of one reactant forming one product.

**Name** Calcium Leakage

### Reaction equation



### Reactant

Table 21: Properties of each reactant.

Id	Name	SBO
Y	Calcium in store	

### Product

Table 22: Properties of each product.

Id	Name	SBO
Z	Calcium in cytoplasm	

### Kinetic Law

**Derived unit** contains undeclared units

$$v_8 = k_1 \cdot [Y] \quad (18)$$

Table 23: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
k1			0.7		<input checked="" type="checkbox"/>

## 7.9 Reaction Leakage\_from\_cytoplasm

This is a reversible reaction of one reactant forming no product.

**Name** Leakage from cytoplasm

### Reaction equation



### Reactant

Table 24: Properties of each reactant.

Id	Name	SBO
Z	Calcium in cytoplasm	

### Kinetic Law

**Derived unit** contains undeclared units

$$v_9 = k \cdot [Z] \quad (20)$$

Table 25: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
k			10.0		<input checked="" type="checkbox"/>

## 8 Derived Rate Equations

When interpreted as an ordinary differential equation framework, this model implies the following set of equations for the rates of change of each species.

Identifiers for kinetic laws highlighted in gray cannot be verified to evaluate to units of SBML substance per time. As a result, some SBML interpreters may not be able to verify the consistency of the units on quantities in the model. Please check if

- parameters without an unit definition are involved or
- volume correction is necessary because the `hasOnlySubstanceUnits` flag may be set to `false` and `spacialDimensions`  $> 0$  for certain species.

### 8.1 Species X

**Name** TF\_A

**Initial concentration**  $15 \mu\text{mol} \cdot \text{l}^{-1}$

This species takes part in three reactions (as a reactant in [TF\\_degradation](#) and as a product in [TF\\_synthesis](#), [TF\\_synthesis\\_basal](#)).

$$\frac{d}{dt}X = v_1 + v_3 - v_2 \quad (21)$$

### 8.2 Species Y

**Name** Calcium in store

**Initial concentration**  $0 \mu\text{mol} \cdot \text{l}^{-1}$

This species takes part in three reactions (as a reactant in [Calcium\\_into\\_cytoplasm](#), [Leakage](#) and as a product in [Calcium\\_into\\_store](#)).

$$\frac{d}{dt}Y = v_6 - v_7 - v_8 \quad (22)$$

### 8.3 Species Z

**Name** Calcium in cytoplasm

**Initial concentration**  $0.25 \mu\text{mol} \cdot \text{l}^{-1}$

This species takes part in six reactions (as a reactant in [Calcium\\_into\\_store](#), [Leakage\\_from\\_cytoplasm](#) and as a product in [Calcium\\_Influx](#), [Calcium\\_Influx\\_stimulation](#), [Calcium\\_into\\_cytoplasm](#), [Leakage](#)).

$$\frac{d}{dt}Z = v_4 + v_5 + v_7 + v_8 - v_6 - v_9 \quad (23)$$

SBML<sup>2</sup>TeX was developed by Andreas Dräger<sup>a</sup>, Hannes Planatscher<sup>a</sup>, Dieudonné M Wouamba<sup>a</sup>, Adrian Schröder<sup>a</sup>, Michael Hucka<sup>b</sup>, Lukas Endler<sup>c</sup>, Martin Golebiewski<sup>d</sup> and Andreas Zell<sup>a</sup>. Please see <http://www.ra.cs.uni-tuebingen.de/software/SBML2LaTeX> for more information.

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