The HomeworkAssignment class*

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1 Abstract

This class provides a relative simple docuemnt—type for homework, mainly created for assignments at the University This class is inherited from article, it is not perfect, but I am trying my verry best.

2 Options

problemstyle=<1>
subproblemstyle=<1>
subsubproblemstyle=<1>

These options allow the customizatuion of the displayed numbers. For Example, if problemstyle=Roman, subproblemstyle=arabic, subsubproblemstyle=roman is passed, The first subsubproblem of the first subproblem of the first problem would be labled as i) of **Problem I.1**.

Available options are arabic, Alph, alph, Roman, and roman. Standard values are: problemstyle=arabic, subproblemstyle=alph, subsubproblemstyle=roman.

design=<1>

Allows the User to select an older page-style, for backwards compatibility.

Recognized values are v1 and v2. Everytime a version Changes the default look, a new possible value will be added.

Only set this if you really need to get an old look, older styles are not going to be maintained!

2.1 Inherited options

Because the class is inherited by article, every Option that can be passed to article, will be passed to article.

3 Commands

3.1 Document Informations

\subject \kurs

Sets the subject of the document. Takes the subject as argument. Standard Value

^{*}This document corresponds to HomeworkAssignment v2.0,dated 2017/05/13.

is "Kein Kurs" \kurs is deprecated.

\tutorial \tutorium

Sets the tutorial of the author. Takes it as an argument. Stamdard Value is empty, so that this command can be omitted.

\tutorium is deprecated.

\deadline \abgabe

Sets the deadline of the document. Takes it as an argument. Standard value is \today.

\abgabe is deprecated

Inherited from article 3.1.1

\author \date Sets the author of the document.

Sets the date of the document.

3.2 Sectioning

Because the class is designed for Assignments, the sectioning-commands are different from Article

3.2.1'plain' Sectioning

\problem \subproblem \subsubproblem

These commands work like theyr counterpart in article, except that there will be no number, nor will they increase a counter. Nevertheless, hey will be shown in the table of contents.

\solution \proof \given \toShow

They work like Paragraph, but do not take an argument, instead they print out "Lösung", "Beweis" "Gegeben", and "Zu zeigen", respectively¹. They are not mentioned in the table of contents.

3.2.2'better' Sectioning

The following commands are an augmented version of the "plain" commands.

These commands require no argument, and automatically create a numbered \newproblem \newsubproblem title. The optional Argument is the new value for the coresponding counter.

\newsubsubproblem

Useful Macros 3.3

3.3.1Quod Erat Demunstarndum, End of Proof

Display a flushed-right QED, \square , or \blacksquare , respectively. \qed is not implemented, to \QED keep compatibility to several Math-packages, which define the later. \EOP

\eop

See 8.2 for all Translations

¹As of v1.6, Translations are added, depending on the choosen Language, there may be an other Text displayed.

3.3.2 Quod Non Erat Demunstarndum at iucundum est

\QNED \qned Display a flushed-right \triangle . \QNED displays it in a new line, \quad at the end of the same line.

In Mathematical proofs this symbol is used to mark things, which we did not intend to proof, but are interesting anyway.

3.4 Stolen Goods

»Das ist alles nur geklaut«

 \sim Tobias Künzel

These Commands are not mine, they are all stolen from Alexander Bartolomey's 2 2 amath-Class 3

\N	⁴⁵ Defines a set of mathematical fields, which are verry usefull (see Table 1)		
\Z			
\R	Command	Output	Description
\Q	\N	\mathbb{N}	Natural Numbers
\C	\Z	$\mathbb Z$	Whole? Numbers
\F	\Q	\mathbb{Q}	Rational Numbers
\Primes	\R	\mathbb{R}	Real Numbers
	\C	\mathbb{C}	Complex Numbers
	\ F	\mathbb{F}	Prime-Fieled?

Table 1: Field-Commands

Set of all Primes

Functions and Operators

Output usefull Plaintext-Operators and Functions.

\Primes

All, except \diff<1>\} print the 'themselve' as text, \diff{<1>} outputs $\frac{d}{d<1>}$.

4 Pagestyle

4.1 Headers

 $^{^2\,\}mathrm{``Occloxium''}$ on GitHub:https://github.com/occloxium

³Amath.sty is part of Alexander Bartolomey's Alphabet Classes: https://github.com/occloxium/AlphabetClasses

⁴Has to be \mathbb{P} , because \P is already in use

 $^{^5\}mathrm{not}$ a Field

5 Development and support

The package is developed at github:

https://github.com/ACHinrichs/LaTeX-templates

Please refer to that site for any bug report or development information.

6 Changelog

```
v1.0 - 2016/10/23 Intial
```

v1.1 - 2016/11/02 ...

v1.2 - 2016/11/03 ...

v1.3 - 2016/12/01 Provide the Class as .dtx file and more

v1.4 - 2017/04/29 "Minor" bugfixes

v1.5 - 2017/04/29 Problems are displayed in the table of contents. Type of numeration is now configurable.

v1.5.1 - 2017/04/29 Bugfix

v1.5.2 - 2017/04/29 Add version-number

v1.6 - 2017/05/02 Add Translations (German and English) Add \given and \toShow

Add \QED, \EOP, and \eop

v1.6.3 - 2017/05/05 Bugfixes

v1.6.4 - 2017/05/09 Change \eop to be in the same line

v2.0 - 2017/05/09 Change Margins,

Add Option to select older Page-Style,

Change standardlayout to twocolumn and twoside

7 Examples

For examples, pleas see the Git-Repo at https://github.com/ACHinrichs/LaTeX-templates

8 Implementation

The following part is verry boring, but I have not found a solution to create a .cls-file without including the implementation into the document. Loads LATEX2e and sets the Version Loads the article, which is the base-class.

8.1 Packages & Options

```
1 \RequirePackage{kvoptions}
2 \SetupKeyvalOptions{ family=hwachar '
   prefix=hwa@ }
4 \DeclareStringOption[arabic]{problemsty}
5 \DeclareStringOption[alph]{subproblemsty}
6 \DeclareStringOption[roman] {subsubproblemsty}
7 \DeclareBoolOption[false]{listings}
8 \DeclareStringOption[v2] {design}
9 \DeclareBoolOption[true] {twoside}
10 \DeclareComplementaryOption{oneside}{twoside}
11 \DeclareBoolOption[true] {twocolumn}
13 % Redefine the articlechar 'options
       \begin{macrocode}
15 \DeclareDefaultOption{\PassOptionsToClass{\CurrentOptionKey}{article}}
   Processes the Options and loades article
16 \ProcessKeyvalOptions*
17 \ifhwa@twoside
18 \PassOptionsToClass{twoside}{article}
20 \PassOptionsToClass{oneside}{article}
21 \fi
22 \ifhwa@twocolumn
23 \PassOptionsToClass{twocolumn}{article}
25 \PassOptionsToClass{onecolumn}{article}
27 \LoadClass{article}
   Loads required Packages
28 \RequirePackage{suffix}
29 \RequirePackage{fancyhdr}
30 \RequirePackage{ifthen}
31 \RequirePackage{translations}
32 \RequirePackage{amssymb}
```

```
33 \RequirePackage{amschar 'ath}
34 \ifhwa@listings
35 \RequirePackage{listings}
36 \lstset{
    frame = singlechar '
37
    breaklines = truechar '
    postbreak=\raisebox{0ex}[0ex][0ex][\ensuremath{\hookrightarrow\space}}char '
40
    basicstyle=\scriptsize
41 }
42 \ensuremath{\setminus} else
43 \empty
44 \fi
45
46 % Make sure that this is the last Package loaded
47 \left( \frac{v2}{v2} \right)
    \RequirePackage{geometry}
48
    \ifhwa@twocolumn
49
    \geometry{top=2cmchar ' bottom=2cmchar ' left=2cmchar '
50
      headsep=14ptchar 'hmarginratio={1:1}}
51
52
    \geometry{top=2cmchar 'bottom=2cmchar 'width=35emchar '
53
      headsep=14ptchar 'hmarginratio={4:3}}
54
    \fi
55
56 }{
    57
      \empty
58
59
      \ClassError{HomeworkAssignment}{Value char '\egrouphwa@designchar 'for key char 'designch
60
      is not known"-The option design takes an argument to set the
61
      Pagestyle to the one of a previous version. Acceptable values are
62
      char 'v1char 'char ' or char 'v2char '}
63
64
    }
65 }
```

8.2 Translations

Load translations, currently supports English and German, Fallback is German

```
66 \DeclareTranslationFallback{aufgabe}{Aufgabe}
67 \DeclareTranslationFallback{loesung}{L\"osung}
68 \DeclareTranslationFallback{beweis}{Beweis}
69 \DeclareTranslationFallback{uebungsgruppe}{\"Ubungsgruppe}
70 \DeclareTranslationFallback{abgabe}{Abgabe}
71 \DeclareTranslationFallback{zuZeigen}{Zu zeigen}
72 \DeclareTranslationFallback{gegeben}{Gegeben}
73 \DeclareTranslationFallback{falls}{falls}
74 \DeclareTranslationFallback{Falls}{Falls}
75
76 \DeclareTranslation{German}{aufgabe}{Aufgabe}
77 \DeclareTranslation{German}{loesung}{L\"osung}
78 \DeclareTranslation{German}{beweis}{Beweis}
```

```
79 \DeclareTranslation{German}{uebungsgruppe}{\"Ubungsgruppe}
80 \DeclareTranslation{German}{abgabe}{Abgabe}
81 \DeclareTranslation{German}{zuZeigen}{Zu zeigen}
82 \DeclareTranslation{German}{gegeben}{Gegeben}
83 \DeclareTranslation{German}{falls}{falls}
84 \DeclareTranslation{German}{Falls}{Falls}
85
86 \DeclareTranslation{English}{aufgabe}{Problem}
87 \DeclareTranslation{English}{loesung}{Solution}
88 \DeclareTranslation{English}{beweis}{Proof}
89 \DeclareTranslation{English}{uebungsgruppe}{Tutorial}
90 \DeclareTranslation{English}{abgabe}{Deadline}
91 \DeclareTranslation{English}{zuZeigen}{To show}
92 \DeclareTranslation{English}{gegeben}{Given}
93 \DeclareTranslation{English}{falls}{if}
94 \DeclareTranslation{English}{falls}{if}
```

8.3 Headers & Footers

Sets the page-headers.

All headers are cleread before they get any Text — just to be sure. The headers look like specified above (4.1). Also inserts the Titlepage.

```
95 \makeatletter
96 \fancypagestyle{firstpage}{
    %
97
    \fancyhf{}
98
    % clear all six fields
     \renewcommand{\headrulewidth}{.7pt}
100
     \renewcommand{\footrulewidth}{Opt}
101
     \fancyfoot[R]{\thepage}
102
     \fancyhead[L]{\hwa@tutorium}
103
     \fancyhead[R]{\@date } }
104
105 \fancypagestyle{followingpage}{
106
     \fancyhf{}
107
108
     109
       \ifhwa@twoside % IF
110
111
       \fancyhead[RO]{\@author}
112
       \fancyhead[L0]{\hwa@kurs}\
113
         \hwa@tutorium}
114
       \fancyhead[LE]{\GetTranslation{abgabe}: \hwa@abgabe}
115
       \fancyfoot[ROchar 'LE]{\thepage}
116
117
       \else %ELSE
118
119
       \fancyhead[R]{\hwa@kurs\\
120
         \@author}
121
```

```
\fancyhead[L]{\hwa@tutorium\\
122
          \GetTranslation{abgabe}: \hwa@abgabe}
123
       \fancyfoot[R]{\thepage}
124
       \fi %ENDIF
125
     }{
126
127
       \left( \frac{\ensuremath{\text{hwa@design}}}{v1} \right) 
128
         \fancyhead[REchar 'LO]{\@author}
         \fancyhead[LEchar 'RO]{\hwa@kurs\\
129
            \GetTranslation{abgabe}: \hwa@abgabe}
130
         \fancyfoot[REchar 'LO]{\thepage}
131
       }{
132
         \ClassError{HomeworkAssignment}{Value char '\egrouphwa@designchar 'for key char 'design
133
            is not known"-The option design takes an argument to set the
134
           Pagestyle to the one of a previous version. Acceptable values are
135
            char 'v1char 'char ' or char 'v2char '}
136
       }
137
     }
138
139
140
141
     \renewcommand{\headrulewidth}{0.7pt}
     \renewcommand{\footrulewidth}{Opt} } \pagestyle{followingpage}
142
143 \AtBeginDocument{ \thispagestyle{firstpage}
     \setlength{\headheight}{25pt} }
```

8.4 Internal commands

8.4.1 Counter-Commands

Counter--Commands

```
These are used to output the Exercise numbers in the desired style 145 \newcommand{\hwa@problemno}{\arabic{problem}} 146 \newcommand{\hwa@subproblemno}{\alph{subproblem}} 147 \newcommand{\hwa@subsubproblemno}{\roman{subsubproblem}}
```

8.4.2 Counter-Style Parser

Counter--Style Parser

This takes a style-input (#1), one of the three previous defined commands (#2) and the coresponding counter (#3) to redefine #1, so that it corresponds to #2. See 8.4.3 for example usement.

```
148 \newcommand{\hwa@parseCounterStyle}[3]{
     \left\{ \frac{\#1}{\arabic} \right\} 
149
       \ifthenelse{\equal{#1}{roman}}{ \renewcommand{#2}{\roman{#3}} }{
150
         \ifthenelse{\equal{#1}{alph}}{ \renewcommand{#2}{\alph{#3}} }{
151
           \ifthenelse{\equal{#1}{Alph}}{ \renewcommand{#2}{\Alph{#3}} }{
152
             \ifthenelse{\equal{#1}{Roman}}{
153
              \mbox{renewcommand}{\#2}{\mathbb{4}}} 
154
              \ClassError{HomeworkAssignment}{Invalid Value #1 for
155
                option Counterchar 'Styling}{Possible Values are alphchar '
156
                arabicchar ' Arabicchar ' roman or Roman.} } } } }
157
```

8.4.3 Counter-Commands II

counter--Style ParserCommands II Redefines the three counter-commands

```
158 \hwa@parseCounterStyle{\hwa@problemsty}{\hwa@problemno}{problem}
           159 \hwa@parseCounterStyle{\hwa@subproblemsty}{\hwa@subproblemno}{subproblem}
           160 \hwa@parseCounterStyle{\hwa@subsubproblemsty}{\hwa@subsubproblemno}{subsubproblem}
            8.5
                   Commands
 \subject Defines \kurs. \subject equals \kurs
           161 \newcommand{\hwa@kurs}{?\GetTranslation{subject}?}
           162 \newcommand{\subject}[1]{\renewcommand{\hwa@kurs}{#1}}
           163 \newcommand{\kurs}[1]{\subject{#1}}
\tutorial Defines \tutorial. \tutorium equals \tutorial
           164 \newcommand{\hwa@tutorium}{?\GetTranslation{uebungsgruppe}?}
           165 \newcommand{\tutorial}[1]{\renewcommand{\hwa@tutorium}{#1}}
           166 \newcommand{\tutorium}[1]{\tutorial{#1}}
 \deadline Defines \deadline. \abgabe equals \deadline
           167 \newcommand{\hwa@abgabe}{\today}
           168 \newcommand{\deadline}[1]{\def\hwa@abgabe{#1}}
           169 \newcommand{\abgabe}[1]{\deadline{#1}}
\maketitle Overrides maketitle.
           170
           171 \renewcommand{\maketitle} {
                \twocolumn[{%
           172
                   \begin{centering}
           173
                    \huge{\textbf{\hwa@kurs}} \vspace{.25cm} {\hrule height 2pt}
           174
                    \vspace{.25cm} \large
           175
                    \GetTranslation{abgabe}: \hwa@abgabe\\
           176
                    \vspace{.5cm} \hrule \vspace{.25cm}
           177
                    \normalsize{\@author}\\
           178
                     \vspace{.25cm} \hrule \vspace{.25cm} \normalsize
           179
                   \end{centering}
           180
                }]
           181
           182 }
            Defines and initialize all counters.
           183 \newcounter{problem} \setcounter{problem}{0}
           184 \newcounter{subproblem}[problem] \setcounter{subproblem}{0}
           185 \newcounter{subsubproblem}[subproblem] \setcounter{subsubproblem}{0}
           186
               Defines 'plain' sectioning-commands. See 3.2 for more informations.
           187 \newcommand{\problem}[1]{\@startsection{problem}%Name
               {1}%Level
           188
```

{\z@}%indent

189

```
{char '2em \@plus char '1em \@minus char '1em}%beforeskip
190
                         {1ex \@plus .5ex}%afterskip
191
                         {\normalfont\Large\bfseries}%style
192
                         *{#1} \addcontentsline{toc}{section}{#1} }
193
194
195 \newcommand{\subproblem}[1]{\@startsection{subproblem}%Name
196
                      {2}%Level
                         {\z@}%indent
197
                      {char '1em \@plus char '.5em \@minus char '.5em}%beforeskip
198
                      {.5ex \@plus .5ex}%afterskip
199
                         {\normalfont\large\bfseries}%style
200
                         *{#1} \addcontentsline{toc}{subsection}{#1} }
201
203 \newcommand{\subsubproblem}[1]{\@startsection{subsubproblem}\%Name
                      {3}%Level
204
                      {\z_0}\%indent
205
                     {char '.5em}%beforeskip
206
                     {.5em}%afterskip
207
                      {\normalfont\bfseries}%style
209
                         *{#1} }
210
211 \newcommand{\solution}[1][]{\@startsection{solution}%Name
                      {4}%Level
212
                         {\parindent}%indent
213
                         {char '.1em}%beforeskip
214
                         {\z@}%afterskip
                          {\normalfont\bfseries}%style
216
                           *{\operatorname{CetTranslation}} \operatorname{loesung} \operatorname{loesung} \operatorname{loesung} { \#1}{} { } { } { } #1}: \begin{tikzpicture}(3.5,0.5) \begin{tikzpicture}(3
217
218
219 \mbox{\ensuremath{\mbox{\sc tion{proof}}\hspace}} [1] [] {\c tartsection{proof}\hspace, was a second of the content of t
                    {4}%Level
220
221
                      {\parindent}%indent
                     {char '.1em}%beforeskip
                      {\z@}%afterskip
223
                         {\normalfont\bfseries}%style
224
                         {\colored{0.5cm} *{\colored{0.5cm} *{\colored{0.5cm} {\colored{0.5cm} {\
225
226
227 \newcommand{\toShow}[1][]{\@startsection{to show}%Name
228
                     {4}%Level
                         {\parindent}%indent
229
230
                       {char '.1em}%beforeskip
231
                      {\z@}%afterskip
                       {\normalfont\bfseries}%style
232
                        *{\GetTranslation{zuZeigen}\ifthenelse{\equal{#1} {} } {} #1}:~~ } }
233
234
235 \newcommand{\given}[1][]{\@startsection{given}%Name
236
                      {4}%Level
237
                      {\parindent}%indent
                     {char '.1em}%beforeskip
238
239 {\z0}%afterskip
```

```
 *{\GetTranslation{gegeben}\  \  } {} {} {} {} {} {} {} {} 
                                 241
                                 242
                                      Defines 'better' sectioning commands. See 3.2 and 3.2.2 for more informations.
                                 243 \newcommand{\newproblem}[1][]{\stepcounter{problem}
                                       \ifthenelse{\equal{#1}{}} { } {\setcounter{problem}{#1}}
                                 244
                                       \problem{\GetTranslation{aufgabe} \hwa@problemno} }
                                 245
                                 247 \newcommand{\newsubproblem}[1][]{\stepcounter{subproblem}
                                       \ifthenelse{\equal{#1}{}} { } {\setcounter{subproblem}{#1}}
                                 248
                                       \subproblem{\GetTranslation{aufgabe} \hwa@problemno{}.\hwa@subproblemno} }
                                 249
                                 250
                                 251 \newcommand{\newsubsubproblem}[1][]{\stepcounter{subsubproblem}
                                       \ifthenelse{\equal{#1}{}} { } {\setcounter{subsubproblem}{#1}}
                                 252
                                 253
                                       \subsubproblem{\hwa@subsubproblemno)} }
                                 254
                   End of Proof
                                 255 \newcommand{\QED}{\begin{flushright}
                                         \textit{QED}
                                 256
                                       \end{flushright}
                                 257
                                 258 }
                                 259 \newcommand{\EOP}{\begin{flushright}
                                         $\square$
                                 261
                                       \end{flushright}
                                 262 }
                                 263 \newcommand{\eop}{\hfill$\blacksquare$}
demonstrandum at iucundum est
                                 264 \newcommand{\QNED}{\begin{flushright}
                                 265
                                         $\triangle$
                                 266
                                       \end{flushright}
                                 267 }
                                 268 \mbox{newcommand} {\qned}{\fill} \
                                  The following Macros are all stolen (and adapted) from occloxium (see 3.4)
       Math Common Set Symbols
                                 269 \mbox{newcommand{N}{\operatorname{N}}{\operatorname{mathbb{N}}}}
                                 270 \mbox{newcommand}\{Z\}{\mbox{cmath}\{\mathbb{Z}\}}
                                 271 \mbox{newcommand}(R){\mbox{ensuremath}(\mathbb{R})}
                                 272 \mbox{ newcommand} \Q}{\mbox{ ensuremath} \mbox{ mathbb} \Q}}
                                 273 \newcommand{\C}{\ensuremath{\mathbb{C}}}}
                                 274 \mbox{newcommand}(F){\mbox{mathbb}{F}}
                                 275 % The last one is mine
                                 276 \newcommand{\Primes}{\ensuremath{\mathbb{P}}}
        Mathematical Functions
                                 277 \newcommand{\GL}{\ensuremath{\text{GL}}}}
```

{\normalfont\bfseries}%style

240

```
278 \mbox{newcommand}(\id){\ensuremath}
                                                                                        279 \newcommand{\diff}[1]{\ensuremath{\frac{d}{d#1}}}
                                                                                        280 \mbox{newcommand} \dx}{\:dx}
Mathematical Functions
                                                                                        281 \newcommand{\divides}{\ensuremath{\ |\ }}
                                                                                        282 \newcommand{\property}{\ensuremath{\ |\ }}
                                                                                        284 \newcommand{\Var}{\ensuremath{\text{Var}}}
                                                                                        285 \newcommand{\Perm}{\ensuremath{\text{Perm}}}}
                                                                                        286 \mbox{\comb}{\comb}}
                                                                                        287 \newcommand{\Comb}{\ensuremath{\text{Comb}}}}
                                                                                        289 \renewcommand{\dim}[1][]{\ensuremath{\text{dim}_{#1}\}}
                                                                                        290 \renewcommand{\Im}{\ensuremath{\text{Im}\\}}
                                                                                        291 \newcommand{\modulo}[2]{#1/\!\!#2\:}
                                                                                        293 \mbox{Pot}{\command{\Pot}}
                                                                                        294 \newcommand{\Map}{\ensuremath{\text{Map}}}}
                                                                                        295
                                                                                        296 \newcommand{\excup}{\ensuremath{\stackrel{.}{\cup}}}
                                                                                        298 \newcommand{\falls}{\text{\ \GetTranslation{falls}}\ }
                                                                                        299
                                                                                        300 \newcommand{\Bin}{\ensuremath{\text{Bin}\ }}
                                                                                        301 \renewcommand{\char}{\ensuremath{\text{char}\\}}
                   Math Big Quantors
                                                                                        302 \let\oforall\forall
                                                                                        303 \let\oexists\exists
                                                                                        304 \ensuremath{\hskip 2pt \oforall \hskip 2pt}}
                                                                                        305 \renewcommand{\exists}{\ensuremath{\hskip 2pt \oexists \hskip 2pt}}
                                                                                        306 \newcommand{\bigforall}{\mbox{\raisebox{char '2pt}[\height][\depth]{\Large $\mathsurround4pt\fo
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